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اللجنة الأكاديمية لقسم الهندسة المدنية

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## 15.4 | Obtaining the Value of the electric field from the electric potential

$$V_B - V_A = \int_A^B \vec{E} \cdot d\vec{s}$$

whence  
we get  $\vec{E} = -\nabla V$ .

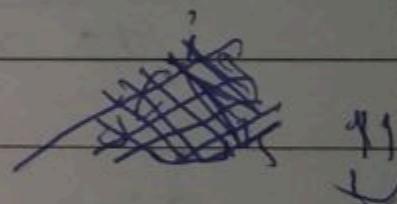
$$dV = -\vec{E} \cdot d\vec{s}$$

If the electric field has only one component,  $E_x$

$$\vec{E} = E_x \hat{i}$$

$$d\vec{s} = dx \hat{i} + dy \hat{j} + dz \hat{k}$$

$$\vec{E} \cdot d\vec{s} = E_x dx$$



$$E_x = -\frac{dV}{dx} \rightarrow$$

we get  $E_x = -\nabla V$

$$E_x = -\frac{\partial V}{\partial x}$$

$$E_y = -\frac{\partial V}{\partial y}$$

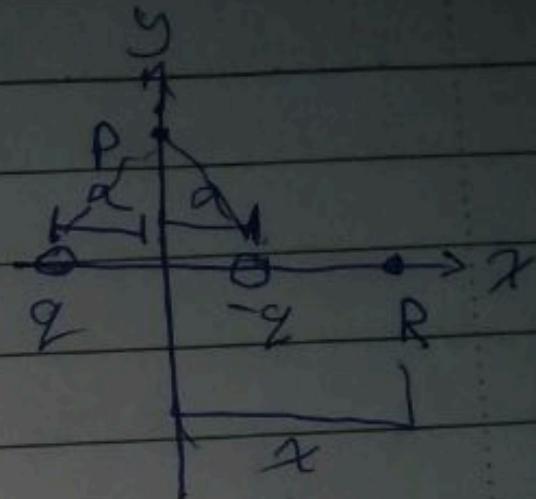
$$E_z = -\frac{\partial V}{\partial z}$$

Ex 125.41 $v_p ? \quad y = ?$ 

$$1) v_p = k \left( \frac{q_1}{r_1} + \frac{-q_2}{r_2} \right)$$

$$= kq \left( \frac{1}{\sqrt{a^2+y^2}} - \frac{1}{\sqrt{a^2+y^2}} \right)$$

$v_p = 0$



$v=0 \leftarrow y\text{-axis is a symmetry axis}$

$$2) v_B = k \left( \frac{q}{x-a} - \frac{q}{x+a} \right)$$

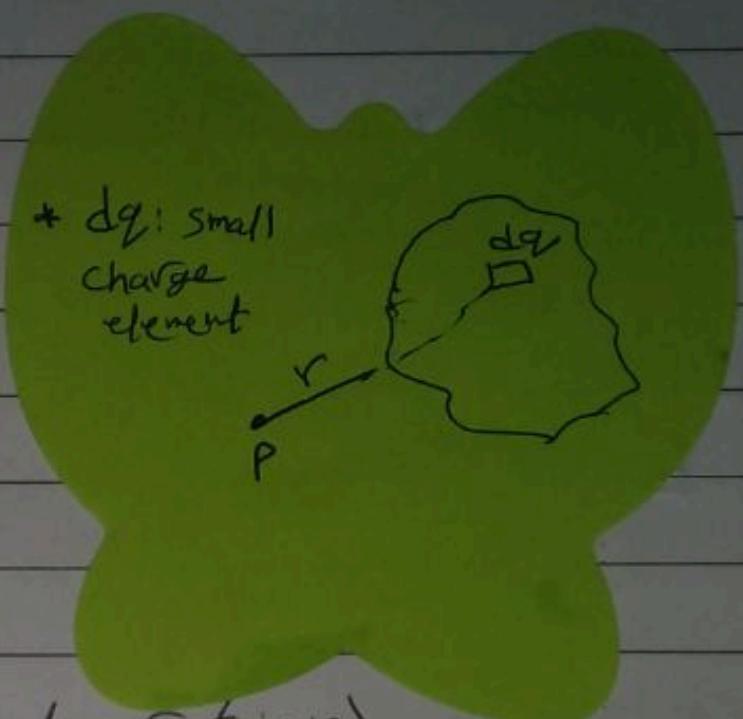
$$= -\frac{2kq}{(x^2-a^2)}$$

Ex 25.5 | Electric potential due to continuous charge distributions :-

- The electric potential due to a small charge element  $dq$  at point P at distance  $r$  from  $dq$  is

$$\int dV = \int K \frac{dq}{r}$$

\*  $dq$ : small charge element



- sum over all charge elements (integration)

$$V = \int \frac{dq}{r}$$

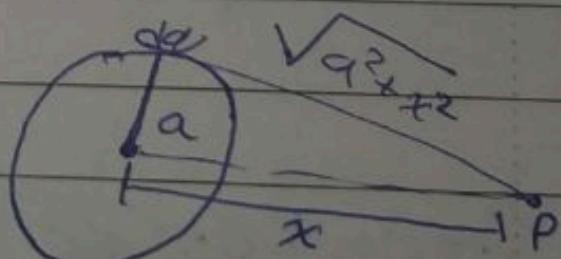
$dq \rightarrow \lambda dL \rightarrow$  line charge distribution.

$dq \rightarrow \sigma dA \rightarrow$  surface charge distribution.

$dq \rightarrow \rho dv \rightarrow$  Volume charge distribution.

Ex. 25.5 |

$$r = \sqrt{a^2 + x^2}$$



$$V = K \int \frac{dq}{\sqrt{a^2 + x^2}}$$

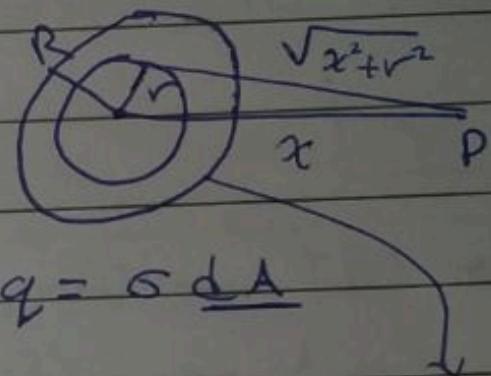
$$V = \frac{K Q}{\sqrt{a^2 + x^2}}$$

$$\text{B) } V = \frac{kQ}{\sqrt{x^2 + a^2}} \xrightarrow{\text{جذب}} E = -\frac{\partial V}{\partial x} = -\frac{1}{2} \frac{(x^2 + a^2)^{-1/2}}{x}$$

$$E = kQ \frac{x}{\sqrt{x^2 + a^2}^3} \rightarrow -\left(\frac{1}{2} \frac{x}{\sqrt{x^2 + a^2}^3}\right)$$

$$\boxed{E = \frac{kxQ}{\sqrt{(x^2 + a^2)^3}}}$$

Ex 125.6



$$V = k \int \frac{dq}{r}$$

$$= \int \frac{k}{\sqrt{x^2 + r^2}} \oint dq$$

$$= \int_0^R k \frac{(2\pi r dr)}{\sqrt{x^2 + r^2}} = 2\pi k \int_0^R \frac{2r dr}{\sqrt{x^2 + r^2}}$$

$$dr = 2\pi r dr$$

~~$$V = 2\pi k \int_0^R \frac{r^2 dr}{\sqrt{x^2 + r^2}}$$~~

$$\boxed{V = 2\pi k \sigma \left[ \left( R^2 + x^2 \right)^{1/2} - x \right]}$$

$$V = 2\pi k \sigma \left( \left( R^2 + x^2 \right)^{-\frac{1}{2}} - x \right)$$

$$E = -\frac{\partial V}{\partial x}$$

$$= -\left( 2\pi k \sigma \left( \frac{1}{2} x \left( R^2 + x^2 \right)^{-\frac{1}{2}} - 1 \right) \right)$$

$$E = 2\pi k \sigma \left( 1 - \frac{x}{\sqrt{R^2 + x^2}} \right)$$

Ex. 125  $\rightarrow$

total charge  $= Q$

Uniform linear charge  $\rightarrow \lambda$

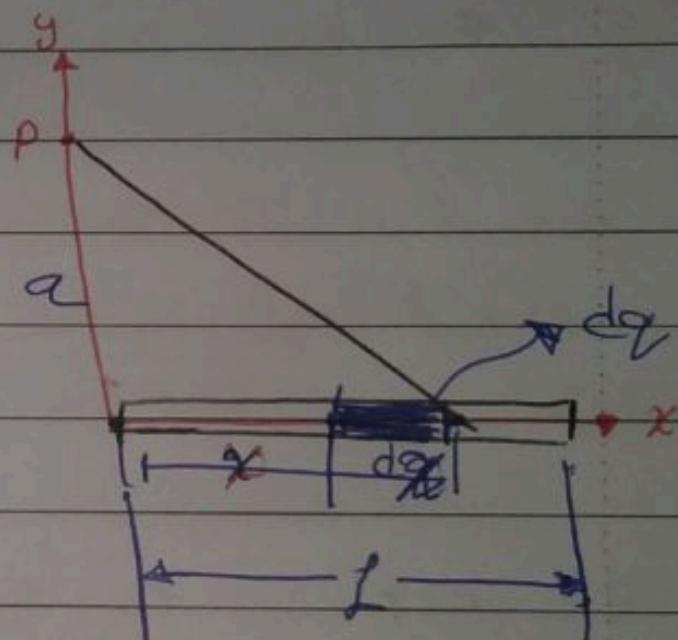
$$V = \frac{k}{\sqrt{x^2 + a^2}} \int dq$$

$$V = k \int_0^L \frac{\lambda dx}{\sqrt{x^2 + a^2}}$$

$$= k \frac{Q}{L} \int_0^L \frac{a \sec^2 u du}{\sqrt{a^2(\tan^2 u + 1)}}$$

$$= \frac{kQ}{L} \left[ \ln[\sec u + \tan u] \right] \Big|_0^L$$

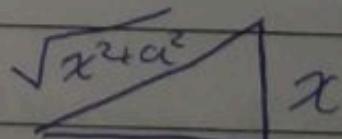
$$V = \frac{kQ}{L} \ln \left[ \frac{\sqrt{L^2 + a^2} + L}{a} \right]$$



$$r = \sqrt{x^2 + a^2}$$

$$dr = \sqrt{x^2 + a^2} dx$$

$$\lambda = \frac{Q}{L}$$



$$x = a \tan u$$

$$dx = a \sec^2 u du$$

$$+ \tan^2 u + 1 = \sec^2 u$$

## 125.6 | Electric potential due to a charged conductor

- properties of conductors in electrostatic equilibrium:-

1)  $\vec{E}_{\text{in}} = 0$  (Inside the conductor)

2) The charge resides on the surface of a charged conductor

المتحدة تترك على سطح المروج

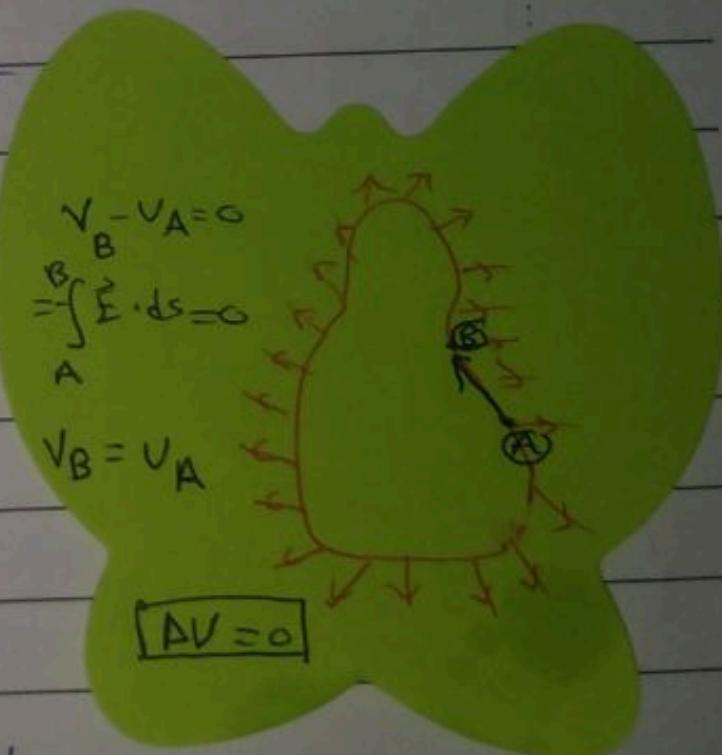
3) Just outside the conductor

$\vec{E} \perp \text{surface}$

$$E = \sigma / \epsilon_0$$

- The potential difference between any two points, A and B, on the surface of a charged conductor is

$\Delta V = 0$ . Between any two points on the surface.



$$\frac{V_{\text{outer}}}{\text{الخارج}} = \frac{V_{\text{inner}}}{\text{الداخل}} \quad V \rightarrow \text{constant}$$

لأنه في كل الحالة

- The work required to move a charge between any two points on the surface of a charged conductor is zero

$$W = \frac{\Delta V}{U} = q \cdot \frac{\Delta V}{U} = 0$$

لأنه في كل الحالة

The potential difference between a point inside the conductor ( $O$ ), and a point on the surface ( $A$ ).

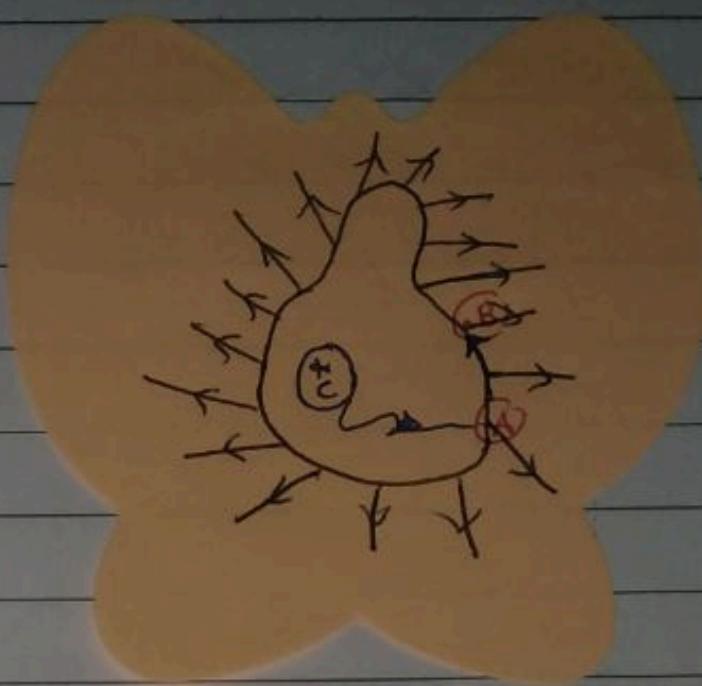
$$V_C - V_A = - \int_A^C \vec{E} \cdot d\vec{s} = 0$$

$\vec{E}_{in} = 0$

$$V_C - V_A = 0$$

$$V_C - V_A = V_{surface}$$

$V_{in} = V_{surface}$



- The potential inside a charged conductor is constant and equals to the potential on the surface.

- Conducting sphere :-

for a conducting sphere of radius  $R$ , the excess charge is uniformly distributed on its surface.

Inside the sphere	On the sphere	Outside the sphere
$E_{in} = 0$	$E_s = \frac{kQ}{R^2} = \frac{\sigma}{\epsilon_0}$	$E_{out} = \frac{kQ}{r^2}$
$V_{in} = V_s = \frac{kQ}{R}$	$V_s = \frac{kQ}{R}$	$V_{out} = \frac{kQ}{r}$

\* The charge density ( $\sigma$ ) and the electric field ( $\vec{E}$ ) on the surface of a conductor are high where the radius of curvature is small and low where the radius of curvature is high.

$E_{in}$  or  $\sigma$  would be  $\rightarrow r \downarrow$   
 $E_{in}$  or  $\sigma$  would be  $\rightarrow r \downarrow$

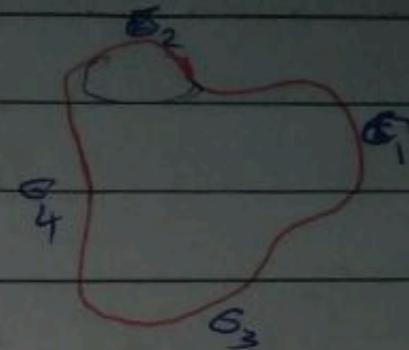
$$r_1 < r_2 < r_3 < r_4$$

$$\epsilon_1 > \epsilon_2 > \epsilon_3 > \epsilon_4$$

$$\Sigma_1 > \Sigma_2 > \Sigma_3 > \Sigma_4$$

↓

$$E = \frac{Q}{\epsilon_0}$$



### Ex 25.8

+ Two connected charged sphere:-

$$\Sigma_1 = \frac{KQ_1}{r_1^2}$$

$$E_2 = \frac{KQ_2}{r_2^2}$$

$$\frac{q_1}{q_2} = \frac{r_1}{r_2}$$

$$\frac{E_1}{E_2} = \frac{KQ_1}{r_1^2} * \frac{r_2^2}{KQ_2} = \frac{r_2^2 q_1}{r_1^2 q_2}$$

$$\frac{\Sigma_1}{\Sigma_2} = \frac{r_2^2}{r_1^2} * \frac{r_1}{r_2} = \frac{r_2}{r_1}$$

$$\frac{\Sigma_1}{E_2} = \frac{r_2}{r_1}$$

Ans  $\therefore$

$$V_{S1} = V_{S2}$$

$$\frac{KQ_1}{r_1} = K \frac{q_2}{r_2}$$

$$\frac{q_1}{q_2} = \frac{r_1}{r_2}$$

(1)

$$E_1 = \frac{\sigma_1}{\epsilon_0}$$

$$E_2 = \frac{\sigma_2}{\epsilon_0}$$

$$\frac{E_1}{E_2} = \frac{\sigma_1}{\sigma_2} = \frac{r_2}{r_1}$$

$E_1 > E_2$  because  $\sigma_1 > \sigma_2$

## Ch. 26 Capacitance and Dielectrics

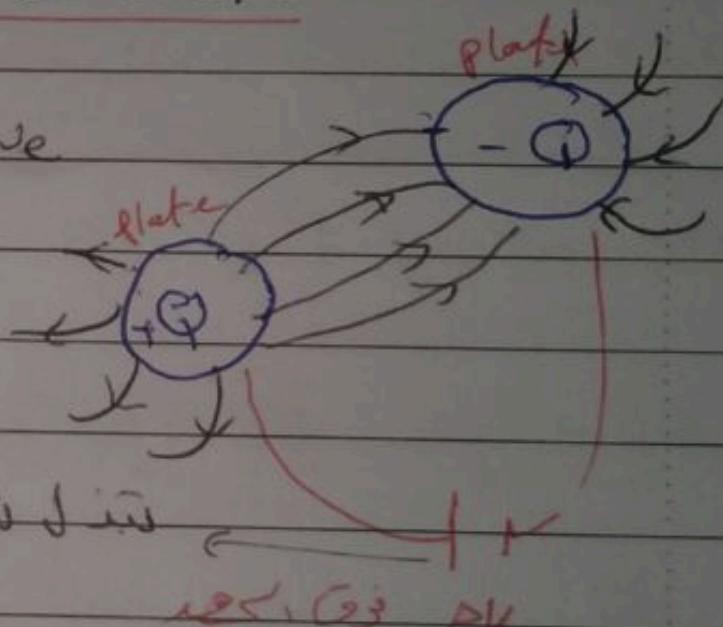
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### III Capacitance:-

A capacitor consists of two conductors. صو

\* The capacitor is used to store electric charge (or energy) احتياط الكهرباء



\* When the capacitor is charged the charges on the two plates كلا are of equal magnitude and opposite signs +Q -Q ΔV

\* The capacitance  $C$  of a capacitor is defined as the ratio of the charge  $Q$  on either plate to the magnitude of the potential difference ( $\Delta V$ ) between the plates.

$$C = \frac{Q}{\Delta V}$$

علاقة علاقة

~~SI~~ unit of C is Farad (F) =

$$1 \text{ F} = 1 \text{ C/V}$$

1-  $C > 0$  (C is positive)

2-  $C = \text{constant} \rightarrow$  (well depends on  
size + shape)

3- Measure the ability of capacitor to store electric charge

4- farad is large unit  $\rightarrow$  we use MF/nF

\* calculating the capacitance 26.2

Ex. spherical conductor

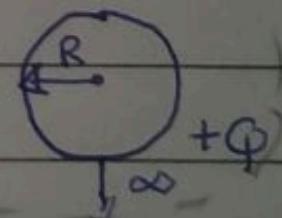
$$C = \frac{Q}{\Delta V}$$

$$\rightarrow C = \frac{Q}{\Delta V} = \frac{Q}{k\epsilon_0 R}$$

$$\Delta V = V_+ - V_-$$

$$= V_R - V_\infty$$

$$= \frac{k\phi}{R}$$



$$C = \frac{R}{k}$$

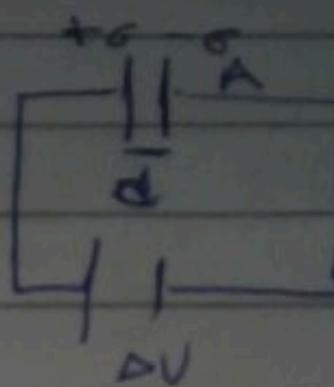
$$C = 4\pi\epsilon_0 R$$

$\rightarrow$  spherical conductor

## Ex 25 parallel plates capacitor

مقدار المجال بين الألواح  $E$

$$C = \frac{Q}{\Delta V}$$



$$E = \frac{\sigma}{\epsilon_0} \quad \sigma = \frac{Q}{A}$$

$$E = \frac{Q}{\epsilon_0 A}$$

$$\Delta V = Ed$$

$$\Delta V = \frac{Qd}{\epsilon_0 A}$$

$$C = Q \times \frac{\epsilon_0 A}{d} = \frac{\epsilon_0 A}{d}$$

$$C = \frac{\epsilon_0 A}{d} \quad \text{parallel plate capacitor}$$

## Ex 26.1 cylindrical capacitor

$$\oint F dA = \frac{q_{in}}{\epsilon_0}$$



$$E(2\pi rh) = \frac{\pi rh}{\epsilon_0}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{2}{r} = \frac{\rho}{\epsilon_0} \frac{2\pi r}{l} \quad R = \frac{Q}{\rho l}$$

$$\Delta V = V_+ - V_-$$

$$\Delta V = - \int_b^a \frac{2\kappa\lambda}{r} dr$$

$$= -2\kappa\lambda \int_b^a \frac{1}{r} dr = -2\kappa\lambda \ln\left(\frac{a}{b}\right) - 2\kappa\lambda \ln\left(\frac{a}{b}\right)$$

$$\Delta V = 2\kappa\lambda \ln\left(\frac{b}{a}\right) = \frac{2\kappa\Phi}{l} \ln\left(\frac{b}{a}\right)$$

$$C = \frac{\Phi}{\Delta V} \rightarrow \frac{\Phi}{\frac{2\kappa Q}{l} \ln(b/a)}$$

$$C = \frac{l}{2\kappa \ln(b/a)}$$

$\rightarrow$  cylindrical capacitor

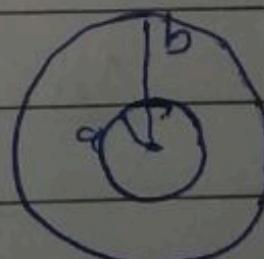
$$\boxed{C = \frac{l}{2\kappa \ln(b/a)}}$$

$\rightarrow$  capacitance per unit length

### Ex 26.2 Spherical Capacitor

$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0}$$



$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} = \frac{kQ}{r^2}$$

$$\Delta V = V_+ - V_- = - \int E \cdot ds$$

$$\Delta V = - \int_b^a \frac{kQ}{r^2} dr = - kQ \left( \frac{1}{r} \right) \Big|_{b \rightarrow a} = kQ \left( \frac{1}{a} - \frac{1}{b} \right)$$

$$\Delta V = kQ \left( \frac{1}{a} - \frac{1}{b} \right)$$

$$C = \frac{Q}{\Delta V} = \frac{Q}{kQ \left( \frac{1}{a} - \frac{1}{b} \right)} = \frac{1}{k \left( \frac{1}{a} - \frac{1}{b} \right)}$$

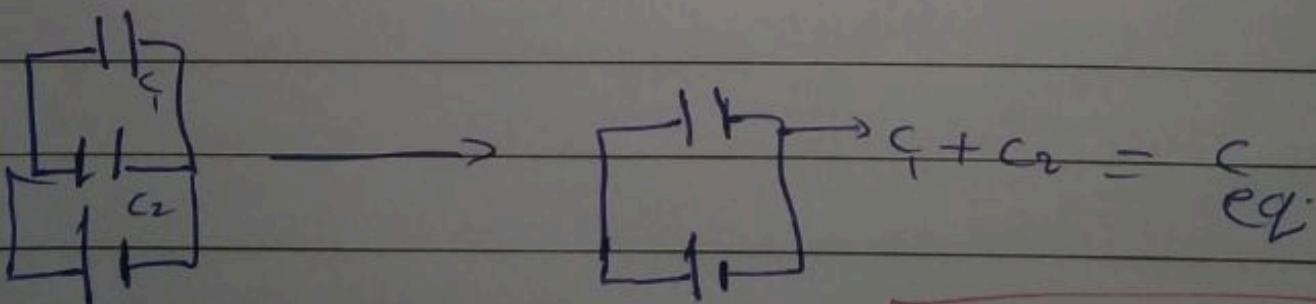
$$C = \frac{1}{k \left( \frac{1}{a} - \frac{1}{b} \right)} = \frac{ab}{k(b-a)} \quad \rightarrow \text{spherical capacitor}$$

### 26.3 Combinations of Capacitors

#### 1) Parallel combination

مُعَدِّل على الموارد

$$\Delta V_1 = \Delta V_2 = \Delta V$$



$$C_{eq} = C_1 + C_2$$

$$Q = Q_1 + Q_2 \rightarrow \frac{C_{eq}}{C_{eq}} \Delta V = \frac{C_1}{C_1} \Delta V + \frac{C_2}{C_2} \Delta V$$

$$Q = C_{eq} \Delta V$$

$$Q_1 = C_1 \Delta V$$

$$Q_2 = C_2 \Delta V$$

$$C_{eq} = C_1 + C_2 + C_3 + \dots$$

Parallel combination

$C_{eq}$  is greater than  $\rightarrow$  series

2) series combination

$C_{eq}$  (series)

$$\Delta V = V_1 + V_2$$

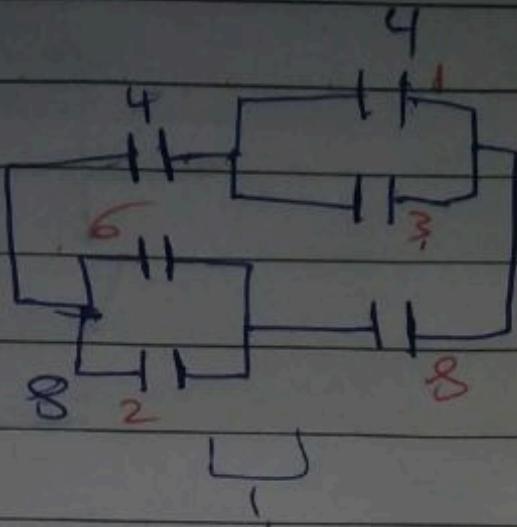
$$\frac{Q}{C_{eq}} = \frac{Q_1}{C_1} + \frac{Q_2}{C_2}$$

$$\frac{Q}{C_{eq}} = \frac{Q_1}{C_1} + \frac{Q_2}{C_2}$$

$$\boxed{\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow C_{eq} = \frac{C_1 C_2}{C_1 + C_2}}$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \dots$$

$C_{eq} \rightarrow$   $C_{eq}$  (series)

Ex 26.3

$$C_{eq} = \frac{18}{8} = 2$$

$$C_{eq} = \frac{64}{16} = 4$$

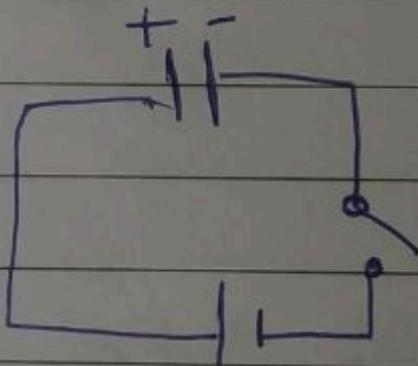
$$C_{eq} = 6 \text{ MF}$$

26.4 Energy stored in a capacitor.

النهر لنقل سطحات ملء حب الماء

$\Delta V$  من خلال دخوا

Potential difference



$$dW = \Delta V dq$$

$$\int dW = \int \frac{q}{C} dq \rightarrow W = \frac{1}{C} \int_0^q q dq = \frac{Q^2}{2C}$$

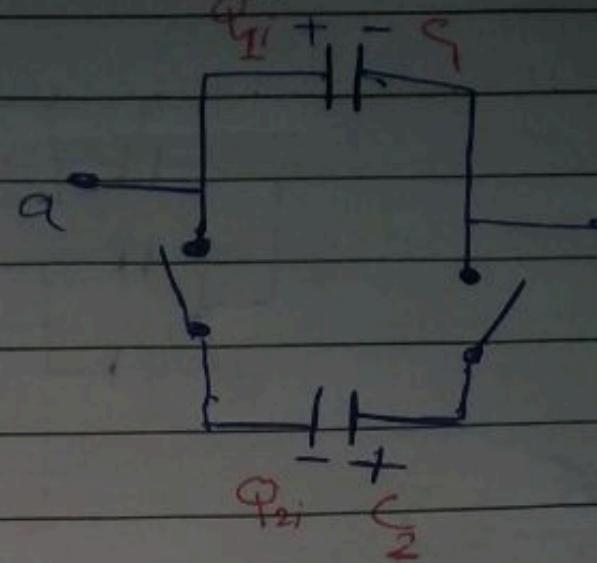
$$W = U = \frac{Q^2}{2C} \quad | \quad Q = C \Delta V \rightarrow U = \frac{1}{2} C (\Delta V)^2$$

$$C = \frac{Q}{\Delta V} \rightarrow U = \frac{1}{2} Q \Delta V$$

$$W = U = \frac{Q^2}{2C} = \frac{1}{2} C (\Delta V)^2 = \frac{1}{2} Q \Delta V$$

Ex 26.4

$$C_1 > C_2$$



$$\Delta V_1 = \Delta V_2$$

$$\varphi_i = C_1 \Delta V_i$$

$$Q_{2i} = -C_2 \Delta V_i$$

$$Q_i = \varphi_i \Delta V + Q_{2i} \Delta V$$

$$Q_i = \Delta V (C_1 + C_2)$$

=

$$\Delta V_i = \frac{Q_i}{C_1 + C_2}$$

$$\Delta V_f - \Delta V_i = \frac{Q_i}{C_1 + C_2} + \frac{\Delta V_i (C_1 + C_2)}{C_1 + C_2}$$

A)

$$\Delta V_f =$$

$$\Delta V_f = ?$$

$$\varphi_i = \varphi_{1i} + \varphi_{2i}$$

$$Q_i = \Delta V (C_1 + C_2)$$

after close  $S_1 + S_2$  |  $\xrightarrow{\text{الآن}} Q_{1f} \quad Q_{2f}$   
الآن

$$Q_f = Q_{1f} + Q_{2f}$$

$$= C_1 \Delta V_f + C_2 \Delta V_f$$

$$Q_f = \Delta V_f (C_1 + C_2)$$

$$Q_f = Q_i \rightarrow$$

الآن  
الآن

$$(c_1 + c_2) \Delta U_f = (c_1 - c_2) \Delta U_i$$

$$\Delta U_f = \frac{(c_1 - c_2)}{c_1 + c_2} \Delta U_i$$

B)  $\frac{U_f}{U_i}$

$$U_i = \frac{1}{2} c_1 \Delta U_i^2 + \frac{1}{2} c_2 \Delta U_i^2 = \frac{1}{2} \Delta U_i^2 (c_1 + c_2)$$

$$U_f = \frac{1}{2} c_1 \Delta U_f^2 + \frac{1}{2} c_2 \Delta U_f^2 = \frac{1}{2} \Delta U_f^2 (c_1 + c_2)$$

~~$$\frac{U_f}{U_i} = \frac{1}{2} \Delta U_i^2 (c_1 + c_2)$$~~

$$U_f = \frac{1}{2} (c_1 + c_2) \left[ \frac{(c_1 - c_2)^2 \Delta U_i^2}{(c_1 + c_2)^2} \right]$$

$$\frac{U_f}{U_i} = \frac{\frac{1}{2} (c_1 + c_2) \left[ \left( \frac{c_1 - c_2}{c_1 + c_2} \right)^2 \Delta U_i^2 \right]}{\frac{1}{2} (c_1 + c_2) \Delta U_i^2} = \left( \frac{c_1 - c_2}{c_1 + c_2} \right)^2$$

وَالْأَعْلَى حِلْمَانِي

26.5 Capacitors with dielectrics

\* مادة غير موصلية تؤدي إلى

- السُّخنة طبقة مسحودة تزداد سعة القدرة

\* لوحة مسحودة يتغير السُّخنة

$$\Delta U = \frac{\Delta V_0}{K} \rightarrow \text{نعم}$$

$\downarrow$  بحسب المفهوم  
العنوان

مسحودة



K: Constant (يعتمد على نوع المادة)

$$K > 1$$

$$C_0 = \frac{Q_0}{\Delta V_0} \rightarrow C = \frac{Q_0}{\Delta V} = \frac{Q_0}{\Delta V_0 / K} = K \frac{Q_0}{\Delta V_0}$$

$$C = K C_0$$

$\downarrow$  تزويج المقادير

$K \rightarrow$  ثوابت

- For parallel plates capacitor

$$C_0 = \frac{\epsilon_0 A}{d} \rightarrow C = K C_0$$

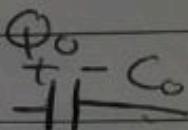
$$C = K \frac{\epsilon_0 A}{d}$$

إيجارات الموارد~~الله يسمى~~

1) زيادة السعة المخزنة

2) زيادة القدرة الكهربائية

3) إمكانية توفير معيار يحيي بعض الصناعات

Ex 26.5

$$U = ?$$

$$U_0 = \frac{Q_0^2}{2C_0}$$

$$C = kC_0$$

$$U = \frac{Q^2}{2C} \rightarrow U = \frac{1}{k} \frac{Q^2}{2C_0}$$

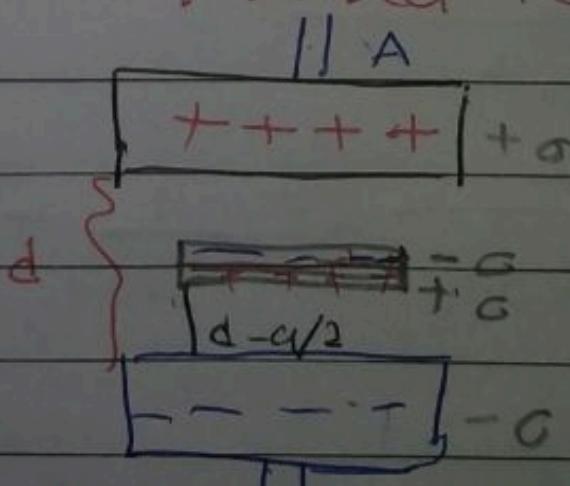
$$U = \frac{U_0}{k}$$

$$\frac{U}{U_0} = \frac{1}{k} < 1$$

26.7 An Atomic Description of Dielectrics

$$C_1 = \frac{\epsilon_0 A}{d-a/2}$$

$$C_2 = \frac{\epsilon_0 A}{d-a/2}$$



$$\frac{1}{C} = \frac{1}{d-a} + \frac{1}{d-a}$$

$$C_1 = \frac{\epsilon_0 A}{d-a/2} = \frac{2\epsilon_0 A}{d-a}$$

$$C_2 = \frac{2\epsilon_0 A}{d-a}$$

$$\frac{1}{C} = \frac{d-a}{2\epsilon_0 A} + \frac{d-a}{2\epsilon_0 A}$$

$$C = \frac{\epsilon_0 A}{d-a}$$

Ex 26.8

$$C_1 = \frac{k\epsilon_0 A}{fd} \quad C_2 = \frac{k\epsilon_0 A}{(1-f)d}$$

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{fd}{k\epsilon_0 A} + \frac{(1-f)d}{k\epsilon_0 A}$$

$$\frac{1}{C} = \frac{fd + kd(1-f)}{k\epsilon_0 A}$$

$$C = \frac{k\epsilon_0 A}{fd + kd(1-f)} = \left( \frac{k}{f + k(1-f)} \right) \frac{\epsilon_0 A}{d}$$

$$C = \frac{k}{f + k(1-f)} \epsilon_0 A$$

Ch 27 Current and Resistance

$$I = \frac{\Delta Q}{\Delta t}$$

$$I = \frac{dQ}{dt}$$

$$\boxed{I = \frac{V}{R}}$$

$$\boxed{IS = \sigma L \cdot m}$$

$$J = \sigma E$$

$$\Delta V = IR$$

$$R = \frac{\rho L}{A} = \frac{l}{\sigma A}$$

$$\boxed{\sigma = \frac{1}{\rho}}$$

conductivity

~~conductivity~~

Ex. 27.2

$$0.32 \text{ mm} \rightarrow 3.2 \times 10^{-3} \text{ m}$$

$$\textcircled{A} \quad R = \frac{\rho}{L} = \frac{1.1 \times 10^{-6}}{\pi (0.32 \times 10^{-3})^2} = \frac{1.1 \times 10^{-2}}{10^{-4}} \Omega \text{ m}$$

$$\textcircled{B} \quad \Delta V = 10 \quad l = 1$$

$$I = \frac{\Delta V}{R} = \frac{10}{\frac{1.1 \times 10^{-6}}{\pi (0.32 \times 10^{-3})^2}} = 3.2 \text{ A}$$

Resistance and temperature

$$\rho = \rho_0 [1 + \alpha (T - T_0)]$$

$$\alpha = \frac{1}{\rho_0} \frac{\Delta \rho}{\Delta T}$$

Cubit

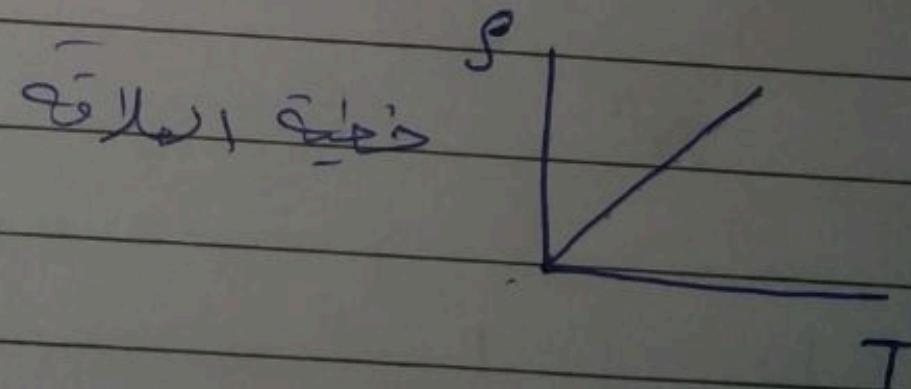
$$\alpha \rightarrow {}^\circ C^{-1}$$

$$R = \frac{\rho L}{A}$$

$$\frac{\rho L}{A} = \frac{\rho_0}{A} [1 + \alpha (T - T_0)]$$

$$R = R_0 [1 + \alpha (T - T_0)]$$

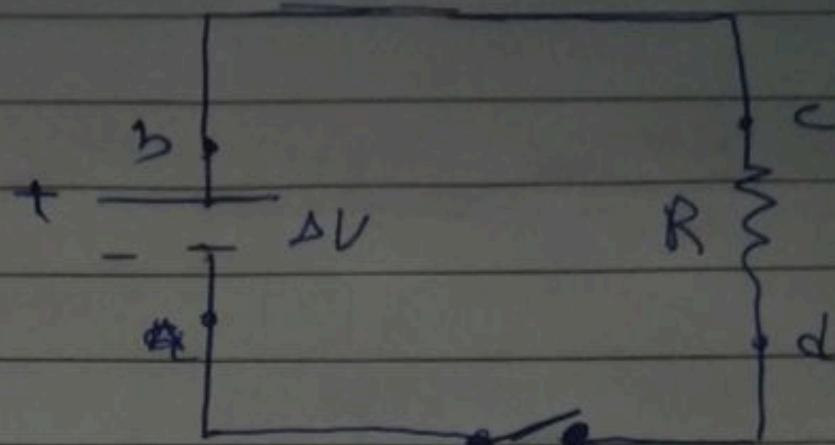
$$T \leftarrow T_0 + \alpha \Delta T$$



## 27.6 Electrical power

الطاقة الكهربائية

تحسب طاقة مجموع من  
إلى طاقة فعل  
 $R$  في



- The energy a when charged  $\Delta Q$  moved from a to b  $\frac{w_{\text{aff}}}{2000 \text{ J/s}}$
- $\rightarrow$  تحسب طاقة في حال فرق جهد بين

$$\Delta U = (\Delta Q)(\Delta V) \rightarrow R \text{ (حيث)} \Delta V = I \Delta U$$

$$P = \frac{\Delta U}{\Delta t} = \frac{\Delta Q}{\Delta t} \star \Delta V = I \Delta U$$

Power

$$\Delta U = R I$$

$$w_{\text{aff}} \left[ \frac{\text{J}}{\text{s}} \right]$$

$$P = I^2 R$$

$$P = \frac{\Delta U^2}{R}$$

$$\Delta U = P \Delta t$$

EX 27.4 $\overset{\rightarrow}{I}$  Current

$$\Delta V = 120$$

$$R = 8$$

$$\Delta V = IR$$

$$1) I = \frac{\Delta V}{R} = \frac{120}{8} = 15 \text{ A}$$

$$2) P = \frac{\Delta V^2}{R} = 1800 \omega = 1.8 \text{ kW}$$

EX 27.5

$$m = 1.5 \text{ kg} \quad T_1 = 10 \quad T_2 = 50 \quad T = 10 \text{ min} \quad \Delta V = 110 \text{ V}$$

$$R = \frac{(110)^2 (600)}{(1.5)(4186)(50-10)} = 28.9 \Omega$$