



# Civilittee

اللجنة الأكاديمية لقسم الهندسة المدنية

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15.4 | Obtaining the Value of the electric field from the electric potential

$$V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{s}$$

$\vec{E}$  is the electric field  
 $d\vec{s}$  is the differential displacement vector

$$dV = -\vec{E} \cdot d\vec{s}$$

If the electric field has only one component,  $E_x$   
 $\vec{E} = E_x \hat{i}$

$$d\vec{s} = dx \hat{i} + dy \hat{j} + dz \hat{k}$$

$$\vec{E} \cdot d\vec{s} = E_x dx$$

$$E_x = - \frac{dV}{dx} \rightarrow \text{relation}$$

$$E_x = - \frac{\partial V}{\partial x}$$

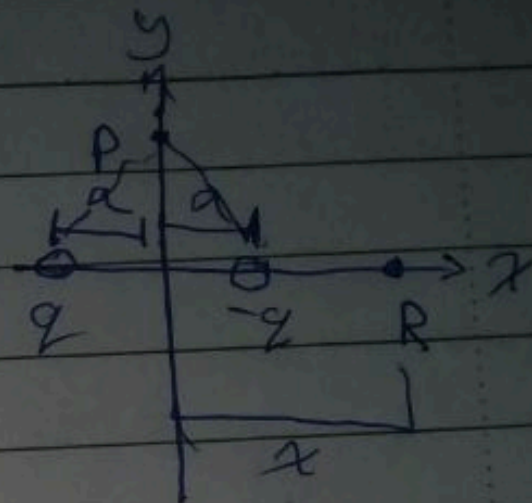
$$E_y = - \frac{\partial V}{\partial y}$$

$$E_z = - \frac{\partial V}{\partial z}$$



$$\Sigma x \quad 125.41$$

$$V_P ? \quad y = ?$$



$$1) V_P = k \left( \frac{q}{r_1} + \frac{-q}{r_2} \right)$$

$$= kq \left( \frac{1}{\sqrt{a^2 + y^2}} - \frac{1}{\sqrt{a^2 + y^2}} \right)$$

$$\boxed{V_P = 0}$$

$V = 0 \leftarrow y$ -axis is the perpendicular bisector

$$2) V_R = k \left( \frac{q}{x-a} - \frac{q}{x+a} \right)$$

$$= \frac{-2kq}{(x^2 - a^2)}$$

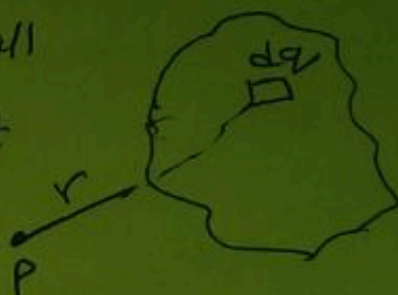


## Ex 25.5 | Electric potential due to continuous charge distributions:-

- The electric potential due to a small charge element  $dq$  at point  $P$  a distance  $r$  from  $dq$  is

$$\int dV = \int k \frac{dq}{r}$$

\*  $dq$ : small charge element



- sum over all charge elements (integration)

$$V = k \int \frac{dq}{r}$$

$dq \rightarrow \lambda dL \rightarrow$  line charge distribution.

$dq \rightarrow \sigma dA \rightarrow$  surface charge distribution.

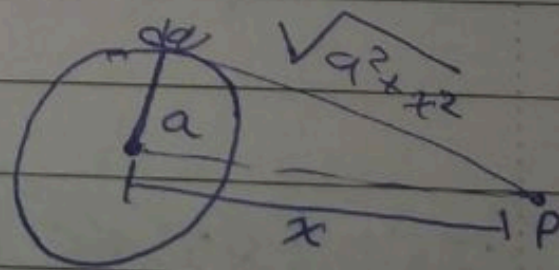
$dq \rightarrow \rho dv \rightarrow$  Volume charge distribution.

### Ex. 25.5 |

$$V = k \int \frac{dq}{\sqrt{a^2 + x^2}}$$

$\underbrace{\hspace{1cm}}_{Q}$

$$r = \sqrt{a^2 + x^2}$$



$$V = \frac{kQ}{\sqrt{a^2 + x^2}}$$



B)  $V = \frac{kQ}{\sqrt{x^2 + a^2}} \xrightarrow{\text{Gradient}} E = -\frac{\partial V}{\partial x}$

$$E = kQ \frac{x}{\sqrt{(x^2 + a^2)^3}} \rightarrow \left( -\frac{1}{2} \times 2x (x^2 + a^2)^{-3/2} \right)$$

$$\rightarrow \frac{kxQ}{\sqrt{(x^2 + a^2)^3}}$$

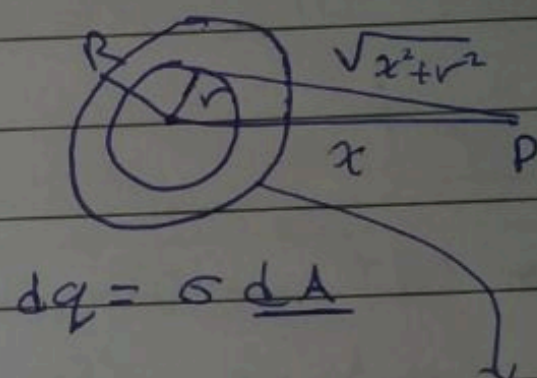
$$E = \frac{kxQ}{\sqrt{(x^2 + a^2)^3}}$$

Ex [25.6]

1)  $V = k \int \frac{dq}{r}$

$$= \int \frac{k}{\sqrt{x^2 + r^2}} \oint dq$$

$$= \int_0^R k \frac{(2\sigma \pi r dr)}{\sqrt{x^2 + r^2}} = 2\sigma \pi k \int_0^R \frac{2r dr}{\sqrt{x^2 + r^2}}$$



$$dq = \sigma dA$$

$$dA = 2\pi r dr$$

~~$$= 2\sigma \pi k \ln \left| \sqrt{x^2 + r^2} \right| \Big|_0^R \rightarrow \sigma \pi k \ln \left| \sqrt{x^2 + R^2} \right|$$~~

$$V = 2\pi k \sigma \left[ (R^2 + x^2)^{1/2} - x \right]$$



$$B) \quad V = 2\pi k\sigma \left( (R^2 + x^2)^{1/2} - x \right)$$

$$E = -\frac{\partial V}{\partial x}$$

$$= -\left( 2\pi k\sigma \left( \frac{1}{2} \cdot 2x (R^2 + x^2)^{-1/2} - 1 \right) \right)$$

$$E = 2\pi k\sigma \left( 1 - \frac{x}{\sqrt{R^2 + x^2}} \right)$$

Ex. 125-71

total charge =  $Q$

uniform linear charge  $\rightarrow \lambda$

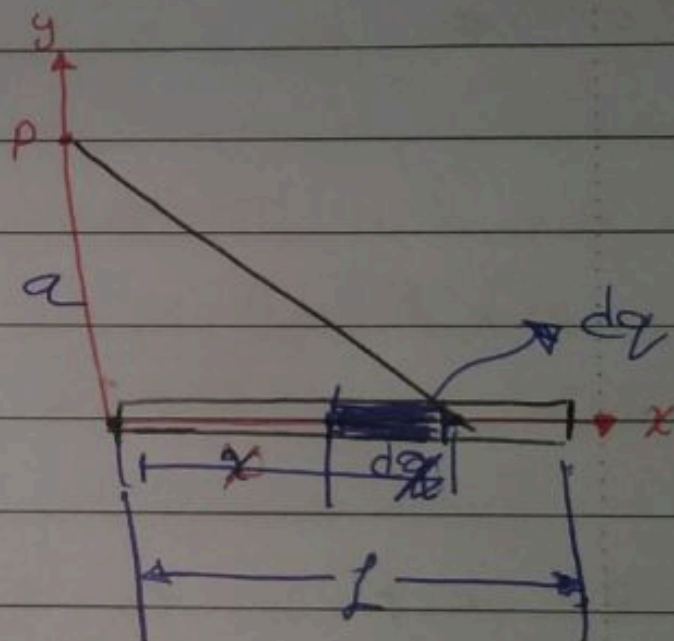
$$V = k \int \frac{dq}{r}$$

$$V = k \int_0^L \frac{\lambda dx}{\sqrt{x^2 + a^2}}$$

$$= k \frac{Q}{L} \int_0^L \frac{a \sec^2 u du}{\sqrt{a^2(\tan^2 u + 1)}}$$

$$= \frac{kQ}{L} \left[ \ln[\sec u + \tan u] \right]_0^L$$

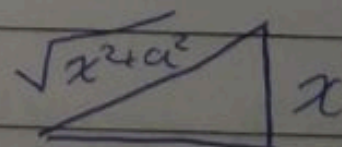
$$V = \frac{kQ}{L} \ln \left[ \frac{\sqrt{L^2 + a^2} + L}{a} \right]$$



$$r = \sqrt{x^2 + a^2}$$

$$dq = \lambda dx$$

$$\lambda = \frac{Q}{L}$$



$$x = a \tan u$$

$$dx = a \sec^2 u du$$

$$\tan^2 u + 1 = \sec^2 u$$



## 25.6 Electric potential due to a charged conductor

- properties of conductors in electrostatic equilibrium:-

1)  $\vec{E}_{in} = 0$  (Inside the conductor)

2) The charge resides on the surface of a charged conductor  
الشحنة تبقى على سطح الموصل

3) Just outside the conductor

$\vec{E} \perp \text{surface}$

$$E = \sigma / \epsilon_0$$

- The potential difference between any two points, A and B, on the surface of a charged conductor is  $\longrightarrow$

$\Delta V = 0$  between any two points on the surface.

$$V_B - V_A = 0$$

$$-\int_A^B \vec{E} \cdot d\vec{s} = 0$$

$$V_B = V_A$$

$$\Delta V = 0$$

$$V_{\text{surface}} = V_{\text{interior}}$$

$V \rightarrow \text{constant}$   
الشحنة ثابتة

- The work required to move a charge between any two points on the surface of a charged conductor is Zero

$$W = \Delta V = q \Delta V = 0$$



The potential difference between a point inside the conductor (C) and a point on the surface (A).

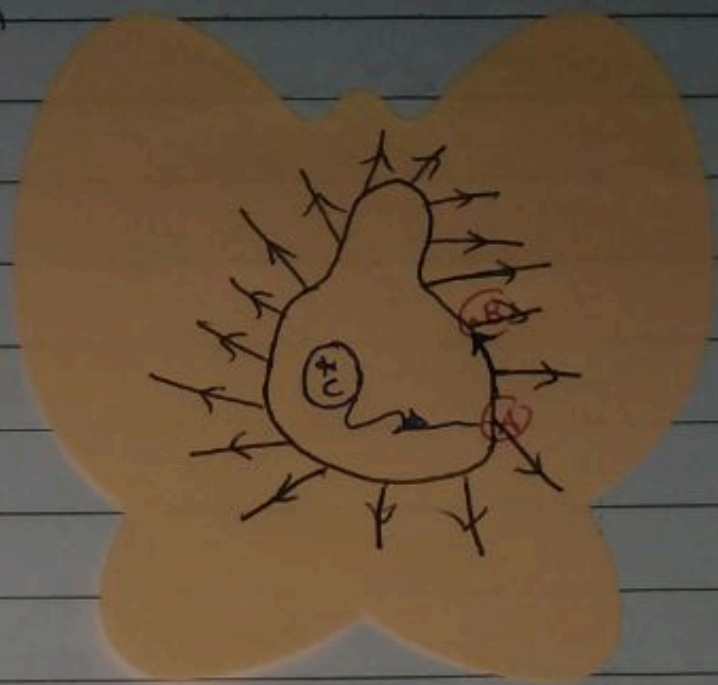
$$V_C - V_A = - \int_A^C \vec{E} \cdot d\vec{s} = 0$$

$\vec{E}_{in} = 0$

$$V_C - V_A = 0$$

$$V_C - V_A = V_{surface}$$

$$V_{in} = V_{surface}$$



The potential inside a charged conductor is constant and equals to the potential on the surface.

conducting sphere :-

for a conducting sphere of radius  $R$ , the excess charge is uniformly distributed on its surface.

Inside the sphere

On the sphere

outside the sphere

$$E_{in} = 0$$

$$V_{in} = V_s = \frac{kQ}{R}$$

$$E_s = \frac{kQ}{R^2} = \frac{\sigma}{\epsilon_0}$$

$$V_s = \frac{kQ}{R}$$

$$E_{out} = \frac{kQ}{r^2}$$

$$V_{out} = \frac{kQ}{r}$$

The charge density ( $\sigma$ ) and the electric field ( $\vec{E}$ ) on the surface of a conductor are high where the radius of curvature is small and low where the radius of curvature is high.

$E \propto \sigma$  possible  $\rightarrow r \uparrow$   
 $E \propto \sigma$  possible  $\rightarrow r \downarrow$



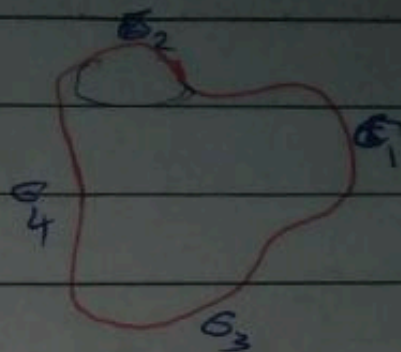
$$r_1 < r_2 < r_3 < r_4$$

$$Q_1 > Q_2 < Q_3 < Q_4$$

$$E_1 > E_2 > E_3 > E_4$$

↓

$$E = \frac{Q}{\epsilon_0}$$



Ex 25.8

two connected charged sphere:-

$$E_1 = \frac{kQ_1}{r_1^2}$$

$$E_2 = \frac{kQ_2}{r_2^2}$$

$$\frac{Q_1}{Q_2} = \frac{r_1}{r_2}$$

$$\frac{E_1}{E_2} = \frac{kQ_1}{r_1^2} \times \frac{r_2^2}{kQ_2} = \frac{r_2^2 Q_1}{r_1^2 Q_2}$$

$$\frac{E_1}{E_2} = \frac{r_2^2}{r_1^2} \times \frac{r_1}{r_2} = \frac{r_2}{r_1}$$

$$\frac{E_1}{E_2} = \frac{r_2}{r_1}$$

Wip's ①

$$V_{S1} = V_{S2}$$

$$\frac{kQ_1}{r_1} = \frac{kQ_2}{r_2}$$

$$\left[ \frac{Q_1}{Q_2} = \frac{r_1}{r_2} \right] \text{ --- (1)}$$



$$E_1 = \frac{\sigma_1}{\epsilon_0}$$

$$E_2 = \frac{\sigma_2}{\epsilon_0}$$

$$\frac{E_1}{E_2} = \frac{\sigma_1}{\sigma_2} = \frac{r_2}{r_1}$$

$E_1, \sigma_1$  ~~مساوية~~

## Ch. 26 Capacitance and Dielectrics

(سعة مكثف)

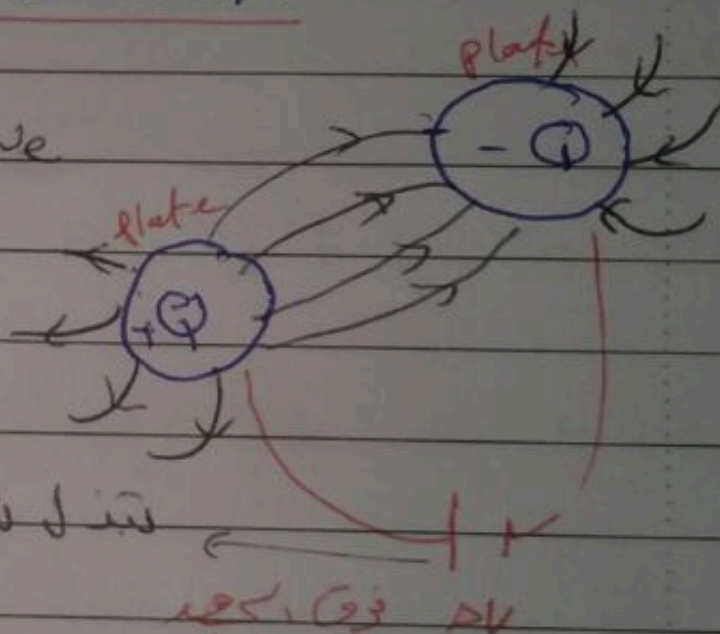
العازل

### 1.1 Capacitance:-

A capacitor consists of two conductors.

\* The capacitor is used to store electric charge (or energy)

الشحن الكهربائي



\* When the capacitor is charged the charges on the two plates will be of equal magnitude and opposite sign

1.5V

سعة

مكثف

\* The capacitance  $C$  of a capacitor is defined as the ratio of the charge  $Q$  on either plate to the magnitude of the potential difference ( $\Delta V$ ) between the plates.

$$C = \frac{Q}{\Delta V}$$

سعة / شحن



SI of  $C$  is Farad (F) =

$$1 \text{ F} = 1 \text{ C/V}$$

- 1-  $C > 0$  ( $C$  is positive)
- 2-  $C = \text{constant} \rightarrow$  (size + shape)
- 3- Measure the ability of capacitor to store electric charge

4\* farad is large unit  $\rightarrow$  we use  $\mu\text{F}/\text{nF}$

\* calculating the capacitance 25.2

EX. Spherical conductor

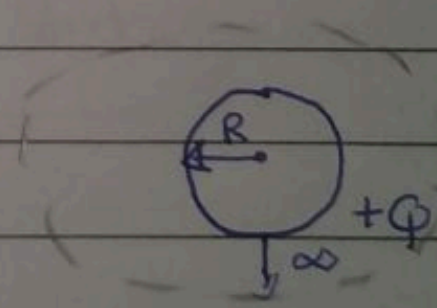
$$C = \frac{Q}{\Delta V}$$

$$\rightarrow C = \frac{Q}{\Delta V} = \frac{Q}{\frac{kQ}{R}}$$

$$\begin{aligned} \Delta V &= V_+ - V_- \\ &= V_R - V_\infty \\ &= \frac{kQ}{R} \end{aligned}$$

$$C = \frac{R}{k}$$

$$C = 4\pi\epsilon_0 R \rightarrow \text{spherical conductor}$$

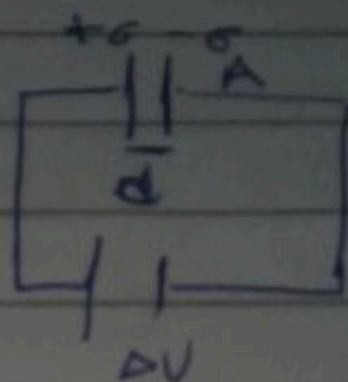




## Ex 25 parallel plates capacitor

المجال الكهربائي  $E$  بين اللوحين

$$C = \frac{Q}{\Delta V}$$



$$E = \frac{\sigma}{\epsilon_0} \quad \sigma = \frac{Q}{A}$$

$$E = \frac{Q}{\epsilon_0 A}$$

$$\Delta V = Ed$$

$$\Delta V = \frac{Qd}{\epsilon_0 A}$$

$$C = \frac{Q}{\Delta V} = \frac{\epsilon_0 A}{d}$$

$$C = \frac{\epsilon_0 A}{d} \quad \text{parallel plate capacitor}$$

## Ex 26.1 cylindrical capacitor

$$\oint E dA = \frac{q_{in}}{\epsilon_0}$$



$$E(2\pi rL) = \frac{\lambda L}{\epsilon_0}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{\lambda}{r} = \frac{2k\lambda}{r}$$

$$\lambda = \frac{Q}{L}$$

$$\Delta V = V_+ - V_-$$



$$\Delta V = - \int_b^a \frac{2K\lambda}{r} dr$$

$$= -2K\lambda \int_b^a \frac{1}{r} dr = -2K\lambda \ln\left(\frac{a}{b}\right) = 2K\lambda \ln\left(\frac{b}{a}\right)$$

$$\Delta V = 2K\lambda \ln\left(\frac{b}{a}\right) = \frac{2KQ}{L} \ln\left(\frac{b}{a}\right)$$

$$C = \frac{Q}{\Delta V} = \frac{Q}{\frac{2KQ}{L} \ln(b/a)}$$

$$C = \frac{L}{2K \ln(b/a)} \rightarrow \text{cylindrical capacitor}$$

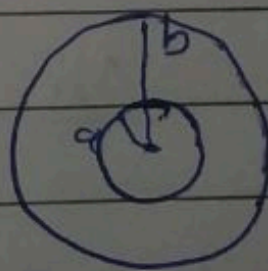
$$\frac{C}{L} = \frac{1}{2K \ln(b/a)} \rightarrow \text{capacitance per unit length}$$

Ex 26.2 spherical capacitor

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} = \frac{KQ}{r^2}$$





$$\Delta V = V_+ - V_- = - \int_-^+ E \cdot ds$$

$$\Delta V = - \int_b^a \frac{kQ}{r^2} dr = -kQ \left( -\frac{1}{r} \right) \Big|_b^a = kQ \left( \frac{1}{a} - \frac{1}{b} \right)$$

$$\Delta V = kQ \left( \frac{1}{a} - \frac{1}{b} \right)$$

$$C = \frac{Q}{\Delta V} = \frac{Q}{kQ \left( \frac{1}{a} - \frac{1}{b} \right)} = \frac{1}{k \left( \frac{1}{a} - \frac{1}{b} \right)}$$

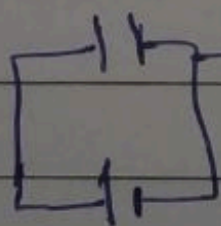
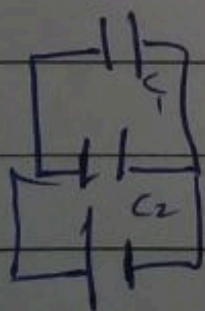
$$C = \frac{1}{k \left( \frac{1}{a} - \frac{1}{b} \right)} = \frac{ab}{k(b-a)} \rightarrow \text{spherical capacitor}$$

### 26.3 combinations of capacitors

#### 1) parallel combination

توصيل على التوازي

$$\Delta V_1 = \Delta V_2 = \Delta V$$



$$C_1 + C_2 = C_{eq}$$

$$Q = Q_1 + Q_2 \rightarrow C_{eq} \Delta V = C_1 \Delta V + C_2 \Delta V$$

$$C_{eq} = C_1 + C_2$$

$$Q = C_{eq} \Delta V$$

$$Q_1 = C_1 \Delta V$$

$$Q_2 = C_2 \Delta V$$



$$C_{eq} = C_1 + C_2 + C_3 + \dots$$

Parallel combination

$C_{eq}$  is greater than

من اكبر من

وحدة (C)

## 2) series combination

$$\Delta V = V_1 + V_2$$

$$\frac{Q}{C_{eq}} = \frac{Q_1}{C_1} + \frac{Q_2}{C_2}$$

$$\frac{Q}{C_{eq}} = \frac{Q}{C_1} + \frac{Q}{C_2}$$

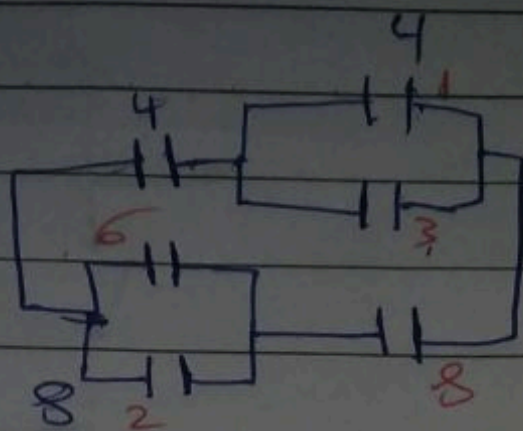
$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow C_{eq} = \frac{C_1 C_2}{C_1 + C_2}$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots$$

$C_{eq} \rightarrow$  المجموع  
المعزوجة في (C)



Ex 26.3



$$C_{eq} = \frac{18}{8} = 2$$

$$C_{eq} = \frac{64}{16} = 4$$

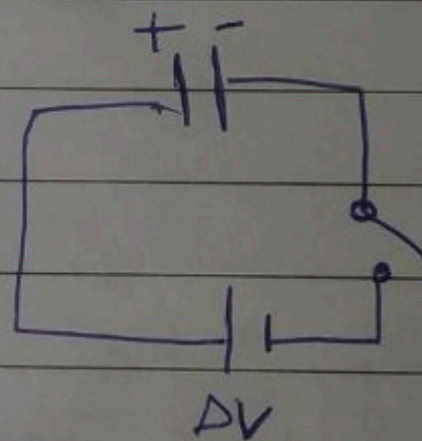
$$C_{eq} = 6 \mu F$$

### 26.4 Energy stored in a capacitor.

الشغل لنقل شحنة من الخارج إلى الداخل

الشغل  $(dq)$  من خلال وجود  $\Delta V$

Potential difference



$$dW = \Delta V dq$$

$$\int dW = \int_0^Q \frac{Q}{C} dq \rightarrow W = \frac{1}{C} \int_0^Q Q dq = \frac{Q^2}{2C}$$

$$W = U = \frac{Q^2}{2C}$$

$$Q = C \Delta V \rightarrow U = \frac{1}{2} C (\Delta V)^2$$

$$C = \frac{Q}{\Delta V} \rightarrow U = \frac{1}{2} Q \Delta V$$

$$W = U = \frac{Q^2}{2C} = \frac{1}{2} C (\Delta V)^2 = \frac{1}{2} Q \Delta V$$



Ex 26.4

$$C_1 > C_2$$

$$\Delta V_1 = \Delta V_2$$

$$Q_1 = C_1 \Delta V_i$$

$$Q_{2i} = -C_2 \Delta V_i$$

~~$$Q_i = Q_1 \Delta V + Q_2 \Delta V$$~~

~~$$Q_i = \Delta V (C_1 + C_2)$$~~

=

~~$$\Delta V_i = \frac{Q_i}{C_1 + C_2}$$~~

~~$$\Delta V_f = \Delta V_i = \frac{Q_i}{C_1 + C_2} + \frac{\Delta V_i (C_1 + C_2)}{C_1 + C_2}$$~~

A)

~~$$\Delta V_f =$$~~

$$\Delta V_f = ?$$

$$Q_i = Q_{1i} + Q_{2i}$$

$$Q_i = \Delta V (C_1 - C_2)$$

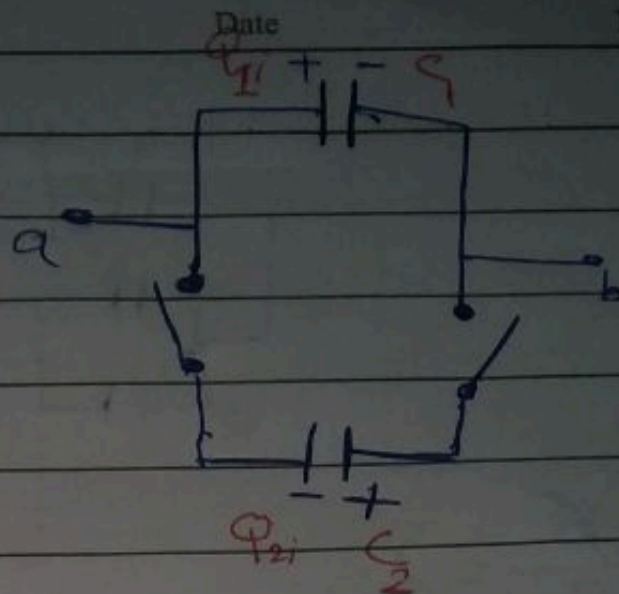
after close  $C_1 + C_2$   $\xrightarrow{Q_i}$   $Q_{1f}$   $Q_{2f}$

$$Q_f = Q_{1f} + Q_{2f}$$

$$= C_1 \Delta V_f + C_2 \Delta V_f$$

$$Q_f = \Delta V_f (C_1 + C_2)$$

$$Q_f = Q_i \rightarrow$$





$$(C_1 + C_2) \Delta U_f = (C_1 - C_2) \Delta U_i$$

$$\Delta U_f = \left( \frac{C_1 - C_2}{C_1 + C_2} \right) \Delta U_i$$

B)  $\frac{U_f}{U_i}$

$$U_i = \frac{1}{2} C_1 \Delta U_i^2 + \frac{1}{2} C_2 \Delta U_i^2 = \frac{1}{2} \Delta U_i^2 (C_1 + C_2)$$

$$U_f = \frac{1}{2} C_1 \Delta U_f^2 + \frac{1}{2} C_2 \Delta U_f^2 = \frac{1}{2} \Delta U_f^2 (C_1 + C_2)$$

~~$$\frac{U_f}{U_i} = \frac{\frac{1}{2} \Delta U_i^2 (C_1 + C_2)}{\frac{1}{2} \Delta U_i^2 (C_1 + C_2)}$$~~

$$U_f = \frac{1}{2} (C_1 + C_2) \left[ \frac{(C_1 - C_2)^2 \Delta U_i^2}{(C_1 + C_2)^2} \right]$$

$$\frac{U_f}{U_i} = \frac{\frac{1}{2} (C_1 + C_2) \left[ \frac{(C_1 - C_2)^2 \Delta U_i^2}{(C_1 + C_2)^2} \right]}{\frac{1}{2} (C_1 + C_2) \Delta U_i^2} = \left( \frac{C_1 - C_2}{C_1 + C_2} \right)^2 < 1$$

حصر الهمي الطاقة



## 26.5 Capacitors with dielectrics

\* مادة غير موصلة لا تمنح بين الصفحتين للمحث تزييد المدة

التيه ثابت غير لكن تعلق  $\Delta V$  تزييد Capacity

\* لو ح (ن ص) بطارية بتغير الشحنة

$$\Delta V = \frac{\Delta V_0}{K}$$

بعم  
وجود مادة  
عازلة

بمزاياها  
العازل

$K$ : constant (باعتبار نوع المادة)  
 $K > 1$

$$C_0 = \frac{Q_0}{\Delta V_0} \rightarrow C = \frac{Q_0}{\Delta V} = \frac{Q_0}{\Delta V_0 / K} = K \frac{Q_0}{\Delta V_0}$$

$$C = K C_0$$

تزييد المدة  
بزيادة  $K$

- For parallel plates capacitor

$$C_0 = \frac{\epsilon_0 A}{d} \rightarrow C = K C_0$$

$$C = K \frac{\epsilon_0 A}{d}$$



إجابات الموارث :

(1) زيادة سماحية الخلف

(2) زيادة أقصى جهد تشغيل

(3) إمكانية توفير ميعانتي بين الصفائح

Ex 26.5

$$\Phi_0 = C_0$$

$$U = ?$$

$$U_0 = \frac{\Phi_0^2}{2C_0}$$

$$C = K C_0$$

$$U = \frac{\Phi_0^2}{2C_0} \rightarrow U = \frac{1}{K} \frac{\Phi_0^2}{2C_0}$$

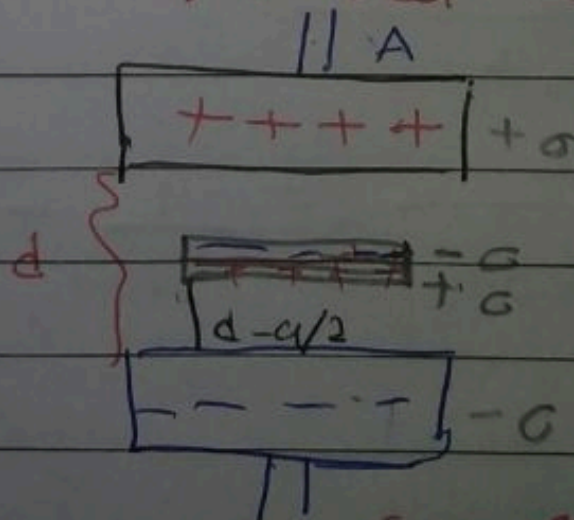
$$U = \frac{U_0}{K}$$

$$\frac{U}{U_0} = \frac{1}{K} < 1$$

## 26.7 An Atomic Description of Dielectrics

$$C_1 = \frac{\epsilon_0 A}{d - a/2}$$

$$C_2 = \frac{\epsilon_0 A}{d - a/2}$$



$$C_0 = \frac{\epsilon_0 A}{d}$$



$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

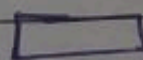
$$C_1 = \frac{\epsilon_0 A}{d-a/2} = \frac{2\epsilon_0 A}{d-a}$$

$$C_2 = \frac{2\epsilon_0 A}{d-a}$$

$$\frac{1}{C} = \frac{d-a}{2\epsilon_0 A} + \frac{d-a}{2\epsilon_0 A}$$

$$C = \frac{\epsilon_0 A}{d-a}$$

EX 26.8



$$C_1 = \frac{\kappa \epsilon_0 A}{fd}$$

لا يوجد عازل للجزء الثاني

$$C_2 = \frac{\epsilon_0 A}{(1-f)d}$$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{fd}{\kappa \epsilon_0 A} + \frac{(1-f)d}{\epsilon_0 A}$$

$$\frac{1}{C} = \frac{fd + \kappa d(1-f)}{\kappa \epsilon_0 A}$$

$$C = \frac{\kappa \epsilon_0 A}{fd + \kappa d(1-f)} = \left( \frac{\kappa}{f + \kappa(1-f)} \right) \frac{\epsilon_0 A}{d}$$

$$C = \frac{\kappa}{f + \kappa(1-f)} C_0$$



## Ch 27 Current and Resistance:

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = \frac{dQ}{dt}$$

$$1 \Omega = \frac{V}{A}$$

$$1 \Omega = \Omega \cdot m$$

$$J = \sigma E$$

$$\Delta V = IR \rightarrow \text{Ohm's law}$$

$$R = \frac{\rho L}{A} = \frac{L}{\sigma A}$$

$$\rho = \frac{1}{\sigma}$$

Conductivity

resistivity

### Ex. 27.2

$$0.32 \text{ mm} \rightarrow 3.2 \times 10^{-3} \text{ m}$$

$$\text{A) } \frac{R}{L} = \frac{\rho}{A} = \frac{1.4 \times 10^{-6} \Omega \cdot m}{\pi (0.32 \times 10^{-3})^2} = \frac{1.4 \times 10^{-6}}{3.1 \times 10^{-4}} \Omega/m$$

$$\text{B) } \Delta V = 10 \quad L = 1$$

$$I = \frac{\Delta V}{R} = \frac{10}{\frac{1.4 \times 10^{-6} \times 1}{\pi (0.32 \times 10^{-3})^2}} = 3.2 \text{ A}$$



Resistance and temperature

س المقاومة على الحرارة

$$\rho = \rho_0 [1 + \alpha (T - T_0)]$$

$$\alpha = \frac{1}{\rho_0} \frac{\Delta \rho}{\Delta T}$$

ثابت

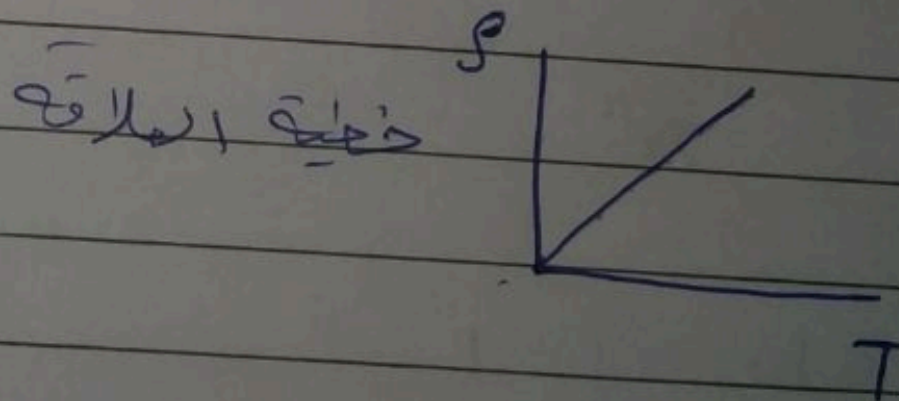
$$\alpha \rightarrow ^\circ\text{C}^{-1}$$

$$R = \frac{\rho L}{A}$$

$$\frac{\rho L}{A} = \frac{\rho_0 L}{A} [1 + \alpha (T - T_0)]$$

$$R = R_0 [1 + \alpha (T - T_0)]$$

← T  
← T<sub>0</sub> (المقاومة عند T<sub>0</sub>)

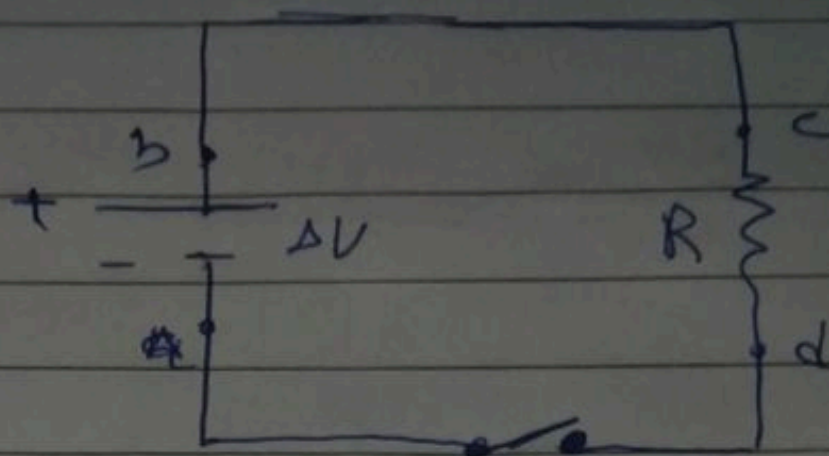




27.6 Electrical power

القدرة الكهربائية

نكتب طاقة دمج من  
 $q$  إلى  $b$  وتستهلك  
 في  $R$



- The energy  $q$  when charged  
 $\Delta q$  moved from  $a$  to  $b$

Watt  
 $2000 \text{ J/s}$

نكتب طاقة دمج خلال فرق جهد  
 معين

$$\Delta U = (\Delta q)(\Delta V) \rightarrow R \text{ تستهلك في}$$

$$P = \frac{\Delta U}{\Delta t} = \frac{\Delta q}{\Delta t} \Delta V = I \Delta V$$

Power

$$\Delta V = R I$$

Watt  $\boxed{\text{J/s}}$

$$P = I^2 R$$

$$P = \frac{\Delta V^2}{R}$$

$$\Delta U = P \Delta t$$



EX 27.4 $I \rightarrow$  Current

$\Delta V = 120$

$R = 8$

$\Delta V = IR$

$$1) I = \frac{\Delta V}{R} = \frac{120}{8} = 15 A$$

$$2) P = \frac{\Delta V^2}{R} = 1800 W = 1.8 kW$$

EX 27.5

$m = 1.5 kg$

$T_1 = 10$

$T_2 = 50$

$T = 10 m/s$

$\Delta V = 110 V$

$$R = \frac{(110)^2 (600)}{(1.5) (4186) (50 - 10)} = 28.9 \Omega$$