

$$\text{Degree of saturation } (s_r) \text{ for Bulk soil} = \frac{v_w}{v_v} \quad \text{when } v_a = 0 \text{ and } v_w = 0 \text{ is } (v_v = 0, v_s = v_t, S = 0)$$

$$\text{Degree of saturation } (s_{r_{min}}) \text{ for Dry soil} = \frac{v_w}{v_v} = \frac{0}{v_a} = 0 \quad \text{S not may be } < 0$$

$$\text{Degree of saturation } (s_{r_{max}}) \text{ for saturated soil} = \frac{v_w}{v_v} = \frac{v_v}{v_w} = 1 \quad \text{S not may be } > 1 \quad 0 < S < 1$$

$$\text{The air content } (A) \text{ for Bulk soil} = \frac{v_a}{v_t}$$

$$\text{The air content } (A_{max}) \text{ for Dry soil} = \frac{v_a}{v_t} = \frac{v_v}{v_t} = n \quad \text{at } v_a = v_v \quad A_{max} = n \quad A \text{ not may be } > n$$

$$\text{The air content } (A_{min}) \text{ for saturated soil} = \frac{v_a}{v_t} = \frac{0}{v_t} = 0 \quad \text{at } v_a = 0 \quad A_{min} = 0 \quad A \text{ not may be } < 0$$

(Mass-Mass) Or (Weight - Weight) Relation

$$\text{Water content } (w_c) = \frac{M_w}{M_s} \quad \text{Or} \quad = \frac{W_w}{W_s} \quad \text{at Dry soil } (wc) = 0 \quad \text{at Sat soil } (wc) = wc_{max}$$

(Mass Or Weight) -Volume Relation

$$\text{Bulk density } (\rho) = \frac{M_t}{v_t} = \frac{Gs\rho_w(1+w)}{1+e} = \frac{\rho_w(Gs+se)}{1+e} \quad \text{Or moist unit weight } (\gamma) = \frac{W_t}{v_t} = \frac{Gs\gamma_w(1+w)}{1+e} = \frac{\gamma_w(Gs+se)}{1+e}$$

$$\text{Solid density } (\rho_s) = \frac{M_s}{v_s} \quad \text{Or solid unit weight } \gamma_{solid} = \frac{W_s}{v_s}$$

$$\text{Dry density } (\rho_{dry}) = \frac{M_s}{v_t} = \frac{\rho_w Gs}{1+e} \quad \text{Or dry unit weight } \gamma_{dry} = \frac{W_s}{v_t} = \frac{\gamma_w Gs}{1+e}$$

$$\text{Saturated density } (\rho_{sat}) = \frac{M_t}{v_t} = \frac{\rho_w(Gs+e)}{1+e} \quad \text{Or saturated unit weight } \gamma_{sat} = \frac{W_t}{v_t} = \frac{\gamma_w(Gs+e)}{1+e}$$

$$\rho_{(effective/Bount/Submerged)} = \rho_{sat} - \rho_w \quad \text{Or effective unit weight } \gamma_{(effective/Bount/Submerged)} = \gamma_{sat} - \gamma_w$$

Derived Relation:

$$\gamma_{dry} = Gs\gamma_w(1-n)$$

$$\gamma_{sat} = \gamma_{dry} + n\gamma_w$$

$$\gamma = \gamma_w Gs(1+w)(1-n)$$

$$w_c Gs = se$$

$$A = \frac{e - wc Gs}{1+e} \quad \text{Or } A = n(1-s)$$

$$e = \frac{n}{1-n}$$

$$Gs = \frac{\rho_s}{\rho_w} = \frac{M_s}{v_s \rho_w} = \frac{M_s v_w}{v_s M_w}$$

$$\rho_{dry} = \frac{\rho}{1+w} \quad \text{Or } \gamma_{dry} = \frac{\gamma}{1+w}$$

$$\gamma_{(effective/Bount/Submerged)} = \frac{\gamma_w(Gs-1)}{1+e} = \frac{\gamma_{dry}(Gs-1)}{Gs}$$

$$\rho_{dry} = \frac{\rho_{solid}}{1+e} \quad \text{Or } \gamma_{dry} = \frac{\gamma_{solid}}{1+e}$$

$$\rho_{dry} = \frac{\rho_{sat}}{1+w_{sat}} \quad \text{Or } \gamma_{dry} = \frac{\gamma_{sat}}{1+w_{sat}}$$

$$n = \frac{e}{1+e}$$

Volume -Volume Relation

$$\text{void ratio } (e) \text{ for Bulk soil} = \frac{v_v}{v_s} \quad \text{when } v_v = 0 \text{ is } (v_s = v_t, e = 0) \text{ and when } v_v = v_s \text{ is } (v_t = 2v_v, e = 1)$$

$$\text{void ratio } (e) \text{ for Dry soil} = \frac{v_v}{v_s} = \frac{v_a}{v_s} \quad \text{when } v_a = 0 \text{ is } (v_s = v_t, e = 0) \text{ and when } v_a = v_s \text{ is } (v_t = 2v_a, e = 1)$$

$$\text{void ratio } (e) \text{ for sat soil} = \frac{v_v}{v_s} = \frac{v_w}{v_s} \quad \text{when } v_w = 0 \text{ is } (v_s = v_t, e = 0) \text{ and when } v_w = v_s \text{ is } (v_t = 2v_w, e = 1)$$

e may be > 1 and e not may be < 0

$$\text{Porosity } (n) \text{ for Bulk soil} = \frac{v_v}{v_t}$$

$$\text{when } v_a = 0 \text{ and } v_w = 0 \text{ is } (v_v = 0, v_s = v_t, n = 0)$$

$$\text{Porosity } (n) \text{ for Dry soil} = \frac{v_v}{v_t} = \frac{v_a}{v_t}$$

$$\text{when } v_a = 0 \text{ is } (v_v = 0, v_s = v_t, n = 0)$$

$$\text{Porosity } (n) \text{ for saturated soil} = \frac{v_v}{v_t} = \frac{v_w}{v_t}$$

$$\text{when } v_w = 0 \text{ is } (v_v = 0, v_s = v_t, n = 0)$$

$$0 < n < 1$$

$$Dr \text{ or } Ir = \frac{e_{max} - e}{e_{max} - e_{min}} \quad \text{is } 0 < Dr < 1$$

$$Dr \text{ or } Ir \text{ for Dense or Compact soil } (e = e_{min}) = \frac{e_{max} - e_{min}}{e_{max} - e_{min}} = 1 \quad \text{is } Dr_{max}$$

$$Dr \text{ or } Ir \text{ for Loose soil } (e = e_{max}) = \frac{e_{max} - e_{max}}{e_{max} - e_{min}} = 0 \quad \text{is } Dr_{min}$$

$$\text{Compactive effort (energy E)} = \frac{\text{Weight of hammer} \times \text{Height of drop hammer} \times \text{Number of blows per layer} \times \text{Number of layers}}{\text{Volume of mold}}$$

Number of layer:

Standard Test = 3 layers

Modified Test = 5 layers

Height of drop of hammer:

Standard Test = 305 mm

Modified Test = 450 mm

Weight of hammer:

Standard Test = 2.5 Kg ~5.5 lb

Modified Test = 4.5 Kg ~10 lb

$$\text{Number of blows per layer} = 25 \quad \text{Volume of mold} = 0.944 \times 10^{-3} \text{ m}^3$$

$$\frac{E_{\text{Modified}}}{E_{\text{Standard}}} = 4.4$$

$$\rho_d = \frac{\rho_s}{1 + e} = \frac{\rho_w \times S}{w_c + \frac{\rho_w}{\rho_s} \times S} = \frac{\rho_w \times S}{w_c + \frac{S}{G_S}} = \frac{\rho_w G_S}{1 + e}$$

$$R.C = \frac{\rho_d - \text{field}}{\rho_d - \text{max-laboratory}}$$

$$R.C = 80 + 0.2 \times D_r$$

*R.C > 95% accepted
o.p.t ± 2% accepted*

$$Cu = \frac{D_{60}}{D_{10}}$$

$1 < Cc < 3$ Cu ≥ 4 Well graded for Gravel
 $1 < Cc < 3$ Cu ≥ 6 Well graded for Sand

$$Cc = \frac{D_{30}^2}{D_{10} \times D_{60}}$$

Cu = 1 uniform soil (one grain soil)

$$SL = w_f(\%) - \Delta w(\%) = \left(\frac{M_1 - M_2}{M_2} \right) \times 100 - \left(\frac{V_1 - V_2}{M_2} \right) \times \rho_w \times 100$$

$$LL = w_u \left(\frac{N}{25} \right)^{\tan \theta = 0.123}$$

$$PI = LL - PL$$

SATURATED SOIL

V_s

DRY SOIL

V_d

M_s

M_d

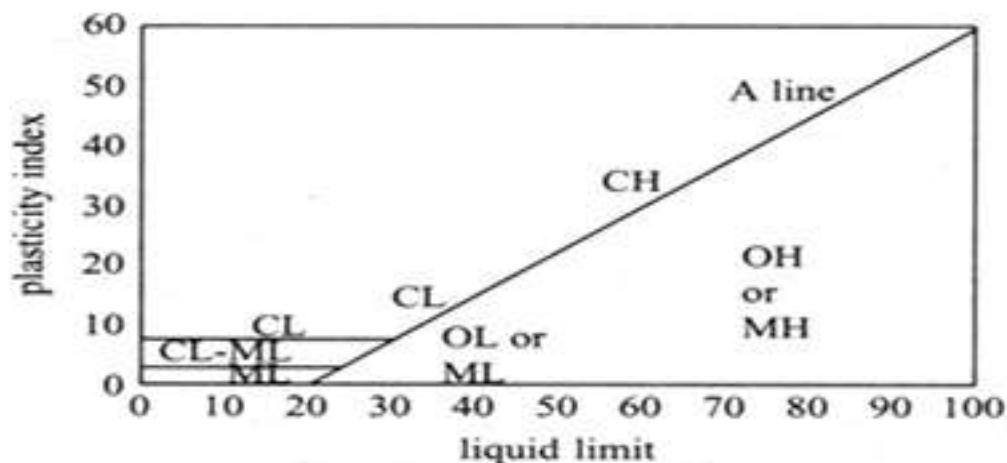
LL < 0 : brittle fracture if sheared

0 < LL < 1 : Plastic solid fracture if sheared

LL > 0 : viscous liquid if sheared

$$A = \frac{PI}{\% \text{ clay fraction (Wt)}} < 0.002 \text{ mm}$$

$$St = \frac{\text{strength(undisturbed)}}{\text{strength(disturbed)}}$$



LL_{Oven dry} < 0.75 LL_{Air dry} **Organic**
LL_{Oven dry} ≥ 0.75 LL_{Air dry} **Not Organic**

*A Line PI = 0.73(LL - 20) > PI_Silt
A Line PI = 0.73(LL - 20) < PI_Clay
U Line PI = 0.9(LL - 20)*

Passing #200 < 50%

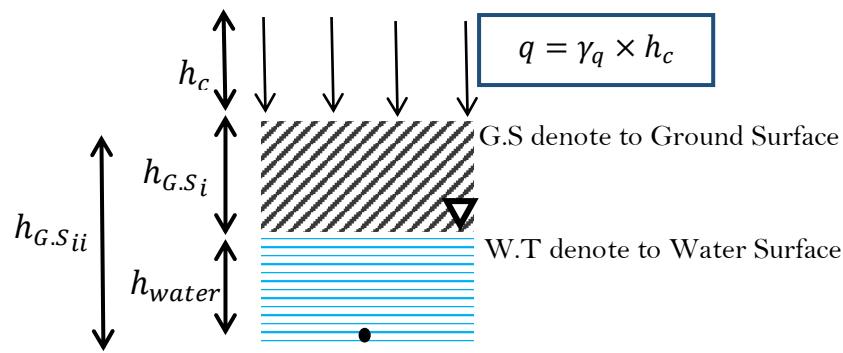
Coarse grain soil

COARSE More than 50% retained sieve #200	Gravel: more than 50% coarse fraction retained on sieve #4	Less than 5% fines	$C_s > 4, 1 \leq C_c \leq 3$	→ GW
		More than 12% fines	Not satisfying GW	→ GP
Passing #200 < 50%	Sand: less than 50% coarse fraction retained on sieve #4	Less than 5% fines	$C_s > 6, 1 \leq C_c \leq 3$	→ SW
		More than 12% fines	Not satisfying SW	→ SP
Coarse grain soil		Below 'A' line	Above 'A' line	→ GM
		Above 'A' line	Below 'A' line	→ GC
				→ SM
			Above 'A' line	→ SC

Assume the soil above the surface of the water
Dry Or Bulk Soil and below **Saturated Soil**.

$$\text{Stress} = \frac{\text{Weight}}{\text{Area}} = \gamma \times h \text{ Unit } \frac{\text{KN}}{\text{m}^2}$$

$$u = \gamma_{\text{water}} \times h_{\text{water}}. (\gamma_{\text{water}} = 9.81 \text{ KN/m}^2)$$



$$\sigma_{\text{effective}} = \Sigma(\gamma_{\text{effective}} \times h_{G.S})$$

$$\text{for - Saturated Soil } \gamma_{\text{effe}} = (\gamma_{\text{sat}} - \gamma_w).$$

$$-\text{Bulk Or Dry Soil } \gamma_{\text{effe}} = \gamma_{\text{Bulk}} \text{ Or } \gamma_{\text{Dry}}.$$

$$\sigma_{\text{total}} = \Sigma(\gamma_{\text{total}} \times h_{G.S})$$

$$\text{for - Saturated Soil } \gamma_{\text{total}} = \gamma_{\text{sat}}.$$

$$-\text{Bulk Or Dry Soil } \gamma_{\text{total}} = \gamma_{\text{Bulk}} \text{ Or } \gamma_{\text{Dry}}.$$

$$\sigma_{\text{effective}} = q + \Sigma(\gamma_{\text{effective}} \times h_{G.S})$$

$$\sigma_{\text{total}} = q + \Sigma(\gamma_{\text{total}} \times h_{G.S})$$

$$u = \gamma_{\text{water}} \times h_{\text{water}}$$

q only added to $\sigma_{\text{effective}}$ and σ_{total}

-q = 0 (Immediately).

.-q = be considered (Many years after the fill)

$$\Delta\sigma_z = \frac{3Pz^3}{2\pi L^5} = \frac{3P}{2\pi} \frac{Z^3}{(r^2 + z^2)^{5/2}} = \frac{P}{z^2} I_1 \text{ for point load.}$$

$$I_1 = \frac{3}{2\pi} \frac{1}{\left(\left[\frac{r}{z}\right]^2 + 1\right)^{5/2}} \text{ for point load.}$$

$$\Delta\sigma_z = \frac{2qz^3}{\pi(x^2 + z^2)^2} = \frac{2q}{\pi z [(x/z)^2 + 1]^2} \text{ for Vertical stress by vertical line}$$

$$\Delta\sigma_z = \Delta\sigma_z = \frac{2q}{\pi} \frac{xz^2}{[x^2 + z^2]^2} \text{ for Vertical stress by horizontal line}$$

$$\Delta\sigma_z = q \left[1 - \frac{1}{\left[\left(\frac{R}{z} \right)^2 + 1 \right]^{3/2}} \right] \text{ for Vertical Stress below the Center of a Uniformly Loaded Circular Area}$$

$$\Delta\sigma_z = \frac{q}{\pi} \left[\left(\frac{\beta_1 + \beta_2}{\beta_2} \right) (\alpha_1 + \alpha_2) - \frac{\beta_1}{\beta_2} (\alpha_2) \right]$$

$$\alpha_1 = \left(\tan^{-1} \left(\frac{\beta_1 + \beta_2}{z} \right) - \tan^{-1} \left(\frac{\beta_1}{z} \right) \right) \times \frac{\pi}{180}$$

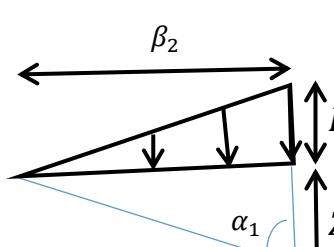
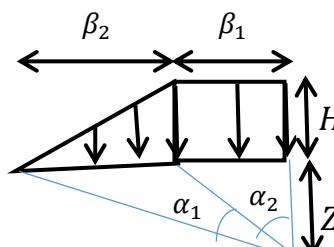
$$\alpha_2 = \tan^{-1} \left(\frac{\beta_1}{z} \right) \times \frac{\pi}{180}$$

$$\Delta\sigma_z = \frac{q\alpha_1}{\pi} \quad \alpha_1 = \tan^{-1} \left(\frac{\beta_2}{z} \right) \times \frac{\pi}{180}$$

$$q = \gamma H$$

γ = unit weight of the embankment

H = height of the embankment



$$m = \frac{L \text{ or } B}{z} \quad n = \frac{L \text{ or } B}{z}$$

$\Delta\sigma_z = q I_3$ for Vertical Stress Caused
Loaded Area by a Rectangular

$\Delta\sigma_z = q$ Surcharge load

$$\Delta\sigma_z = \frac{q \times B}{(B + Z)} \text{ Strip load}$$

$$\Delta\sigma_z = \frac{q \times B^2}{(B + Z) \times (B + Z)} \text{ Square load}$$

$$\Delta\sigma_z = \frac{q \times D^2}{(D + z) \times (D + z)} \text{ Circle load}$$

$$\Delta\sigma_z = \frac{q(B \times L)}{(B + z) \times (L + z)} \text{ Rectangular load}$$

$$k_x \frac{\partial^2 h}{\partial x^2} + k_z \frac{\partial^2 h}{\partial z^2} = 0 \text{ (Laplace equation of continuity)}$$

$k_x = k_z$ (isotropic soil)

$$i = \frac{\Delta h}{L}$$

$$i_{cr} = \frac{\gamma'}{\gamma_w} = \frac{\gamma - \gamma_w}{\gamma_w} = \frac{G_s - 1}{1 + e} \text{ at } \sigma_{eff} = 0$$

$v = ki$ at normal condition Or Darcy velocity

$v_{cr} = ki_{cr}$ at Critical condition

$v = ki$ (Discharge velocity Or Darcy velocity)

$$v_s = \frac{v}{n} = \frac{ki}{n} \text{ (Seepage velocity)}$$

$q = vA$ at normal condition

$q_{cr} = v_{cr}A$ at Critical condition

$q = vA$ by Area total

$q = v_s A_{voide}$ by Area Void

$k = 10^{-2} D_{10}^2$ For Clean Uniform sands (Hazan)

$$q = k \Delta H \frac{Nf}{Nd} \left(\begin{array}{l} \text{Seepage discharge or Flow rate} \\ \text{In isotropic soil } \frac{m^3}{sec}/m \end{array} \right)$$

$$\Delta h = \frac{\Delta H = H_1 - H_2}{Nd} \text{ (Head loss or Drop head m)}$$

$h_i = \Delta H - Nd_i \Delta h - z$ (Pressure head m)

$u_i = \gamma_w h_i = \gamma_w [\Delta H - Nd_i \Delta h - z]$ (Pour pressure m)

$$p_w = \frac{(u_i + u_{ii})}{2} \times L_{Dam} \text{ (pressure of water)}$$

or uplift force KN/m)

$$F.S = \frac{\text{The weight of the dam}}{\text{pressure of water}} \text{ (Factor of safety)}$$

against Uplift force) Wt. Dam = $\gamma_{concrete} \times A_{concrete}$

$$F.S = \frac{i_{cr}}{i_{exit}}$$
 (Factor of safety against piping force)

$$i_{exit} = \frac{\Delta h}{Lexit \text{ Or min}}$$

$$q = k \Delta H \frac{Nf}{Nd} = \sqrt{k_x \times k_z} \Delta H \frac{Nf}{Nd} \text{ (Anisotropic soil)}$$

$$k_{H_{eq}} = \frac{H_1 K_1 + H_2 K_2 + H_3 K_3}{H_1 + H_2 + H_3} \rightarrow \text{Diagram showing a soil profile with three layers and their respective coefficients of permeability.}$$

$$k_{V_{eq}} = \frac{H_1 + H_2 + H_3}{\left(\frac{H_1}{K_1}\right) + \left(\frac{H_2}{K_2}\right) + \left(\frac{H_3}{K_3}\right)} \rightarrow \text{Diagram showing a soil profile with three layers and their respective coefficients of permeability.}$$

$$\Delta \sigma_z = At t = 0$$

Δu Or u_e

Symbolized u_i

$$\sigma_{totalfinal} = \sigma_o + \Delta \sigma_z$$

$$u_{final} = u_o + \Delta \sigma_z$$

$$\sigma_{effefinal} = \sigma_o + \Delta \sigma_z - u_o$$

$$\Delta u = u_e = 0 \text{ at } t = \infty$$

$$\sigma_{totalfinal} = \sigma_o + \Delta \sigma_z$$

$$u_{final} = u_o$$

$$\sigma_{effefinal} = \sigma_o + \Delta \sigma_z - u_o$$

$$U_{avg} = \sqrt{\frac{4T\nu}{\pi}}$$

$$0 \leq T\nu \leq 0.197$$

$$U_{avg} = 1 - \frac{8}{\pi^2} e^{\frac{-\pi^2 T\nu}{4}}$$

$$T\nu > 0.197$$

$$T\nu = \frac{\pi}{4} U_{avg}^2$$

$$U \leq 0.60$$

$$T\nu = -0.933 \log(1 - U) - 0.085$$

$$U > 0.60$$

$$O.C.R = \frac{\sigma_p}{\sigma_o}$$

h: The distance from the surface of the soil in the middle of the clay layer.

Ho : Thick layer clay

-Normally Consolidation Clay (O.C.R) = 1 $\sigma_p = \sigma_o$

-Under Consolidation Clay (O.C.R) < 1 $\sigma_p < \sigma_o$

-Over Consolidation Clay (O.C.R) > 1 $\sigma_p > \sigma_o$

$$\Delta \sigma_z = \frac{1}{6} (\Delta \sigma_{z_{top}} + 4\Delta \sigma_{z_{mid}} + \Delta \sigma_{z_{bottom}})$$

$$\sigma_o = \gamma h \quad \sigma_f = \sigma_o + \Delta \sigma_z$$

$$1. S_f = H_o \frac{\Delta e}{(1 + e_0)}$$

$$S_f = m_v H_o \Delta \sigma_z$$

$$2. S_f = \frac{c_c}{(1 + e_0)} H_o \log \left(\frac{\sigma_f}{\sigma_o} \right)$$

$$\sigma_o < \sigma_f < \sigma_p \quad O.C.R \leq 1$$

$$3. S_f = \frac{c_r}{(1 + e_0)} H_o \log \left(\frac{\sigma_f}{\sigma_o} \right)$$

$$\sigma_o < \sigma_f < \sigma_p \quad O.C.R > 1$$

$$4. S_f = \frac{c_r}{(1 + e_0)} H_o \log \left(\frac{\sigma_p}{\sigma_o} \right) + \frac{c_c}{(1 + e_0)} H_o \log \left(\frac{\sigma_f}{\sigma_p} \right)$$

$$\sigma_o < \sigma_p < \sigma_f \quad O.C.R > 1$$

$$S_f = \frac{c_r}{(1 + e_0)} H_o \log \left(\frac{\sigma_f}{\sigma_o} \right) = -ve \quad \sigma_o > \sigma_f$$

$$U_{avg} = \frac{S_c}{S_f}$$

$$\frac{\partial u_e}{\partial t} = cv \frac{\partial^2 ue}{\partial z^2}$$

$$U_z = 1 - \frac{u_e}{\Delta \sigma_z} = u_i$$

$$T\nu = \frac{cv t}{dr^2}$$

$$t = 0 \quad U_z = 0$$

$$t = \infty \quad U_z = 1$$

$$K = c_v m_v \gamma_w$$

$$\tau = c + \sigma \tan \phi$$

$$\sigma f' = \frac{\sigma_1' + \sigma_3'}{2} + \frac{\sigma_1' - \sigma_3'}{2} \cos 2\theta$$

$$\sigma T f = \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos 2\theta$$

$$\begin{aligned}\tau f &= \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta \\ \theta &= 45^\circ + \frac{\phi}{2}\end{aligned}$$

$$\sin \phi' = \frac{\frac{\sigma_1' - \sigma_3'}{2}}{c' \cot \phi' + \frac{1}{2}(\sigma_1' + \sigma_3')}$$

$$\sigma_1' = \sigma_3' \tan^2 \left(45^\circ + \frac{\phi'}{2} \right) + 2c' \tan \left(45^\circ + \frac{\phi'}{2} \right)$$

$$\sigma f' = \frac{\sigma_1' + \sigma_3'}{2} - \frac{\sigma_1' - \sigma_3'}{2} \sin \phi'$$

$$\sin \phi T = \frac{\sigma_1 - \sigma_3}{\sigma_1 + \sigma_3} \quad \text{if } c = 0$$

ϕ = Angle of friction
 θ = Angle of failure

$$\begin{aligned}\tau f' &= \frac{\sigma_1' - \sigma_3'}{2} \sin 2\theta \\ \theta &= 45^\circ + \frac{\phi'}{2}\end{aligned}$$

UU Test:

$$\begin{aligned}\phi T &= \phi u = 0 \\ su &= cu = \frac{\sigma_1 - \sigma_3}{2}\end{aligned}$$

V = Constant

U = Unknown

su = Undrained Shear Strength

Mohr – Coulomb Circle:

$$\text{Center} = \frac{\sigma_1 + \sigma_3}{2}$$

$$r = \frac{\sigma_1 - \sigma_3}{2}$$

$$\theta_3 = 45 + \frac{\phi}{2}$$

$$\theta_1 = 45 - \frac{\phi}{2}$$

CD Test:

$$\sigma f' = \frac{\sigma_1' + \sigma_3'}{2} - \frac{\sigma_1' - \sigma_3'}{2} \sin \phi'$$

$$\phi' = \sin^{-1} \left(\frac{\sigma_1' - \sigma_3'}{\sigma_1' + \sigma_3'} \right)$$

$$\begin{aligned}U &= 0 \\ \sigma T &= \sigma'\end{aligned}$$

CU Test:

$$\sigma_1 = \sigma_3 + \Delta \sigma d$$

$$\sigma_3' = \sigma_3 - U f$$

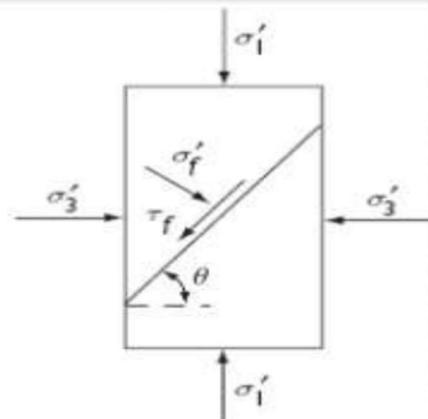
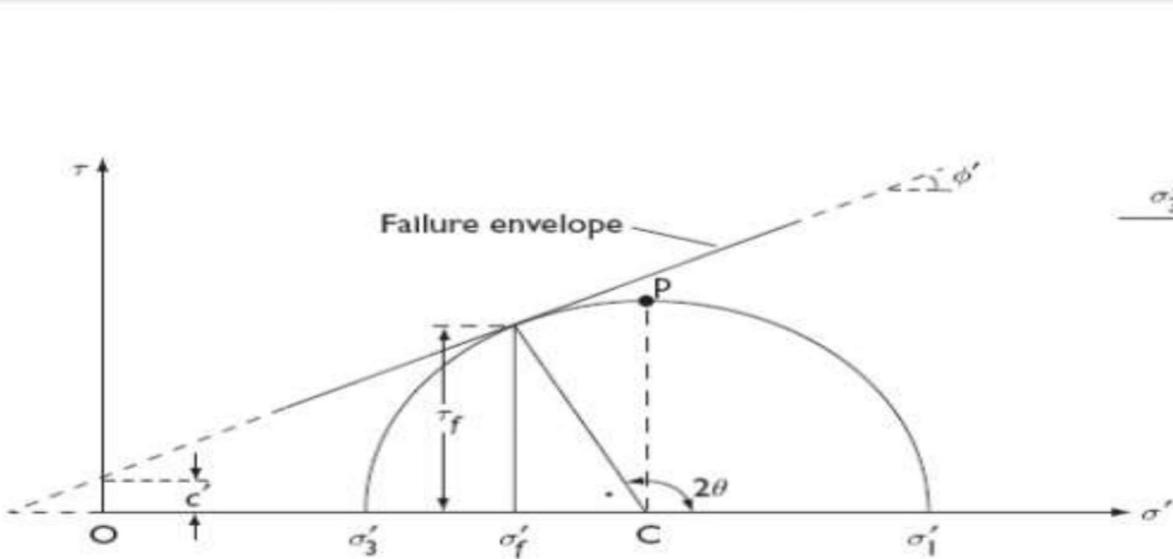
$$\sigma_1' = \sigma_1 - U f$$

$$\begin{aligned}\phi' &> \phi \\ cr &> c'\end{aligned}$$

Sand Normally Consolidated Clay $c = 0$

Over Consolidated Clay $c \neq 0$

$$\phi' = 2 \left[\tan^{-1} \left(\frac{\sigma_1'(I) - \sigma_1'(II)}{\sigma_3'(I) - \sigma_3'(II)} \right)^{0.5} - 45^\circ \right] \quad \text{for two specimens}$$



$$\tau_f = C + \sigma_f \times \tan(\phi)$$

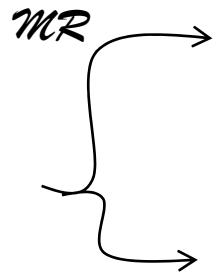
τ : shear strength of soil

C : cohesion intercept

ϕ : angle of friction

σ : total normal stress

on the failure plane



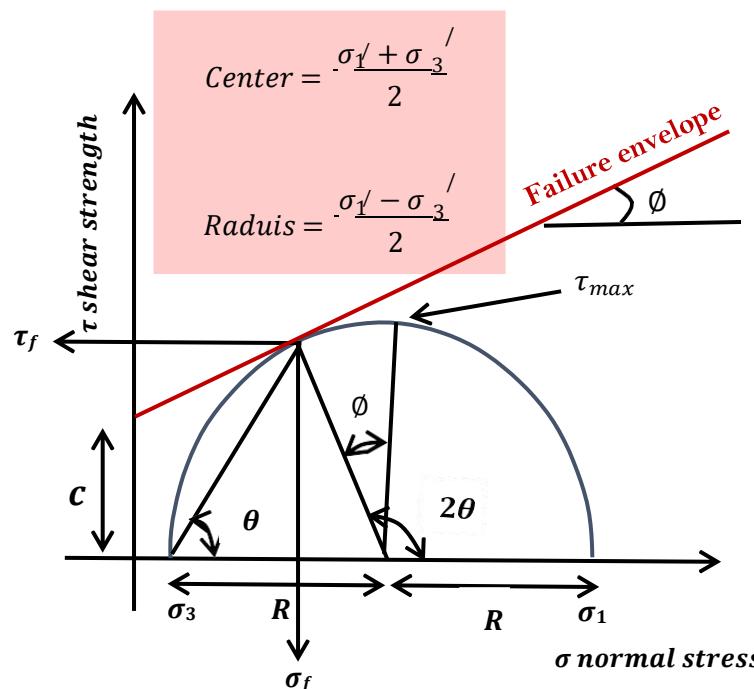
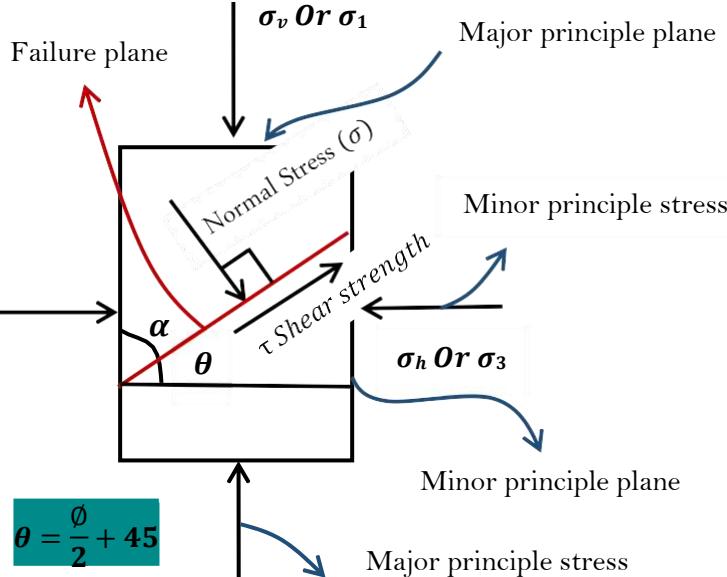
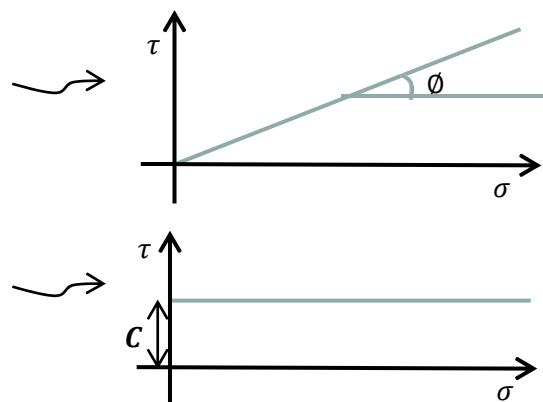
Sandy Soil Or
Normal Consolidated Clay

$$C: 0 \quad \tau_f = f \times \tan(\phi)$$

Clayey Soil

$$\phi: 0 \quad \tau = C$$

C and ϕ shear parameter



$$\tau_f = \frac{1}{2}(\sigma_1 - \sigma_3)\sin(2\theta)$$

$$\sin(\phi) = \frac{\frac{1}{2}(\sigma_1 - \sigma_3)}{C \cot(\phi) + \frac{1}{2}(\sigma_1 + \sigma_3)}$$

$$\sigma_f = \frac{1}{2}(\sigma_1 + \sigma_3) + \frac{1}{2}(\sigma_1 - \sigma_3) \cos(2\theta)$$

$$\sigma_1 = \sigma \tan^2(45 + \frac{\phi}{2}) + 2C \tan(45 + \frac{\phi}{2})$$

Direct shear test (Shear box test).

Function of effective stress $\tau = \sigma' / \times \tan(\phi') + C'$

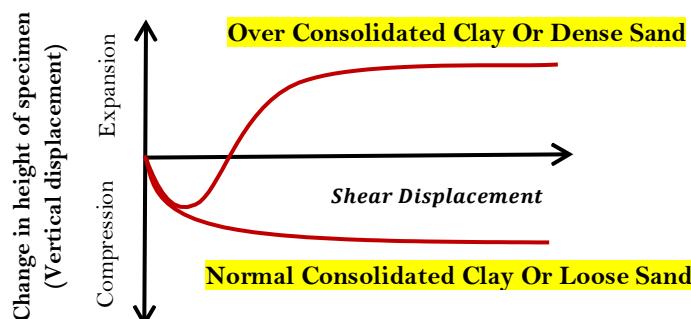
$$\text{Normal force}(\sigma) = \frac{\text{Normal force}}{\text{Cross-sectional area of the specimen}}$$

$$\text{Shear force}(\tau) = \frac{\text{Resisting Shear force}}{\text{Cross-sectional area of the specimen}}$$

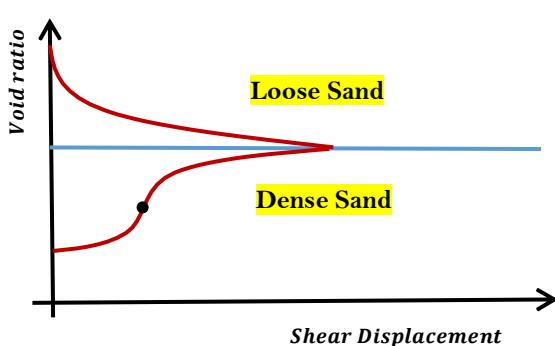
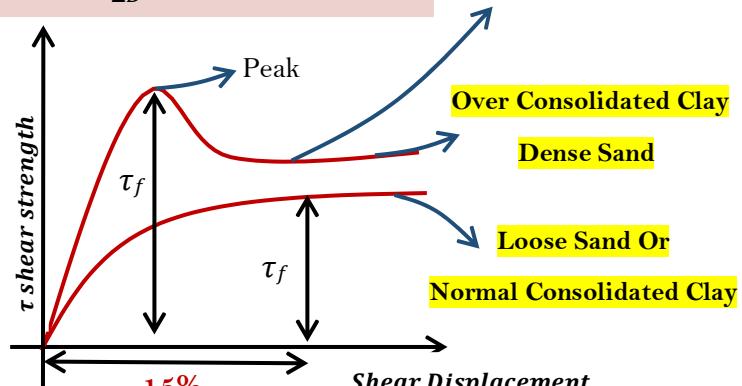
$$C = C' \text{ and } \phi = \phi' \text{ and } \sigma = \sigma' - U = \sigma' - 0 = \sigma'$$

Over Consolidated Clay Residual $C' = 0$

Over Consolidated Clay peak $C' \neq 0$ & $\phi \neq 0$



$$\text{Slope} = E_s = \frac{\Delta t}{\Delta D} = \text{modulus of elasticity}$$



Triaxle Test

1. (CD) Or (S) Test.

Function of effective stress $\tau = \sigma / \tan(\phi') + C'$

$$\text{Axial Strain } (\varepsilon_a) = \frac{\Delta h}{h}$$

$$\text{Volume Strain } (\varepsilon_V) = \frac{\Delta V}{V}$$

Find $C' \text{ & } \phi'$

2. (CU) Or (R) Test.

Function of effective stress $\tau = \sigma / \tan(\phi') + C'$

Function of total stress $\tau = \sigma \times \tan(\phi) + C$

Find $C' \text{ & } \phi' \text{ & } C \text{ & } \phi$

2. (UU) Or (Q) Test

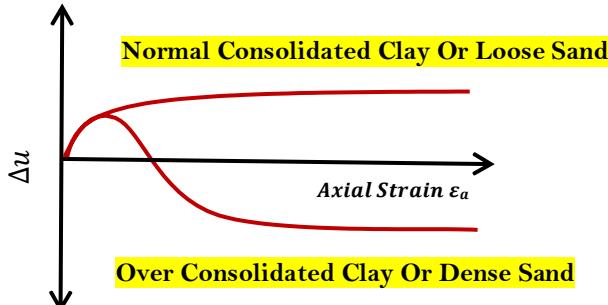
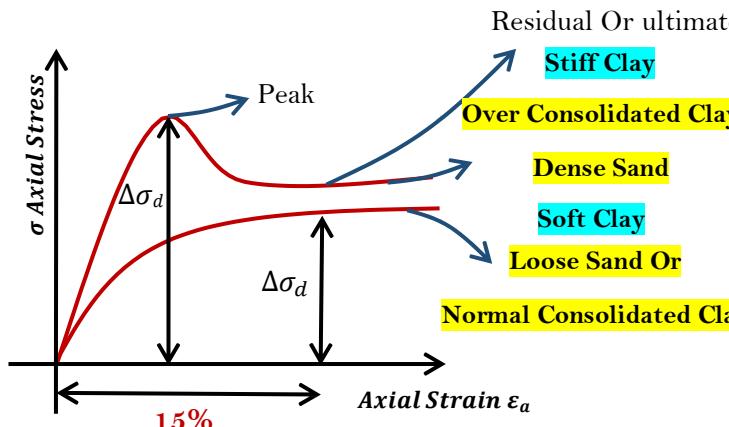
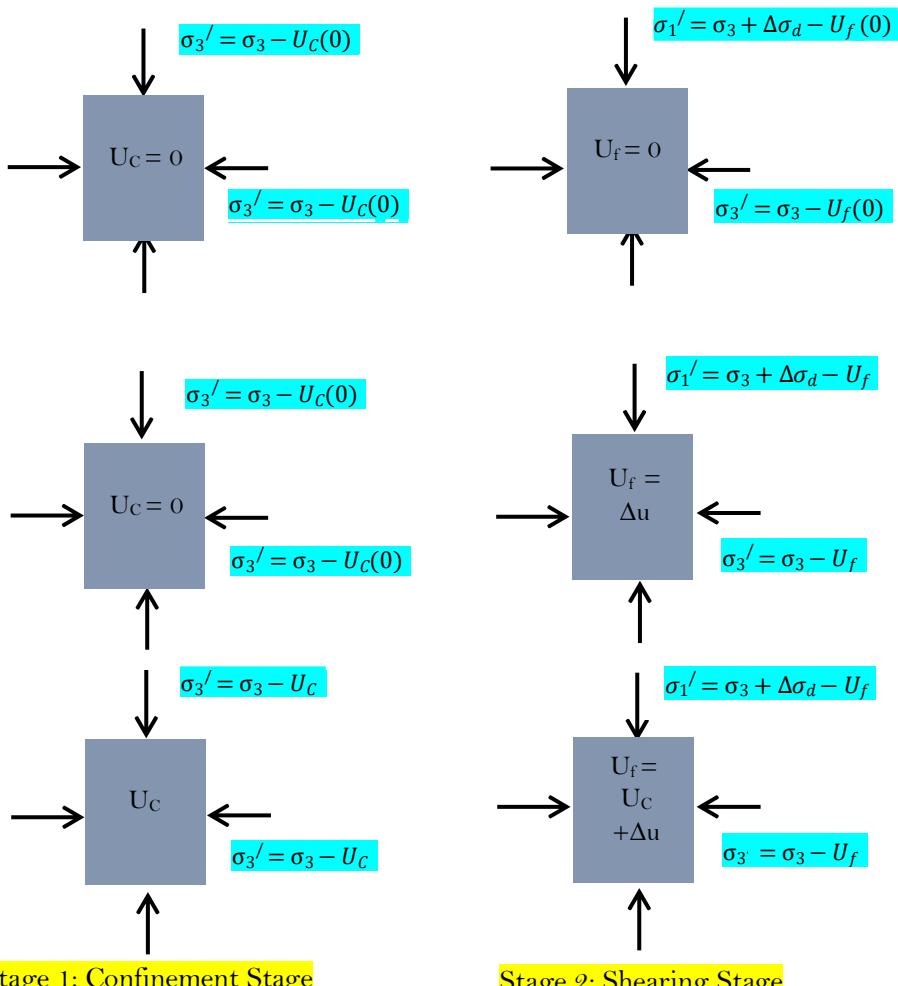
Function of total stress $\tau = \sigma \times \tan(\phi) + C$

$$S = 100\% \quad \phi = 0, C = C_{max}$$

$$S < 100\% \quad \phi > 0, C < C_{max}$$

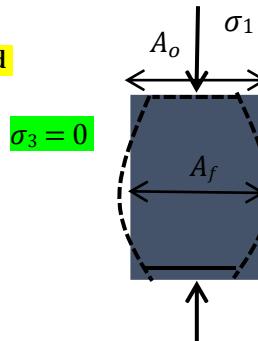
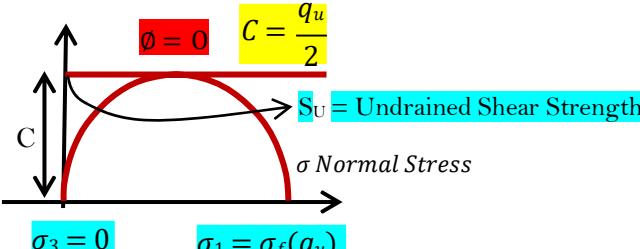
$$A_f = \frac{A_o}{(1 - \varepsilon_a)}$$

Find $C \text{ & } \phi$



Note for A Consolidated – Undrained triaxle test

τ shear strength



$$\phi = 2 \left(\tan^{-1} \left(\frac{\sigma'_1(I) - \sigma'_1(II)}{\sigma'_3(I) - \sigma'_3(II)} \right)^{0.5} - 45 \right)$$

S_u for NC

$$\frac{S_u}{P_o'} = 0.45(PI)^{\frac{1}{2}} \quad PI \text{ in decimal and } > 0.5$$

$$\frac{S_u}{P_o'} = 0.11 + 0.0037PI \quad PI \text{ in percent}$$

$S_u = \text{Undrained Shear Strength}$

$P_o' = \text{In Situ overburden stress}$

$PI = \text{plasticity index}$

$$q_u = \sigma_f = \frac{P_f}{A_f}$$

$$A_f = \frac{A_o}{(1 - \varepsilon_a)}$$

$$(\varepsilon_a) = \frac{\Delta h}{h}$$

$$(O.C.R)^{0.8} = \frac{\left(\frac{C_u}{P_o'} \right)_{\text{over consolidated clay}}}{\left(\frac{C_u}{P_o'} \right)_{\text{normally consolidated clay}}}$$

$$\frac{C_u}{P_o'} = (0.23 \pm 0.04)(O.C.R)^{0.5}$$