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دفتر

# خرسانة مسلحة 1

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# CH 1: Introduction..

DATE: 5/2

8/3 → 10-11

4/4 → 9.30-10.30

## \* Advantages (For Concrete).

- 1] Relatively a low cost material.
- 2] Fire resistance (1-3hrs) fire rating without special fire proofing.
- 3] Suitability of material for architectural & structural functions.
- 4] Rigidity.
- 5] Low maintenance.
- 6] Availability of materials.

## \* Disadvantages

- 1] Low ~~ten~~ tensile strength of conc.
- 2] Forms & shoring.
- 3] Relatively low strength per unit weight or volume.
- 4] Time-Dependent volume changes:
  - \* Drying Shrinkage (Shrinkage).
  - \* Creep (Strains under sustained loads).

## \* Importance of Steel

- 1] Steel has aged bond with concrete.
- 2] Concrete & steel have nearly equal coefficients of thermal expansion.
- 3] Good dense concrete protects steel from corrosion/rusting.

## \* Sources of uncertainty

- 1] Actual load magnitude & distribution may differ from those assumed in the design.

(1)

2) Assumptions & simplifications in the analysis may result in different internal forces.

3) Actual behavior may be different.

4) Actual member dimensions may differ from those specified in the design.

5) Reinforcement may not be in its proper position.

6) Actual materials strength may be different from that specified in the design.

### \* Safety Philosophy:

$$\text{Strength reduction factor } \phi_{sn} \geq \frac{\gamma Q_d}{\phi_{sn}} \rightarrow \text{Over load factor } > 1$$

(.65-.9)

nominal strength ↓  
Reduce strength. ↓

Design load.  
Ultimate load (factored load).

\* Load factors & load combinations from ACI-code:

$$U = 1.2 DL + 1.6 LL$$

↓ principle variable load. → 1 < d/b < 1

$$U = .9 DL + 1.6 WL$$

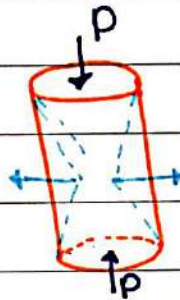
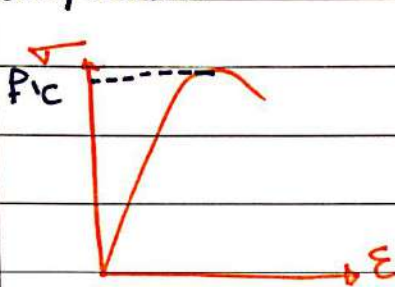
↓ Companion action variable load. 1 > d/b < 1

(2)

# CH: Materials

DATE: 7/2/2018

- \* Mechanism of failure in conc. loaded in compression.
- \* Stage of microcracking & failure in conc. subjected to uniaxial compression:



تension من اليمين واليسار  
تحت تأثير الضغط، Comp. من اليمين واليسار

1] Shrinkage of the paste during hydration (No-load bond cracks)  
↓  
تقلص البستة أثناء التصلب

2] At stresses up to 30 to 40% of the comp. strength → Bond cracks.

discontinuity limit → 3] At stresses up to 50 to 60% of the comp. strength → mortar cracks.  
↓  
تقارب بين الحبيبات

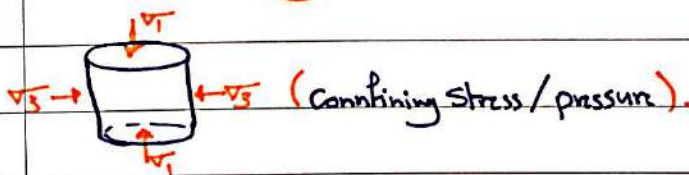
Stable propagation → 4] At stresses up to 75% of the ultimate load.

critical stress → ↳ Number of mortar cracks increases.

unstable cracks → ↳ Fewer undamaged portions to carry the load.

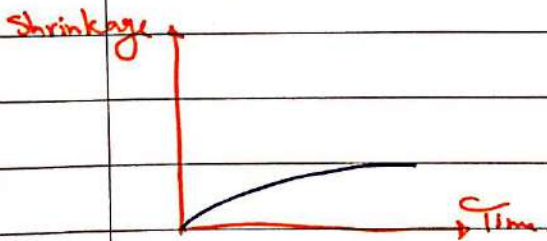
Propagation.

## \* Triaxial loading

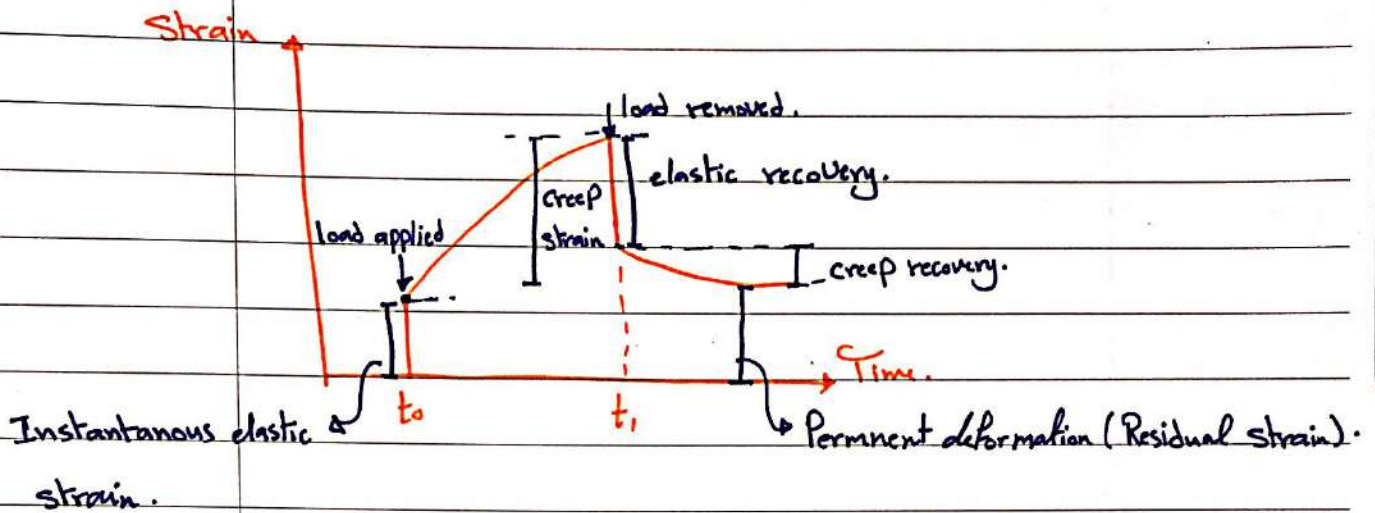


## \* Time-Dependent Volume Changes

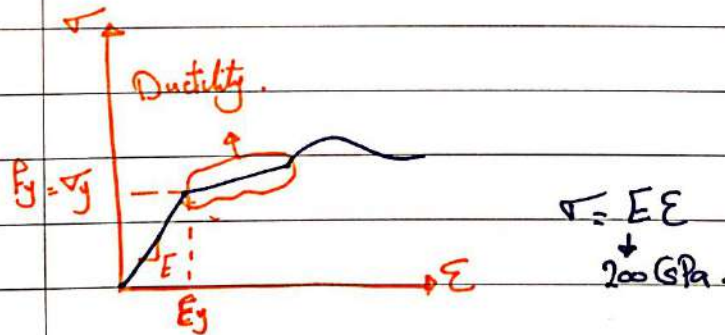
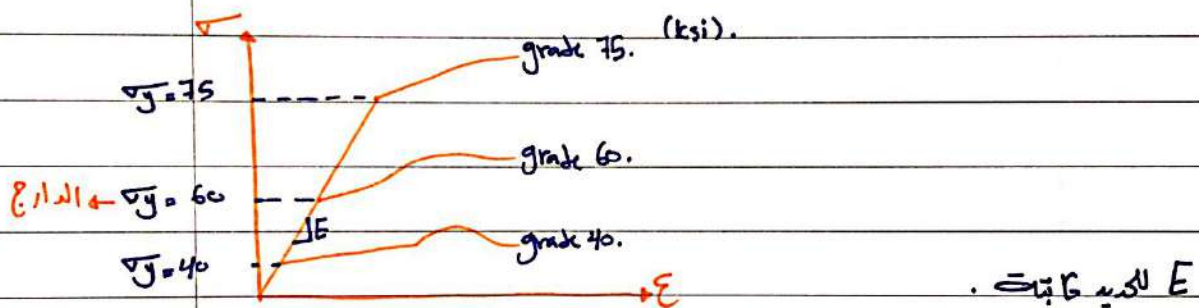
1. Drying Shrinkage (shrinkage).



## 2. Creep: deformations/strains under sustained load.



### \* Reinforcement \*



CH 38

\* The Design Process (objective of the design): (The structure should satisfy)

1] Appropriateness: Designed to serve it's intended use.

2] Economy: Over all cost doesn't exceed client's budget.

3] Structural Adequacy: structure must → Be strong enough to support all anticipated load.

Not deflect, tilt, vibrate or crack in away that affects it's usefulness.

4] Maintainability: minimum & simple maintenance.

## \* The Design Process

Phase I: Defining Client's needs & priorities.

Phase II: Development of project concepts

↳ Number of possible layouts.

↳ Preliminary cost estimates.

Phase III: Design of individual systems.

## \* Limit states & The Design of R.C:

When a structure or an element become unfit for it's intended use it is said to have reached a limit state.

### \* Groups of limit state:

1) **Ultimate limit state:** Involve structural collapse of part or all the structure:

↳ loss of equilibrium.

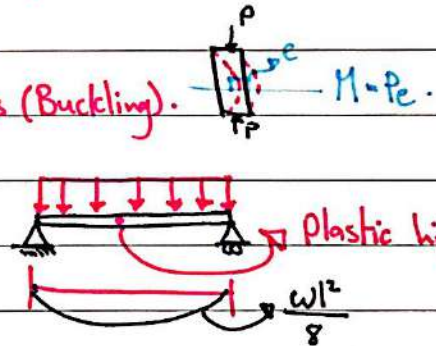
↳ Rupture of critical parts of the structure.

↳ Progressive collapse.

↳ Instability due to deformations (Buckling).

↳ Fatigue.

↳ Formation of plastic mechanism.



2) **Serviceability limit state:** Involves disruption of the functional use of the structure (but not collapse).

↳ Excessive deflections.

↳ Undesirable vibrations.

↳ Excessive crack widths.

3) Special limit state. Involves damages or failure due to up normal conditions.

- ↳ Extreme earthquakes.
- ↳ Fire → explosions.
- ↳ Vehicular collisions.

\* Limit State Design Process:

- Identification of all potential modes of failure.
- Determination of acceptable level of safety per ACI-code.

\* Structural Safety:

- Sources of uncertainty.
- consequences of failure.
  - ↳ loss of life
  - ↳ Cost of clearing debris.
  - ↳ Cost of society in lost time.

\* Design Procedures Specified in the ACI-code:

1) Strength design:  $\phi S_n \geq \gamma Q_d$ .

2) Working-stress-design:  $\phi S_n \geq Q_d \rightarrow$  service load / working load.

3) Plastic-Capacity-limit Design: concedes redistribution of moments as successive cross sections yield.

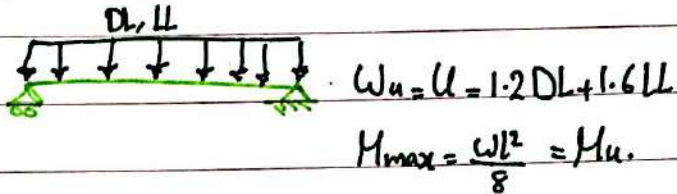
\* Loading & Actions:

- ↳ Permanent loads.
- ↳ Accidental loads.
- ↳ Variable loads → Sustained loads (long-duration).
  - ↳ Short duration.

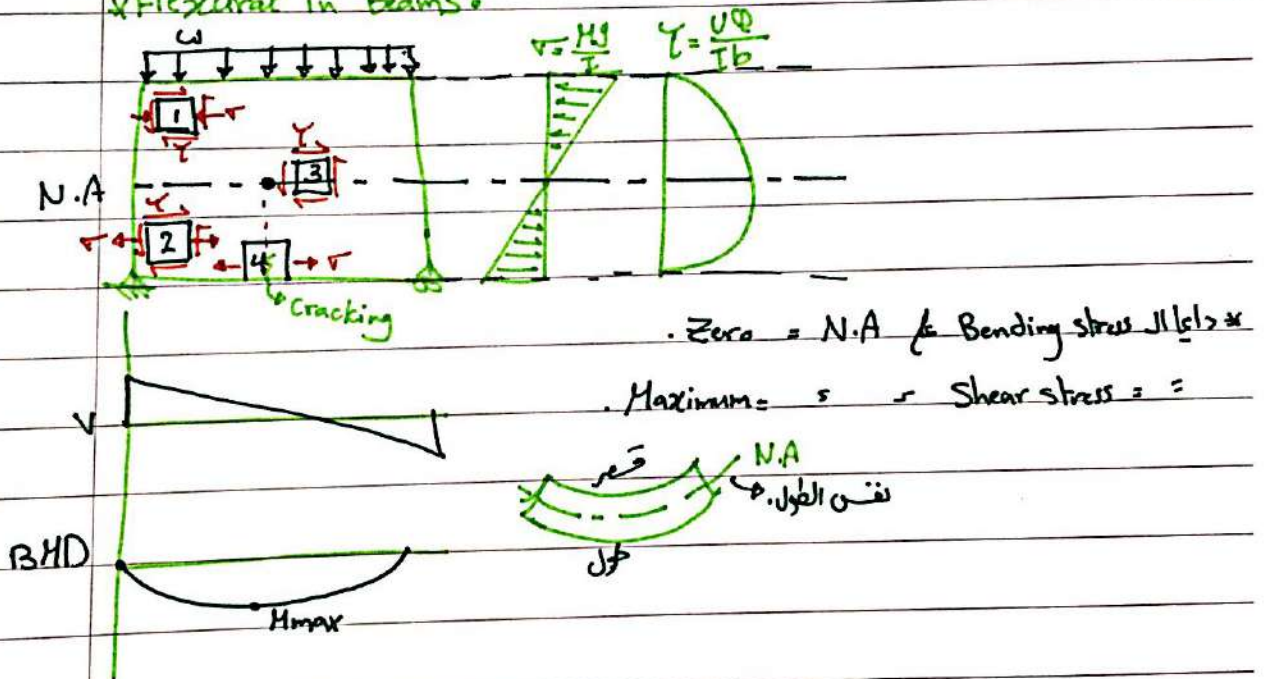
Flexure & Basic Concept (Rectangular Beams).

$\phi S_n \geq \phi D$

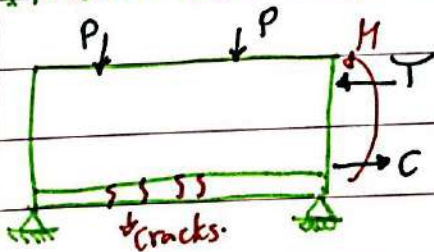
Strength reduction (.85-.9) in analysis  $\phi M_n \geq M_u$  (Basic safety eqn for flexure).  
 ↳ Ultimate moment  
 ↳ nominal moment capacity.



\* Flexural in beams:



\* Flexural behavior (Laboratory Testing).



\* Stage A: Before Cracking.

\* Stage B: Cracking.

\* Stage C: After cracking before yielding of reinforcement.

Transfer of tensile force from conc. to steel.

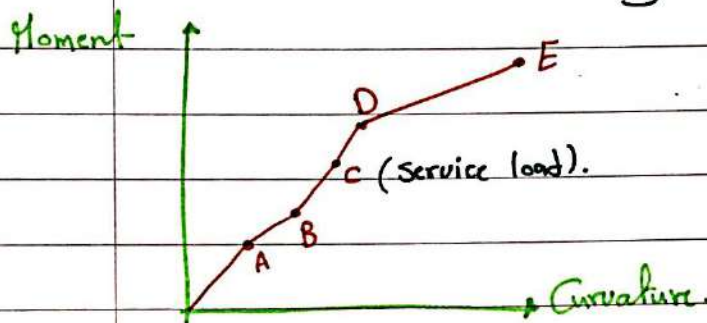


\* Stage D is yielding of reinforcement.

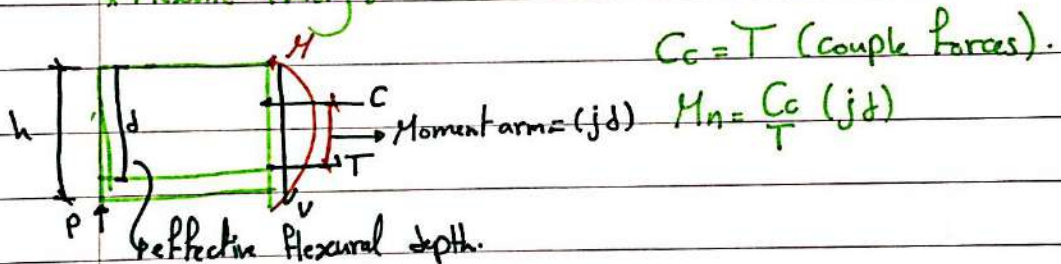
Curvature increases rapidly with very little increases in the moment.

\* Stage E is Failure.

Beam failed as a result of crushing of the conc. on the top of the beam.

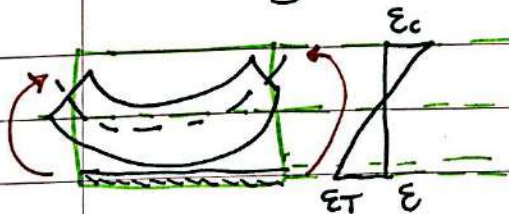


\* Flexure Theory:



Pr \* Basic Assumptions in flexural theory:

1] Sections perpendicular to the axis of bending that are plane before bending remain plane after bending.



2] The strain in the reinforcement is equal to the strain in the conc. at the same level (Perfect bond).

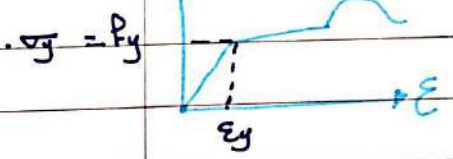
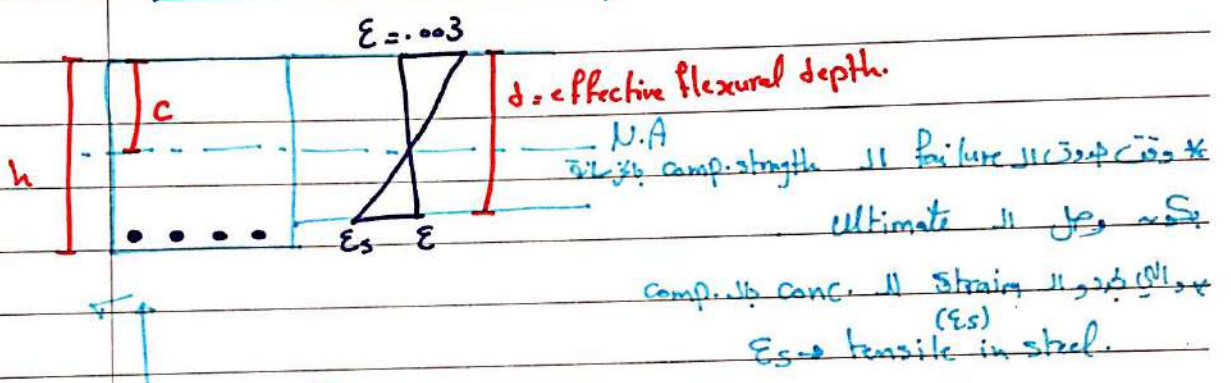
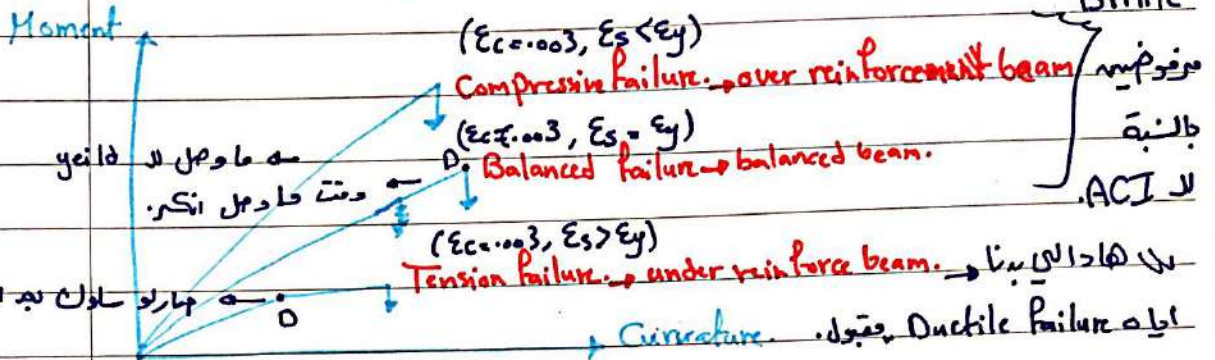
3] The tensile strength of concrete is neglected in flexural strength calculations.

4] Concrete is assumed to fail when the maximum compressive ~~strength~~ strain reaches limiting value

$$\epsilon_c = \epsilon_{cu} = 0.003.$$

(9)

\* Flexure failure may occur in three different ways



$\sigma = E \epsilon$   
 $F_y = E \epsilon_y, \epsilon_y = \frac{F_y}{E}$

grade 60  $\rightarrow F_y \cong 420 \text{ MPa}, \epsilon_y = .0021$

$\epsilon_s = .0022 \rightarrow$  قبل (Tensile failure).

$\epsilon_s = .0019 \rightarrow$  بعد (Compressive failure)  $\rightarrow$  ال قوت ال.

\* Strain limits methods for Analysis & Design

- Per ACI-code  $\rightarrow$  4 types of failure.

Compression controlled failure.

Transition controlled failure.

Tension controlled failure.

Compression controlled beam.

Transition controlled beam

Tension controlled beam.

Balanced failure Beams.

$E_s = \epsilon_y$

$E_s \geq \epsilon_y$   
 $E_s = .005$   
 $E_y$  (تحويل)

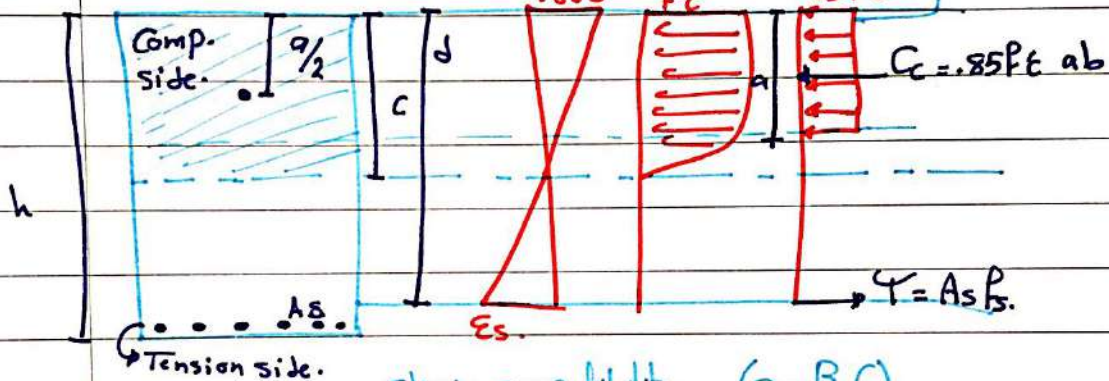
$E_s$   
 $E_s \geq .005$

Assumed equivalent stress block.

$\epsilon_c = .003$

Flexural Theory ( $M_n$ ).

$\sigma = \frac{My}{I}$  (Normal)

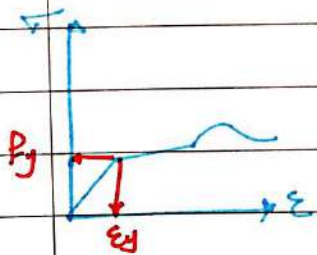


strain compatibility. ( $a = \beta_1 c$ )

$\frac{.003}{c} = \frac{\epsilon_c}{d-c} \rightarrow \epsilon_s = .003 \left( \frac{d-c}{c} \right)$

$jd = (d - \frac{a}{2})$

For rectangular beams only, rectangular comp. Area.



if  $E_s < E_y$  (Not yield),  $F_s = E E_s$ .

if  $E_s \geq E_y$  (yielded)  $\rightarrow (F_s = F_y)$ .

Equilibrium:

$T = C_c$

$A_s F_s = .85 f_c' b a$  (Assume  $E_s \geq E_y$ ,  $F_s = F_y$ ).

$A_s (F_y) = .85 f_c' b a$ .  $\rightarrow F_s = E E$  (if not yielded) \* بل ان كان في المنطقة المرونة \*

$a = \frac{A_s F_y}{.85 f_c' b} \rightarrow$  check Assumption.

$M_n = \frac{T}{C_c} (d - \frac{a}{2})$

normal uniform stress.

$$T = C_c$$

$$A_s f_s = 0.85 f'_c ab, \quad f_s \rightarrow \epsilon_s \geq \epsilon_y, (f_s = f_y)$$

$$M_n = T (jd)$$

$$jd = (d - a/2) \rightarrow \text{rectangular approx. comp. areas}$$

$$\epsilon_s = .003 \left( \frac{d-c}{c} \right)$$

$$\epsilon_s < \epsilon_y, \quad f_s \neq f_y, \quad \text{لوماسته مزمنين}$$

$$f_s = E \epsilon_s \rightarrow E (.003) \left( \frac{d-c}{c} \right)$$

$$(.85 f'_c b \beta_1) c^2 + (A_s E .003) c - A_s E .003 d = 0$$

لغتمه نهج

$$A_s E (.003) \left( \frac{d-c}{c} \right) = .85 f'_c a b \rightarrow (\beta_1, c)$$

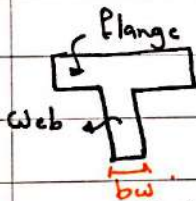
\* Minimum amount of Tension Reinforcement ( $A_{s \min}$ ) per ACI-Cod.

اقل مقدار از فولاد در مقطع

$$A_{s \min} = \text{larger of } \begin{cases} .25 \frac{\sqrt{f'_c}}{f_y} b w d \\ \frac{1.4}{f_y} b w d \end{cases}$$

سبب داشتن d, f'\_c, f\_y

for rectangular & T beams.



\* Value of  $\beta_1$  =

$$\beta_1 = .85 \quad (f'_c \leq 28 \text{ MPa})$$

$$\beta_1 = .85 - .05 \frac{f'_c - 28}{70} \quad (28 < f'_c \leq 56)$$

$$\beta_1 = .85 \quad (f'_c \geq 56 \text{ MPa})$$

\* الكتله هو فقط دسي لا عرف

مقدار دسي و دسي ال دسي

تجربا

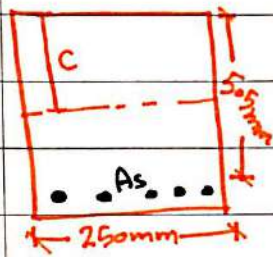
\* Values of  $\phi$ : ( $\phi M_n \geq M_u$ )

$$\phi = .9 \quad (\text{Tension-Controlled}). \quad (\epsilon_s \geq .005)$$

$$\phi = .65 + (\epsilon_s - .002) \left( \frac{250}{3} \right) \quad (\text{Transition}). \quad (\epsilon_y < \epsilon_s < .005)$$

$$\phi = .65 \quad (\text{Balanced & compression}). \quad (\epsilon_s \leq \epsilon_y)$$

### \* Analysis Example (Design Moment Capacity; $\phi M_n$ ).



\* Compute  $a$ :

$$T = C \quad (\text{Assumed: } \epsilon_s \geq \epsilon_y, f_s = f_y).$$

$$A_s f_y = .85 f'_c a b.$$

$$(1530)(420) = .85(20)a(250)$$

$$a = 151.2 \text{ mm.}$$

$$A_s = 1530 \text{ mm}^2.$$

$$f'_c = 20 \text{ MPa.}$$

$$f_y = 420 \text{ MPa.}$$

\* Check Assumption:

$$c = \frac{a}{\beta_1} = \frac{151.2}{.85} = 177.9 \text{ mm.}$$

$$\epsilon_s = .003 \left( \frac{505 - 177.9}{177.9} \right) = .0055$$

$$\epsilon_y = \frac{420}{200000} = .0021$$

$\epsilon_s > \epsilon_y \rightarrow$  Assumption is ok.

\* Compute  $M_n$  &  $\phi M_n$ :

$$M_n = A_s f_y \left( d - \frac{a}{2} \right)$$

$$= (1530)(420) \left( 505 - \frac{151.2}{2} \right)$$

$$M_n = 275.9 \text{ kN}\cdot\text{m.}$$

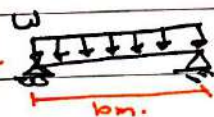
( $\epsilon_s \geq .005$ ) (Tension-controlled).

$$\phi = .9$$

$$\phi M_n = (.9)(275.9) = 248.3 \text{ kN}\cdot\text{m.}$$

kN.m  $\rightarrow$   $10^6$  ؟

..  $\omega$   $\rightarrow$   $50$  ؟



$$\frac{wL^2}{8} = 248.3 \quad \dots \text{دجاج ال } \omega \rightarrow$$

\* Check  $A_s$  min.

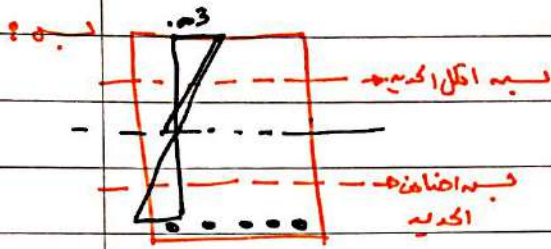
$$A_s \text{ min} \left\{ \frac{.25 \sqrt{f'_c}}{f_y} \times 250 \times 505 = 336 \text{ mm}^2. \right.$$

$$\left. \frac{1.4}{f_y} \times 250 \times 505 = 420 \text{ mm}^2. \right.$$

$$A_s \text{ min} = 420 \text{ mm}^2.$$

$$A_s = 1530 > A_s \text{ min} \rightarrow \text{Ok.}$$

تحتي الزوال اضافي  $A_s = 3060 \text{ mm}^2$



في وقت طريقة ج

الاجل اضافي

\* Compute  $a$ :

$$3060 + 470 = .85 (20) (a) (250)$$

$$a = 302.4 \text{ mm.}$$

\* check assumption:

$$c = \frac{a}{\beta_1} = \frac{302.4}{.85} = 355.8 \text{ mm.}$$

$$\epsilon_s = .003 \left( \frac{505 - 355.8}{355.8} \right) = .00126$$

$$\epsilon_s = .003 \left( \frac{505 - 312.66}{312.66} \right) = .00184 < \epsilon_y \rightarrow \text{Ok. } \nabla$$

$$f_s = (200 \times 10^3) (.00184) = 368 \text{ MPa.}$$

\* Compute  $M_n$  &  $\phi M_n$ :

$$M_n = A_s f_s (d - \frac{a}{2}) = 3060 (368) (505 - \frac{302.4}{2}) = 419 \text{ kN}\cdot\text{m.}$$

$$\epsilon_s < \epsilon_y \text{ (Comp. } \rightarrow .65 = \phi).$$

$$\phi M_n = (.65)(419) = 272.4 \text{ kN}\cdot\text{m.}$$

\* Check  $A_{min} \rightarrow \text{ok. } \nabla$

$\epsilon_s < \epsilon_y \rightarrow \text{Not Ok. } \nabla$

$$A_s (f_s = E \epsilon_s) = .85 \beta_1 c \beta_c b$$

$$3060 \times 200 \times 10^3 \times .003 \left( \frac{505 - c}{c} \right) = .85 \times 20 \times .85$$

$$\times c \times 250$$

$$3618.5 c^2 + 1836000 c - 927180000 = 0$$

$$c = -25412 \pm 566.78$$

$$c = 312.66 \text{ mm.}$$

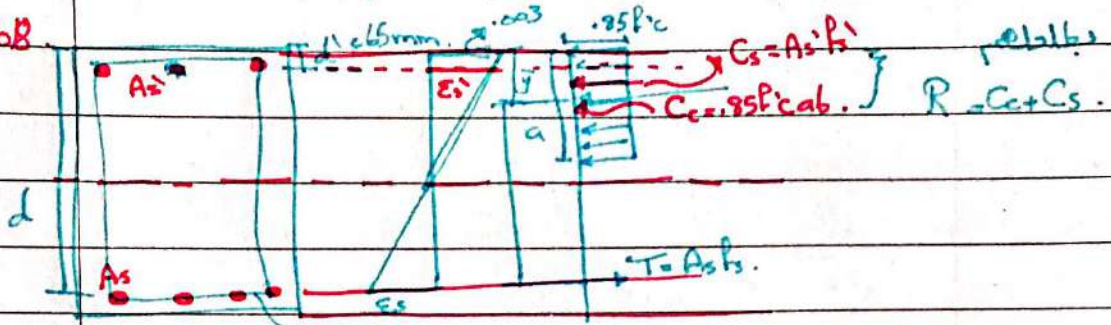
(Doubly reinforcement).

\* Beams with Compression Reinforcement

DATE: 26/2/2018

First 8/3/2018

10-11



$$\epsilon_s = .003 \left( \frac{d-c}{c} \right) \quad \text{Stirrups.}$$

$$\epsilon_{s'} = .003 \left( \frac{c-d'}{c} \right).$$

$$\int \bar{x} \epsilon A_i = \epsilon A_i x_i$$

$$* T = C_c + C_s$$

$$As fs = .85 f_c' c a b + As' fs'$$

\* Assume  $\epsilon_s \geq \epsilon_y$  ( $f_s = f_y$ ).

$\epsilon_{s'} \geq \epsilon_y$  ( $f_{s'} = f_y$ ).

$$As f_y = .85 f_c' c a b + As' f_y$$

$$a \rightarrow c \quad \frac{b}{f_c}$$

$$f_{s'} = E \epsilon_{s'} = E (.003) \left( \frac{c-d'}{c} \right)$$

1)  $\epsilon_{s'}$  check. (not ok,  $\epsilon_{s'} < \epsilon_y$ )

2)  $\epsilon_s$  check. (not ok)  $f_s = E \epsilon_s = E (.003) \left( \frac{d-c}{c} \right)$

وإذا كان  $\epsilon_s < \epsilon_y$

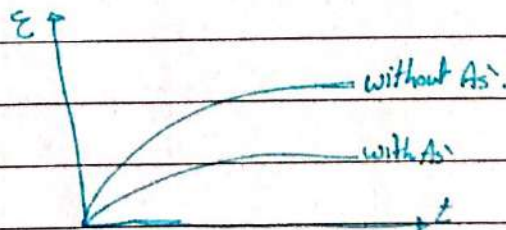
$$* M_u = C_c \left( d - \frac{a}{2} \right) + C_s (d - d')$$

\*  $\partial M_u$

$$\rightarrow As \rightarrow \epsilon_s$$

\* Reasons for providing  $As'$

1) Reduce sustained load deflections.





2) Increase Ductility, ( $\epsilon_s$ ).

3) Change Mode of Failure to Tension-controlled.

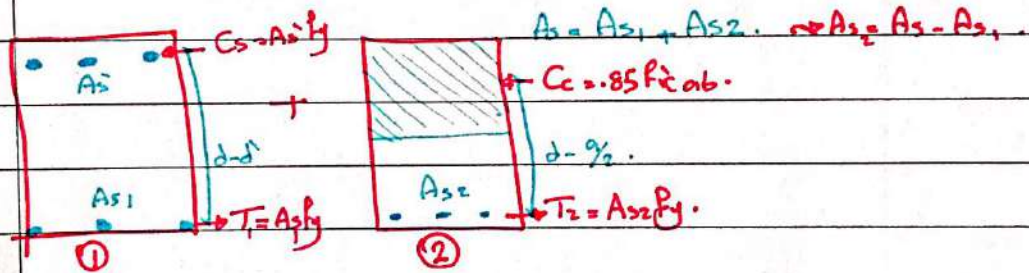
4) Fabrication Ease: Providing small bars @ the corners of the stirrups to hold the stirrups in place & help anchor the stirrups.

→ Ignore in strength calculations.

\* Analysis of beams with  $A_s$  &  $A_s'$ .

$$\epsilon_s \geq \epsilon_{cy}$$

\* Case I:  $\epsilon_s' \geq \epsilon_{cy}$ .



$$T_1 = C_s$$

$$T_2 = C_c$$

$$A_s1 f_y = A_s' f_y$$

$$A_s2 f_y = .85 f_c' ab$$

$$A_s1 = A_s'$$

$$M_{n2} = C_c (d - \gamma/2)$$

$$M_n = C_s (d - d'')$$

$$M_n = M_{n1} + M_{n2}$$

\* Case II:  $\epsilon_s' < \epsilon_{cy}$ .

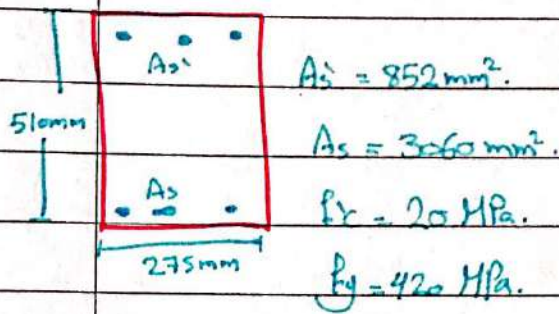
$$T = C_c + C_s$$

$$A_s f_y = .85 f_c' ab + A_s' f_s'$$

$$\hookrightarrow E \epsilon_s' = E (\infty) \left( \frac{c-d''}{c} \right)$$

$$.85 f_c' b d^2 + (.003 E A_s' - A_s f_y) a - .003 E A_s' f_s' d = 0.0$$

## \* Analysis Example :

\* Compute  $a$ :

$$T = C_c + C_s$$

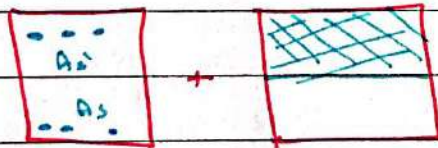
assume  $\epsilon_s > \epsilon_{sy}$  &  $\epsilon_s' > \epsilon_{sy}$

$$A_s f_y = .85 f_c' a b + A_s' f_y$$

$$(3060)(420) = (.85)(20) a (275) + (852)(420)$$

$$a = 198 \text{ mm.}$$

assumed  $\epsilon_s$  is  
OK



$$A_{s1} = 852 \text{ mm}^2 \quad A_{s2} = 2208$$

$$a = 198 \text{ mm.}$$

## \* Check Assumptions.

$$c = \frac{198}{.87} = 233 \text{ mm.}$$

$$\epsilon_s' = .003 \left( \frac{233 - 65}{233} \right) = .0022 > \epsilon_{sy} = .0021 \quad \text{ok. } \nabla$$

$$\epsilon_s = .003 \left( \frac{510 - 233}{233} \right) = .0036 > \epsilon_{sy} = .0021 \quad \text{ok. } \nabla$$

\*  $M_u$  &  $\phi M_u$ .

$$M_u = C_c (d - a/2) + C_s (d - d')$$

$$= (.85)(20)(198)(275)(510 - \frac{198}{2}) + 852(410)(510 - 65) = 540 \text{ kN}\cdot\text{m.}$$

$$\epsilon_y < \epsilon_s < .005$$

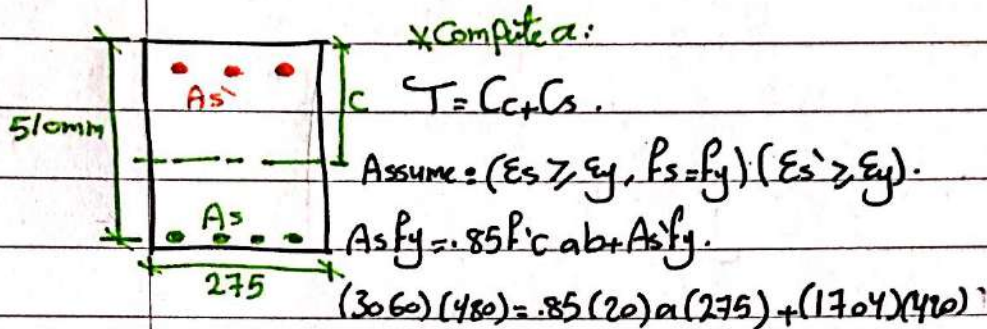
$$\phi = .65 + (.0036 - .002) \left( \frac{250}{3} \right) = .781$$

$$\phi M_u = (.781)(540) = 423 \text{ kN}\cdot\text{m.}$$

\* Check  $A_{s \min}$ : ( $A_s$ ).

28/2/2018

\* Example 8



$$A_s' = 1704 \text{ mm}^2 \quad a = 121.8 \text{ mm.}$$

$$A_s = 3060 \text{ mm}^2 \quad C = \frac{a}{\beta_1} = 143.3 \text{ mm.}$$

$$f_c' = 20 \text{ MPa.}$$

$$f_y = 420 \text{ MPa.}$$

\* Check assumptions:

$$\epsilon_s' = .003 \left( \frac{143.3 - 65}{143.3} \right) = .0016$$

$\epsilon_s' < \epsilon_y \rightarrow$  Not ok.  $\nabla$

$$A_s f_y = .85 f_c' a b + A_s' f_s' \rightarrow [E_s .003 (c - d)].$$

$$3973.75 c^2 + 262800 c - 6645600 = 0$$

$$c = 33.07 \pm 133.48$$

$$c = 166.55 \text{ mm.}$$

$$\alpha = \beta_1 c = 141.57 \text{ mm.}$$

\* Check  $\epsilon_s$ :

$$\epsilon_s = .003 \left( \frac{510 - 166.55}{166.55} \right) = .0062, \quad \epsilon_s > \epsilon_y \rightarrow \text{Ok. } \nabla$$

(18)

\* Compute  $M_n$  &  $\phi M_n$ .

$$M_n = C_c(d - g/2) + C_s(d - d')$$

$$E_s' = .003 \left( \frac{166.55 - 65}{166.55} \right) = .0018 < \epsilon_y$$

$$P_s' = .0018 \times (200,000) = 360 \text{ MPa}$$

$$M_n = .85(20)(141.57)(275) \left( \frac{510 - 141.57}{2} \right) + (1704 \times 360)(510 - 65) = 8563.7 \text{ kN.m}$$

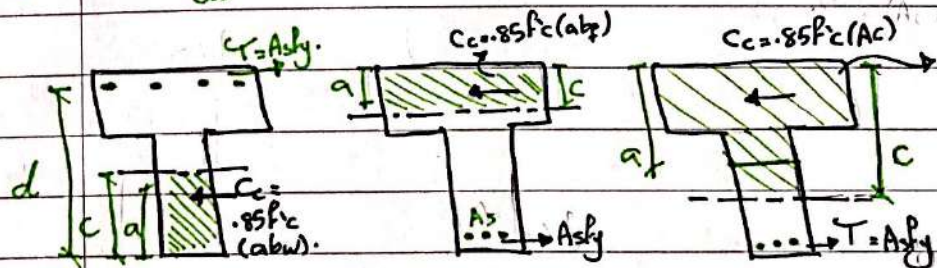
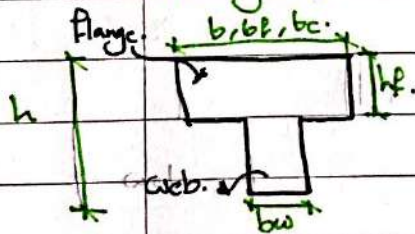
$$E_s > .005 \rightarrow \text{Tension} \rightarrow \phi = .9$$

$$\phi M_n = .9(8563.7) = 7707.3 \text{ kN.m}$$

\* Check  $A_s$  min  $\rightarrow$  Ok..!

Prescrip  $\rightarrow A_s \rightarrow \phi M_n$  (design)  
 $A_s \rightarrow M_n$  (design)

\* Analysis of T-Beams:



نقسم الشكل قتل  
 حسب  $A_s$  و  $h_f$

Case I (-ve M).

Case II: (+ve M).

Case III: (+ve M).

Flange in Tension.

Flange in Comp.

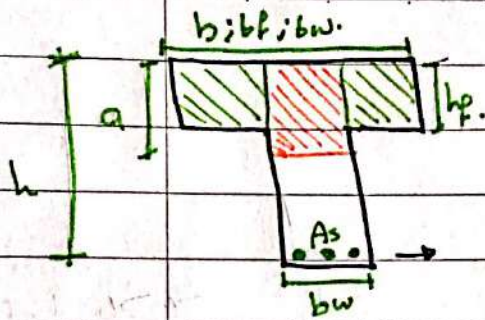
Flange in Comp.

$$M_n = T(d - g/2)$$

$$M_n = T(d - g/2)$$

$$a > h_f$$

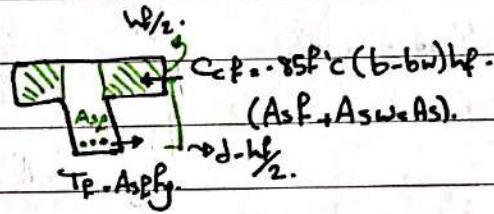
$$a \leq h_f$$



C, L, I Joins  
beams

\* Analysis of Nominal moment capacity for Flanged sections in positive Bending ( $a > hf$ ).

\* Beam Flange (beam F).



$C_F = C_{cf}$

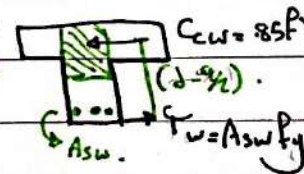
$C_{cf} = .85 f_c (b - b_w) h_f$

$A_{sf} = A_s - A_{sw}$

$A_s = A_{sf} + A_{sw}$

$M_{nf} = \frac{C_{cf}}{f_y} (d - \frac{h_f}{2})$

\* Beam web (Beam W).



$C_w = C_{cw}$   
 $C_{cw} = .85 f_c (a) b_w$   
 $A_{sw} f_y = .85 f_c (a) b_w$

$M_{nw} = \frac{C_w}{C_{cw}} (d - \frac{a}{2})$

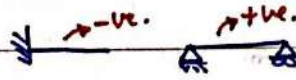
\*  $M_n = M_{nf} + M_{nw}$

~

13/3 → RCI. \* Modification to  $A_{s \min}$ :

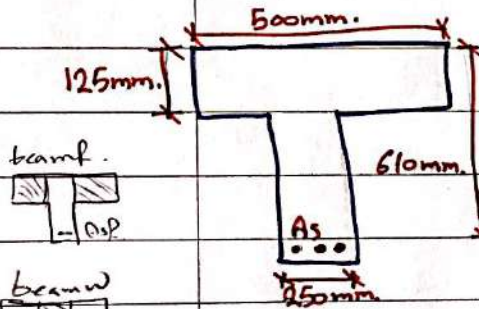
11/3 → foundation.  $A_{s \min} = \sqrt{\frac{f_c}{4f_y}} bwd.$

15/3 →  $\frac{1.4}{f_y} bwd.$



\* For statically determinate beams when the flange portion is in tension ACI-code recommends that  $b_w$  be replaced by smaller of  $\frac{1}{2}b_w$  or  $b_f$ .

Example:



\* Compute  $a$ :

$T = C$  (assume  $E_s \geq E_y$ ) (assume  $a \leq h_f$ ).

$A_s f_y = .85 f'_c a b_f$

$(3060)(420) = .85(20)a(500)$

$a = 151.2 \text{ mm} > h_f \rightarrow T\text{-beam action.}$



The Moment capacity } Beam f:

$f'_c = 20 \text{ MPa}, f_y = 420 \text{ MPa.}$  }  $T_f = C_f$

$A_s = 3060 \text{ mm}^2.$  }  $A_s f_y = .85 f'_c (b - b_w) (h_f)$

$(3060)(420) = .85(20)(500 - 250)(125)$

$A_{sf} = 1264.9 \text{ mm}^2$

$A_{sw} = 3060 - 1264.9 = 1795.1 \text{ mm}^2$

Beam w:

$T_w = C_w$

$A_{sw} f_y = .85 f'_c a b_w$

$(1795.1)(420) = .85(20)a(250)$

$a = 177.4 \text{ mm. } C = 208.7 \text{ mm.}$

$E_s = .003 \left( \frac{610 - 208.7}{208.7} \right) = .0058 > E_y \rightarrow \text{ok.}$

\*  $M_n$  &  $\phi M_n$

\* Check  $A_s$  min  $\rightarrow$  ok!

$$M_n = A_s f_y (d - \frac{1}{2})$$

$$= 290.9 \text{ kN}\cdot\text{m}$$

$$M_{nw} = A_{sw} f_y (d - \frac{9}{2}) = 393 \text{ kN}\cdot\text{m}$$

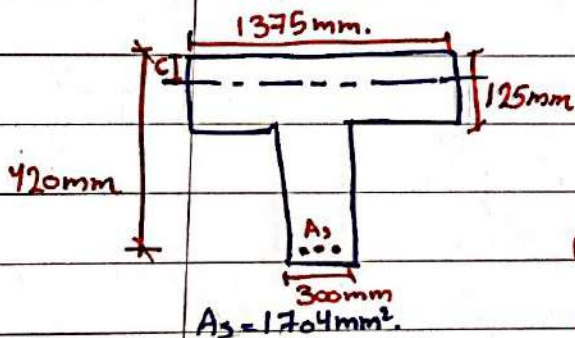
$$M_n = 683.9 \text{ kN}\cdot\text{m}$$

$$\phi M_n = .9 (683.9) = 615.5 \text{ kN}\cdot\text{m}$$

$$\phi = .9 (E_s > .005 \text{ no Tension})$$

~

Example:



$$A_s = 1704 \text{ mm}^2$$

$$f_c = 20 \text{ MPa}$$

$$f_y = 300 \text{ MPa}$$

\* Compute  $a$ :

$$T = C (E_s > E_y, a \leq h_f)$$

$$A_s f_y = .85 f_c' a b$$

$$(1704)(300) = .85(20)a(1375)$$

$$a = 21.9 \text{ mm}, C = 25.8 \text{ mm}$$

$$E_s = .003 \left( \frac{420 - 25.8}{25.8} \right) = .046 > E_y \rightarrow \text{ok!}$$

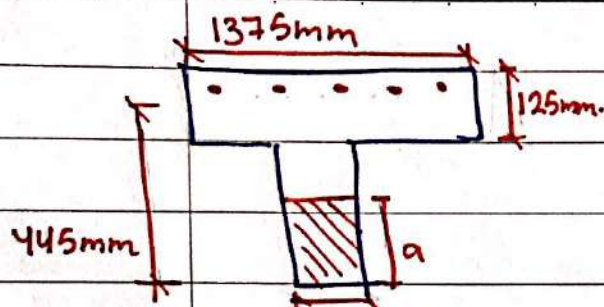
$$M_n = A_s f_y (d - \frac{a}{2}) = 1704 \times 300 \left( 420 - \frac{21.9}{2} \right) = \boxed{29.12} \text{ kN}\cdot\text{m}$$

$$\phi = .9 \rightarrow E_s > E_y \rightarrow \text{Tension}$$

$$\phi M_n = 188 \text{ kN}\cdot\text{m}$$

~

(92)



$$f'_c = 20 \text{ MPa.}$$

$$f_y = 300 \text{ MPa.}$$

$\phi M_n \rightarrow$  Indeterminate  
beam.

$$\gamma = C \quad (\epsilon_s \geq \epsilon_y).$$

$$(2275)(300) = .85(20)a(300)$$

$$a = 133.6 \text{ mm.}$$

$$\epsilon_s = .0055$$

$$M_n = A_s f_y (d - a/2)$$

$$\phi = .9$$

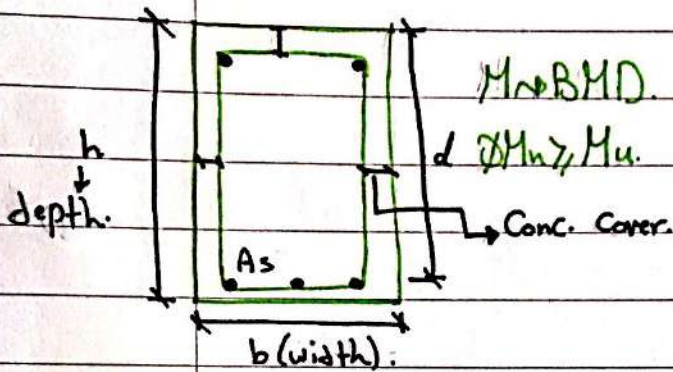
$$\phi M_n = 232 \text{ kN.m.}$$

\* first

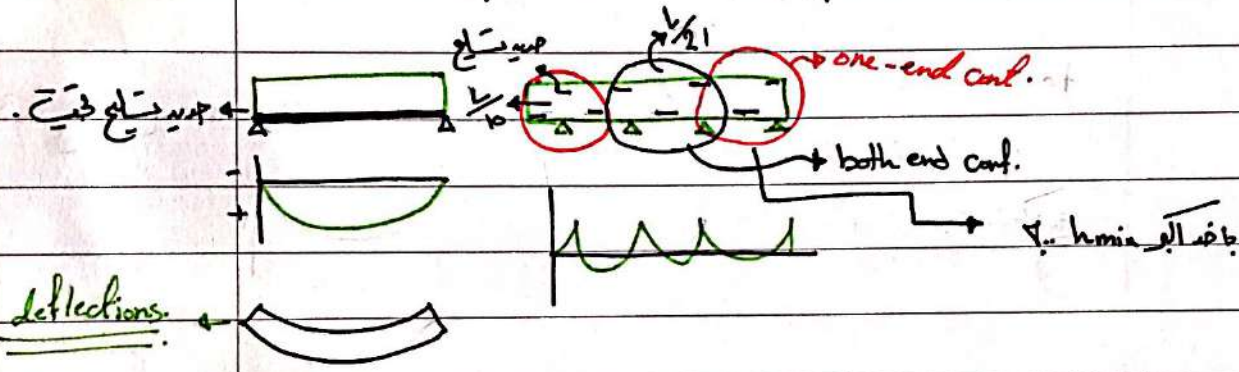
(23)



\* Design of rectangular beams:



\* Visualize expected deflected shape.



\* Relation-Ship between Beam depth & deflections:

from ACI-code (h<sub>min</sub> to avoid deflection calculations) (Table 9.5a).

Simply supported beam:  $h_{min} = \frac{l}{16}$

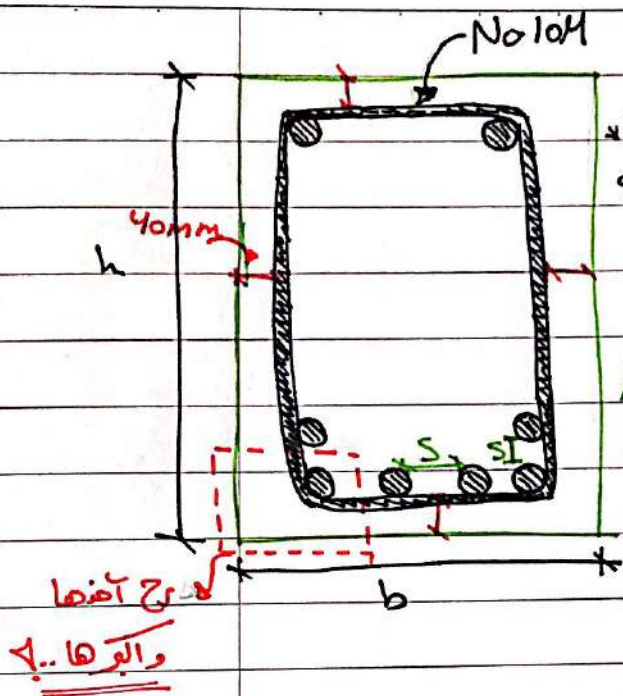
Cantilever beam:  $h_{min} = \frac{l}{8}$

\* Concrete cover & Bar spacing (Per ACI-code).

min. cover = 40mm (beams) (Normal exposure).

\* Reasons for cover.

- 1] Bond.
- 2] Corrosion (rusting of steel).
- 3] strength loss & overheating (fire).



\* Horizontal spacing:

$S_{min} = \text{larger of:}$

↳ Bar diameter  $\leq d_b$ .

↳ 1.33 max. size of coarse aggregate.

↳ 25mm / diameter of vibrator.

\* Vertical spacing:

$S_{min} = \text{larger of:}$

↳ 1.33 max. size of coarse aggregate.

↳ 25mm.

spacing.

$$* b_{min} = 2(40) + 2(10) + 6(20) + 5(25) = 345 \text{ mm.}$$

6 No. 20M  $\rightarrow$  design

$b = 350 \text{ mm}$  (Design)  $\rightarrow$  ok! (one layer).

$b = 300 \text{ mm}$  (Per design)  $\rightarrow$  Not ok! (should be in 2 layers).

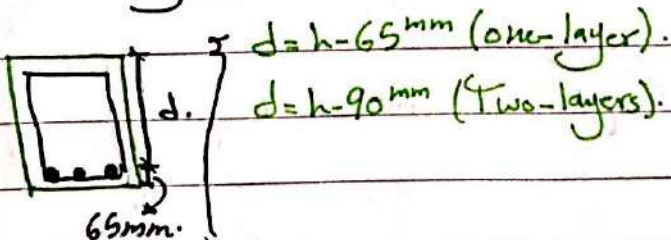


Extra distance =  $(2d_s - 5d_b)$

$$\frac{2(10) - 5(20)}{2(10) - 5(20)} = 10 \text{ mm}$$

$$b_{min} = 345 + 20 = 365 \text{ mm.}$$

\* Estimating  $d$  of a beam:



$d = h - 65 \text{ mm}$  (one-layer).

$d = h - 90 \text{ mm}$  (Two-layers).

(25)

\* Minimum beam width ( $b$ ) (Per ACI-Code).

shall not be less than 250 mm.

↳ Preferably = 300 mm.

\* General Strength Design Requirement for Beams.

$$\phi M_n \geq M_u$$

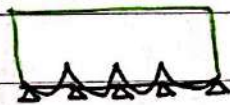
$$W_u = 1.2 D_L + 1.6 L_L \text{ or } W_u = 1.4 D_L$$

$$\phi M_n = \phi A_s f_y \underbrace{(d - a/2)}_{jd}$$

$$\phi M_n = \phi A_s f_y jd$$

$$\phi M_n = M_u$$

$$M_u = \phi A_s f_y jd \rightarrow A_s = \frac{M_u}{\phi f_y jd} \quad \left. \begin{array}{l} \text{when } b \text{ \& } h \text{ are known.} \\ \text{or } \end{array} \right\}$$

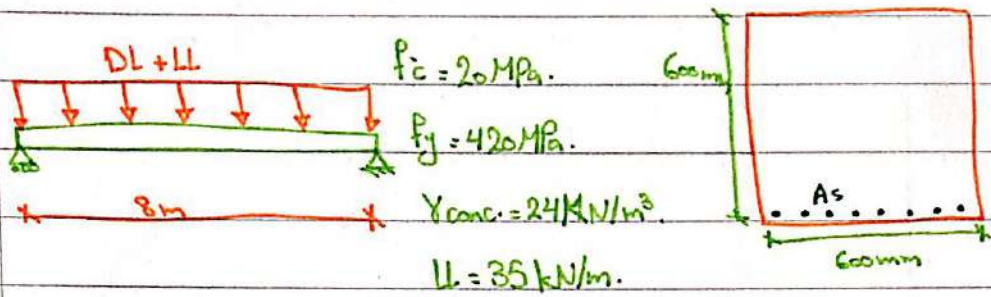


$$j = (.87 - .91)$$

$$\rightarrow j = \underline{0.9}$$

(26)

\*Example: Design of Reinforcement when b & h are known.



DL = 4 kN/m (excluding self wt. of the beam).

$$A_s = \frac{M_u}{\phi f_y j d} \rightarrow j d = d - \frac{a}{2}$$

$$.9 d = d - \frac{a}{2} \rightarrow a = .2 d$$

1] Estimate  $M_u$

$$M_u = \frac{W_u L^2}{8}$$

$$\text{Self wt.} = b h Y$$

$$= .6 \times .6 \times 24$$

$$= 8.64 \text{ kN/m}$$

$$W_u = 1.2 \text{ DL} + 1.6 \text{ LL}$$

$$= 1.2(8.64 + 4) + 1.6(35)$$

$$= 83.2 \text{ kN/m}$$

$$M_u = \frac{83.2 \times 8^2}{8} = 665.6 \text{ kN}\cdot\text{m}$$

2] Estimate  $d$ :

Assume 1 layer:

$$d = h - 65 \text{ mm} = 600 - 65 = 535 \text{ mm}$$

3] Check  $A_s \text{ min}$ :

$$\rightarrow 854 \text{ mm}^2$$

$$\rightarrow 1670 \text{ mm}^2 = A_s \text{ min}$$

4] Compare  $A_s$ :

$$A_s = \frac{665.2 \times 10^6}{.9(420)(.9)(535)} = 3657 \text{ mm}^2 > A_s \text{ min (ok)} \rightarrow \text{Iterations}$$

Iterations ↴

$$a = \frac{A_s f_y}{.85 f'_c b} = \frac{3657 \times 420}{.85(20)(600)} = 150.6 \text{ mm}$$

$$A_s = \frac{665.2 \times 10^6}{.9(420)(535 - \frac{150.6}{2})} = 3830.4 \text{ mm}^2$$

$$a = \frac{3830.4 \times 420}{.85(20)(600)} = 157.7 \text{ mm}$$

$$A_s = \frac{665.2 \times 10^6}{.9(420)(535 - \frac{157.7}{2})} = 3860.3 \text{ mm}^2$$

(27)

$$[a = 159 \text{ mm}, A_s = 3865.6 \text{ mm}^2] \rightarrow \text{Required.}$$

5] Select Steel: (اختار الحديد كبري، اختار 22)

$$8 \text{ No. } 25 \text{ M}; A_s = 4080 \text{ mm}^2. \text{ (القوية الأبر والأقرب لل Required)}$$

6] Check  $b_{min}$ :

$$b_{min} = 2(40) + 2(10) + 8(25) + 7(25) + 2(2(10)) - .5(25)$$

$$b_{min} = 490 \text{ mm} < b \rightarrow \text{One-layer (ok?)}$$

\* أنا بدي ال Check وبتوف ال 600، وحب ال  $b_{min}$  وبتقارن القتين في حال كانت  $b_{min}$  أكبر من ال  $b$ ، فخرج يكون عننا 2-layers، ولازم لدرج ال  $A_s$  من جديد، وبشكل نفس البر سير السابغ.

7] Analysis ( $\phi M_n > M_u$ ) ( $\phi = .9$ )  $\rightarrow$  مزون

$$a = \frac{4080 * 420}{.85(20)(600)} = 168 \text{ mm.}$$

$$c = \frac{a}{\beta} = 197.6 \text{ mm.}$$

$$E_s = .003 \left( \frac{535 - 197.6}{197.6} \right) = .00517 > .005 \text{ (Tension Controlled, } \phi = .9 \text{)}$$

(if it's not ok, we have to put  $A_s$ 's)

$$\phi M_n = .9(4080)(420) \left( \frac{535 - \frac{168}{2}}{2} \right) = 695.6 \text{ kN.m} > M_u \rightarrow \text{ok}$$

8] Check required  $A_s$  based on computed  $a$ : ( $j\delta = \delta - \frac{a}{2}$ )

$$(.9\delta = \delta - \frac{a}{2})$$

$$A_s = \frac{M_u}{\phi f_y (\delta - \frac{a}{2})} = \frac{665.6 * 10^6}{.9(420)(535 - \frac{168}{2})} = 3904 \text{ mm}^2.$$

↳ if it's not ok, we

<  $A_s$  provided (ok) will repeat all the example

$$h_{min} = \frac{l}{16} = \frac{8000}{16} = 500 \text{ mm} < 600 \text{ mm}$$

(No deflection).

deflection  $\rightarrow$   $\delta$

\* Design of rectangular beams. (When  $b, h$  &  $A_s$  are unknown).

$$\alpha = \frac{A_s f_y}{.85 f_c b} \quad (E_s \gg E_c).$$

$\rho$  (Percentage of reinforcement) "steel ratio"

$$\rho = \frac{A_s}{bd} \rightarrow A_s = \rho bd.$$

$$\alpha = \frac{\rho b d f_y}{.85 f_c b} \rightarrow \alpha = \rho \frac{f_y}{f_c} \cdot \frac{d}{.85}$$

$\rho$  (mechanical steel ratio).

$$\alpha = w \cdot \frac{d}{.85}$$

$$\phi M_n = \phi .85 f_c a b (d - \frac{a}{2})$$

$$\phi M_n = \phi [bd^2 f_c w (1 - .59w)] \rightarrow k_n, R_n$$

$\rightarrow$  flexural resistance factor.

$$\times M_u = \phi bd^2 k_n.$$

$$bd^2 = \frac{M_u}{\phi k_n} \rightarrow A_s = \frac{M_u}{\phi f_y j d}.$$

\* Estimating self wt. of rectangular beams.

17 The weight of the rectangular beams will roughly be 10 to 15% of the loads it must carry.

$$\text{Self wt.} = (10-15\%) (DL + LL).$$

21  $h \approx (\frac{1}{18} \text{ to } \frac{1}{12})$  of span length.  $\rightarrow$  only to estimate self weight.

$$b \approx .5h.$$

$$\text{Self wt.} = \gamma bh.$$

\* Selection of a steel ratio:

- Economic consideration: ( $\rho = .01$ ).

- Ductility Consideration:

$$0.35 \rho_b \leq \rho \leq 0.40 \rho_b$$

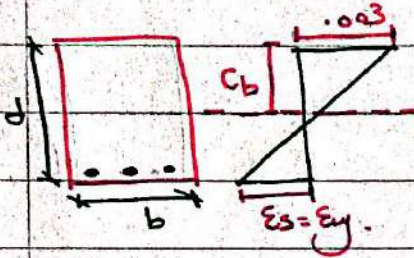
Balanced steel ratio:  $\rho_b = \frac{A_s b}{bd}$   $\rightarrow$  balanced area of steel.

(30)

\* Selection of  $\rho$ :

Ductility Consideration:

$$\rho = (.35 - .40) \rho_b$$



$$A_s b \rho_y = .85 f'_c a b$$

$$\rho_b d f_y = .85 f'_c \beta_1 c_b$$

$$c_b = \frac{\rho_b d f_y}{.85 f'_c \beta_1}$$

balance:

\* Strain Compatibility

$$\frac{.003}{c_b} = \frac{.003 + \epsilon_y}{d}$$

بسیار زیاد ہے

$$c_b = \frac{.003}{.003 + \epsilon_y} \times d$$

$$\rho_b = \frac{.85 \beta_1 f'_c}{f_y} \left( \frac{.003}{.003 + \epsilon_y} \right)$$

$$= \frac{.85 \beta_1 f'_c}{f_y} \left( \frac{600}{600 + f_y} \right)$$

$$= \frac{E}{E} \text{ في حال قریباً}$$

\* في حال ما انتكر شي، فيبداستقر (P) Economy.

\* By placing Consideration:

It may be hard to place the reinforcement if  $\rho$  exceeds .015

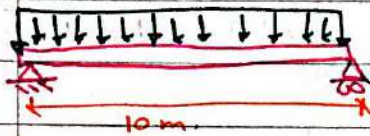
$$\rho = \frac{.24 \beta_1 f'_c}{f_y}, \quad \rho = \frac{\beta_1 f'_c}{4 f_y}$$

(31)



Example: Design of rectangular beam: ( $b, h$  &  $A_s$  are not known).

$w = DL \& LL$ .



$LL = 25.5 \text{ kN/m}$ .

$DL = 14.5 \text{ kN/m}$  (excluding self wt.)

$f'_c = 25 \text{ MPa}, f_y = 420 \text{ MPa}$ .

$$k_b d^2 = \frac{M_u}{\phi k_n} ; A_s = \frac{M_u}{\phi f_y j d}$$

1- Estimate self wt.

$$\begin{aligned} \text{I Self wt.} &= (10 - 15\%) (25.5 + 14.5) \\ &= (4.6) \text{ kN/m.} \end{aligned}$$

OR

$$\text{II } h \approx \left( \frac{1}{18} - \frac{1}{12} \right) \times 10,000 \quad \text{2- Compute } M_u:$$

$$\approx (555 - 833) \text{ mm.}$$

$$W_u = 1.2(14.5 + 8) + 1.6(25.5)$$

$$b \approx .5h \approx (275 - 415) \text{ mm}$$

$$W_u = 67.8 \text{ kN/m.}$$

$$\text{self wt.} = (3.66 - 8.3) \text{ kN/m.}$$

$$M_u = \frac{67.8 \times 10^2}{8} = 848 \text{ kNm.}$$

Try self wt. = 8 kN/m.

3-  $b$  &  $d$ .

$\rho = .01$  (economic consideration).

$$w = \rho \frac{f_y}{f'_c} = .01 \times \frac{420}{25} = .168$$

(32)

$$\phi k_n = .9 (25 \times .168 \times (1 - .59 \times .168))$$

$$\phi k_n = 3.41 \text{ MPa}$$

$$bd^2 = \frac{848 \times 10^6}{3.41} = 248.71 \times 10^6 \text{ mm}^3$$

Possible choices

(d > b)

$$b = 300 \text{ mm}; d = 910 \text{ mm}$$

$$b = 400 \text{ mm}; d = 788 \text{ mm} \checkmark$$

$$b = 450 \text{ mm}; d = 743 \text{ mm}$$

1. concept سبقت على ال

\* Assume 2 layers:

$$h = 788 + 90 = 878 \text{ mm} \approx 900 \text{ mm}$$

$$\underline{b = 400 \text{ mm}, h = 900 \text{ mm}, d = 810 \text{ mm}}$$

- Check self wt & revise  $M_u$  if required.

$$* \text{ Self wt. new} = \gamma b h$$

$$= 24(.4)(.9) = 8.64 \text{ kN/m}$$

لا تكافى بين تكافى البعد

$$W_{u \text{ new}} = 1.2(142 + 8.64) + 1.6 \times 25.5$$

لا تكافى بين تكافى البعد

$$= 68.57 \text{ kN/m}$$

$$M_{u \text{ new}} = \frac{68.57 \times 10^2}{8} = 857 \text{ kN}\cdot\text{m}$$

ACT-code \* IF  $M_u$  is increased by 10% or more repeat the design.

الابعاد الجديدة

$$\frac{857 - 848}{848} \times 100\% = 1.1\% < 10\% \rightarrow \text{Proceed using } M_u = 857 \text{ kN}\cdot\text{m}$$

(33)

$b = 400 \text{ mm}$ ,  $h = 900 \text{ mm}$ ,  $d = 810 \text{ mm}$  (Two-layers).

$M_u = 857 \text{ kN}\cdot\text{m}$ .

Select steel.

$$A_s = \frac{M_u}{\phi F_y d} = \frac{857 \times 10^6}{.9 \times 420 \times .9 \times 810} = 3110 \text{ mm}^2$$

7 No. 25M;  $A_s = 3570 \text{ mm}^2$ .

$$b_{min} = 2 \times 40 + 2 \times 10 + 7(25) + 6(25) + 2(20 + .5 \times 25)$$

$$b_{min} = 440 \text{ mm} > 400 \text{ mm}.$$

Iterations:

$$a = \frac{3110 \times 420}{.85 \times 25 \times 400} = 153.7 \text{ mm}.$$

Assumption is ok (2-layers).

$b_{min}$  (5 No. 25M)  $\rightarrow$  ok.

$$A_s = \frac{857 \times 10^6}{.9(420)(d - \frac{a}{2})} = 3092 \text{ mm}^2$$

check  $A_s$  min:

$$A_{smin} = \begin{cases} 964 \text{ mm}^2 \\ 1080 \text{ mm}^2 \end{cases}$$

$$A_{smin} = 1080 \text{ mm}^2$$

$$A_s = 3570 \text{ mm}^2 > A_{smin} \rightarrow \text{ok}$$

$$a = \frac{A_s \times 420}{.85 \times 25 \times 400} = 152.8 \text{ mm}.$$

$$A_s = \frac{857 \times 10^6}{.85 \times 25 (d - \frac{a}{2})} = 3090 \text{ mm}^2$$

$\phi = .9$ ,  $\phi M_n > M_u$ .

$$C = C_c$$

$$a = \frac{3570 \times 420}{.85 \times 25 \times 400} = 176.4 \text{ mm}.$$

$$C = \frac{a}{\beta_1} = 207.5 \text{ mm}.$$

$$E_s = .003 \left( \frac{810 - 207.5}{207.5} \right) = .0087 > .005 \quad (\phi = .9) \text{ (Tension controlled)}.$$

$$M_n = 357 \times 420 \times \left( \frac{810 - 176.4}{2} \right)$$

$$M_n = 1082 \text{ kN}\cdot\text{m}.$$

$$\phi M_n = 974 \text{ kN}\cdot\text{m} > M_u = 857 \text{ kN}\cdot\text{m} \rightarrow \text{ok}$$

$$A_{smax} = 5229.3 \text{ mm}^2.$$

(34)

Design Example:

600 mm

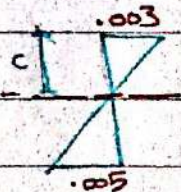
$M_u = 720 \text{ kN}\cdot\text{m}$

$f_c = 28 \text{ MPa}$

$f_y = 414 \text{ MPa}$

400 mm

Maximum Area of Tension Reinforcement:

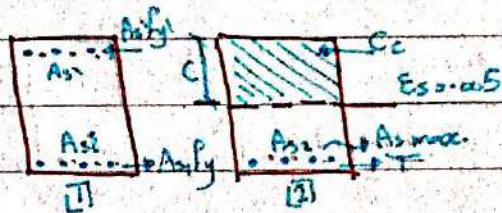


$A_{s \max} \rightarrow \epsilon_s = 0.005$

$A_{s \max} = 0.319 B_f \frac{f_c}{f_y} b d$

$A_s = \frac{M_u}{\phi f_y j d}$

Doubly reinforcement Beam:



assume 2-layers:

$d = 600 - 90 = 510 \text{ mm}$

$A_s = \frac{720 \times 10^3}{0.9 \times 414 \times 0.9 \times 510} = 4210 \text{ mm}^2$

$A_{s \max} = 0.319 (0.85) \frac{28}{414} \times 400 \times 510 = 3741 \text{ mm}^2$

$A_{s2} = A_{s \max} = 3741 \text{ mm}^2$

$T_2 = C_c \rightarrow \epsilon_s = 0.005$

$A_{s2} f_y = C_c + A_{s1} f_c + A_{s1} f_y$

$A_s > A_{s \max}$  (not tension controlled)

$\epsilon_s < 0.05 X$

Beam 2:

$T_2 = C_c$

$3741 \times 414 = 0.85 \times 28 \times a \times 400$

$a = 162.7 \text{ mm}, c = 191.4 \text{ mm}$

$\phi M_{n1} = M_u - \phi M_{n2} = 720 - 597.5 = 122.5 \text{ kN}\cdot\text{m}$

$\phi M_{n1} = \phi A_{s1} f_y (d - d')$

$122.5 \times 10^6 = 0.9 A_{s1} (414) (510 - 65)$

$A_{s1} = 728 \text{ mm}^2$

As check:

$\epsilon_s = 0.003 \left( \frac{510 - 191.4}{191.4} \right) = 0.005$

$\phi M_n = \phi A_{s2} f_y (d - \frac{a}{2})$

$= 0.9 (3741) (414) (510 - \frac{162.7}{2})$

$= 597.5 \text{ kN}\cdot\text{m}$

$A_s = A_{s1} + A_{s2} = 728 + 3741 = 4479 \text{ mm}^2$  (required)

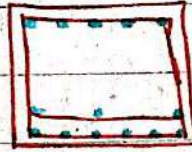
(35)

Select steel for  $A_s$ :

use 9 No. 25M,  $A_s = 4590 \text{ mm}^2$

$b_{min} = 540 \text{ mm} > 400 \rightarrow$  2-layers.

$b_{min} (6 \text{ No. } 25) \rightarrow \underline{\text{ok!}}$



$$A_{s1} = 4590 - 3741$$

$$= 849 \text{ mm}^2.$$

\* Beam 1:

$$T_1 = C_1$$

$$A_{s1} f_y = A_s' f_s'$$

$$E_s' = .03 \left( \frac{191.4 - 65}{191.4} \right)$$

$$= .00198 < \epsilon_y.$$

$$(849)(414) = A_s' \times .00198 \times 200 \times 10^3$$

$$A_s' = 900 \text{ mm}^2. \text{ (required)}$$

\* Select  $A_s'$

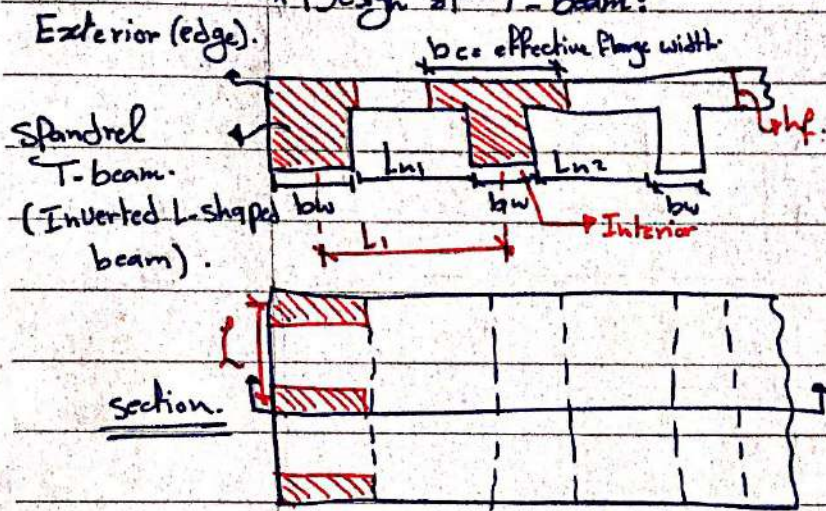
(5 No. 16M,  $A_s' = 995 \text{ mm}^2$ ).  $\rightarrow E_s = 200 \text{ GPa}$

$b_{min} =$

\* Complete Analysis.

(30)

\* Design of T-beam:

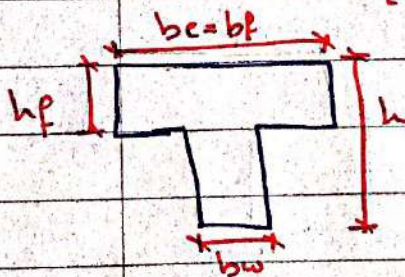


\* Spandrel T-beam:

$$b_c = \text{smaller of } \begin{cases} b_w + \frac{L_{n1}}{2} \\ b_w + 6h_f \\ b_w + \frac{L}{12} \end{cases}$$

\* Interior T-beam:

$$b_c = \text{smaller of } \begin{cases} b_w + \frac{L_{n1}}{2} + \frac{L_{n2}}{2} \\ b_w + 2(8h_f) \\ L/4 \end{cases}$$



\* I<sub>n</sub> design:

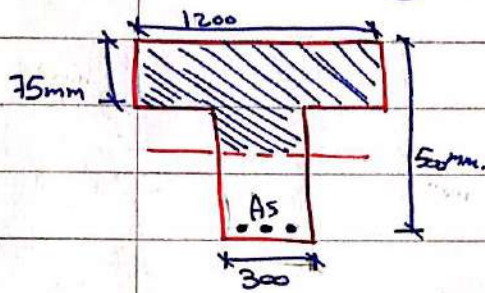
- Compression in web  $\rightarrow$  rectangular beam ( $j = .9$ )  
 $\rightarrow$  (Narrow comp. Areas)

- Compression in flange  $\rightarrow$  ( $j = .95$ ) (wide comp. areas)

$$A_s = \frac{M_u}{\phi f_y j d}$$

$j d =$  moment arm.

\* Exampk: Design of reinforcement.



$$A_s = \frac{740 \times 10^6}{(0.9)(420)(0.95)(500)} = 4121 \text{ mm}^2$$

\* Use 9 No. 25M;  $A_s = 4590 \text{ mm}^2$ .

- check  $A_{s \text{ min}}$ :

$$M_u (+ve) = 740 \text{ kN}\cdot\text{m}$$

$$f_c = 21 \text{ MPa}$$

$$f_y = 420 \text{ MPa}$$

$$\left. \begin{array}{l} 500 \text{ mm}^2 \\ 400 \text{ mm}^2 \end{array} \right\} \rightarrow A_s > A_{s \text{ min}} \text{ ok!}$$

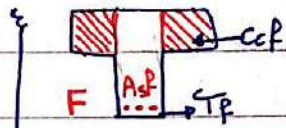
\*  $\phi M_n \geq M_u$  &  $\phi = 0.9$

$$a \leq h_f$$

$$C = T$$

$$0.85(21)a(1200) = 4590(420)$$

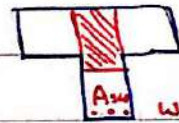
$$a = 90 \text{ mm} > h_f \rightarrow \text{T-beam}$$



$$T_f = C_f$$

$$A_{sf} = 2869 \text{ mm}^2$$

$$A_s = 4590 - 2869 = 1721 \text{ mm}^2$$



$$T_w = C_w$$

$$a = 135 \text{ mm}$$

$$c = 158.8 \text{ mm}$$

$$E_s = 0.003 \left( \frac{500 - 158.8}{158.8} \right) = 0.0064 > 0.005 \rightarrow \phi = 0.9$$

$$\phi M_n = \phi M_{nf} + \phi M_{nw}$$

$$\phi M_{nf} = 0.9 T_f (d - h_f/2) = 501.6 \text{ kN}\cdot\text{m}$$

provided:

$$\phi M_{nw} = 0.9 T_w (d - a/2) = 281.4 \text{ kN}\cdot\text{m}$$

$$\phi M_n = 783 \text{ kN}\cdot\text{m} > M_u = 740 \text{ kN}\cdot\text{m}$$

$\left. \begin{array}{l} \phi M_{nf} \\ \phi M_{nw} \end{array} \right\} A_s \text{ required} < A_s \text{ provided.}$

to check  $\phi M_n \geq M_u$  \* Check  $A_s$  required based on computed value of  $a$ :

$\phi M_n$

$$\phi M_n = \phi M_{nf} + \phi M_{nw}$$

$A_{sw}$

$$501.6 + \phi M_{nw} = 740$$

required:

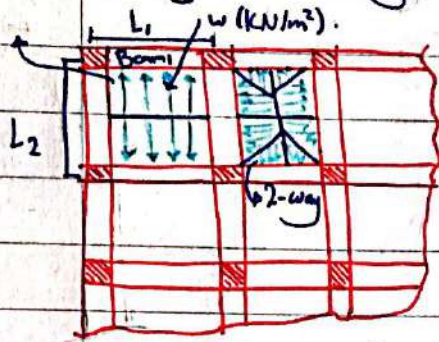
$$\phi M_{nw} = 238.4 \text{ kN}\cdot\text{m} < 281.4 \text{ kN}\cdot\text{m} \text{ (ok!)}$$

$$\frac{238.4 \times 10^6}{0.9(420)(500 - \frac{135}{2})} = 1458 \text{ mm}^2 < 1721 \text{ mm}^2 \text{ (ok!)}$$

(38)

\* Design of one-way solid slabs: (2D element).

Tributary Area for beam 1



$$\frac{L_1}{L_2} > 2$$

longer dimension  $\geq 2$  (one-way).  
shorter dimension

$w(\text{KN/m}^2) \times \frac{L_2}{2}$  → ...

منوع على  $L_1$

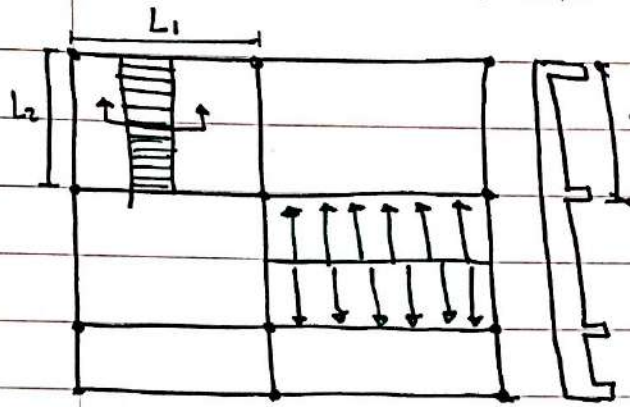
و عبء الأحمال التي ك (stiffness) ...

2-way → Non-uniform.

1-way → always uniform (always to short way).

(39)





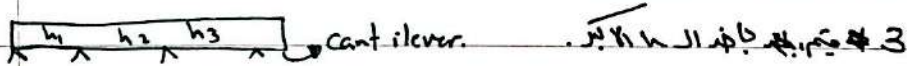
\* الاربعة اركان لا تتكبد  
 \* حالة ب 4 بيضاوي و طول 12 بيضاوي

$h_{min} = \frac{L}{28}$  → الحد الأدنى للارتفاع  
 في حال كانت أقل بارتفاع  $\frac{L}{28}$

$A_s = \frac{M_u}{B \cdot f_y \cdot j \cdot d}$   
 ← .95

\* Table 9.5A →  $h_{min}$ .

\* Cover = 20 mm (Normal).



\* ACI- Moment & Shear coefficients for analysis & design of non-prestressed one-way slabs & continuous beams:

$M_u = C_m \cdot w \cdot l_n^2$

$V_u = C_v \cdot \frac{w \cdot l_n}{2}$

	← $l_{n1}$ →			← $l_{n2}$ →			← $l_{n3}$
$C_m$	$\frac{1}{24}$	$\frac{1}{14}$	$\frac{1}{10}$	$\frac{1}{16}$	$\frac{1}{16}$	$\frac{1}{16}$	* in one end continuous $C_m = \text{Zero}$
$C_v$	1	1.5	1	1	1	1	

Girder supported by other beams.

(يعني لايه على بيضاوي و هاد البيضاوي على البيضاوي)  
 Logirder

\* Use # only if:

1. Two spans or more.
2. Spans are approximately equal Diff < 20%.
3. Loads are uniformly distributed.
4.  $LL \leq 3DL$
5. member are prismatic.

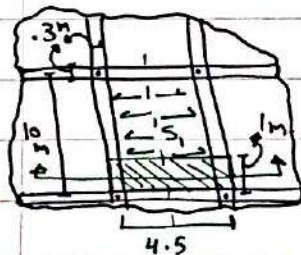
$$A_{s \min} = .0018bh \text{ (grade 60)}$$

$$A_{s \min} = .002bh \text{ (grade 40 or 50).}$$

$$s_{\min} \Rightarrow s = \frac{A_s}{.01 \cdot \frac{b}{bh}}$$

\* Design Example:

« نبتة كالتالي بالاجابة »



$$f_c = 28 \text{ MPa.}$$

$$DL = 3 \text{ kN/m}^2.$$

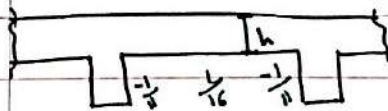
$$f_y = 414 \text{ MPa.}$$

(excluding self wt).

$$LL = 4 \text{ kN/m}^2.$$

$$\frac{10}{4.5} = 2.22 > 2 \rightarrow \text{one-way.}$$

∴ Estimate the thickness (h).



from center to center:

$$h_{\min} = \frac{L}{28} = \frac{4500}{28} = 160 \text{ mm. Use } h = 180 \text{ mm. (both end cont.)}$$

↓ To avoid deflection.

(41)

2) Estimate factored load :

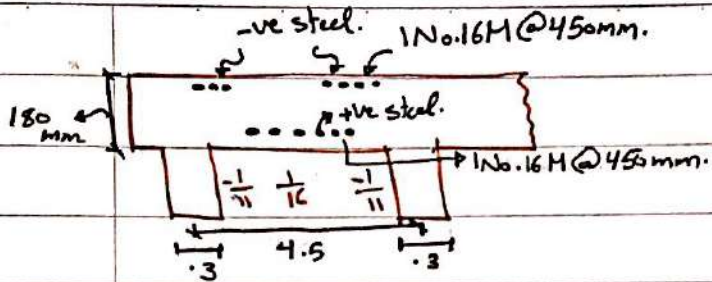
$$\text{Self wt} = 24 \text{ kN/m}^2 \times .18 = 4.32 \text{ kN/m}^2.$$

$$W_u = 1.2(3 + 4.32) + 1.6 \times 4 \\ = 15.18 \text{ kN/m}^2.$$

b=1 سب سے بڑا پاور اسٹیل

\* Cover min = 20mm. (Normal).

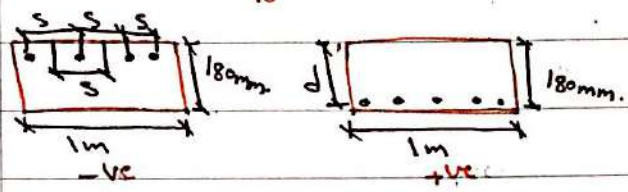
(42)



لا ما دافع عن، لحد  
و يبلغ ال Spacing

$$M_u(-ve) = 15.18 \times 4.2^2 = 24.34 \text{ kN.m}$$

$$M_u(+ve) = 15.18 \times 4.2^2 = 16.74 \text{ kN.m}$$



$$A_s = \frac{M_u}{\phi f_y j d}$$

بعد فترة ال s

Use No. 16M. steel,  $A_b = 199 \text{ mm}^2$

$$d = 180 - 20 - \frac{16}{2} = 152 \text{ mm}$$

1) Design for  $M_u(-ve)$ .

$$A_s = \frac{24.34 \times 10^6}{.9 (414) (.95) (152)} = 452.4 \text{ mm}^2/\text{m} \text{ (required)}$$

$$A_{s \text{ min}} = .0018 \times 1000 \times 180 = 324 \text{ mm}^2/\text{m}$$

$A_s > A_{s \text{ min}}$ .

$$a = \frac{452.4 \times 414}{.85 \times 28 \times 1000} = 7.87 \text{ mm}$$

$$A_s = \frac{24.34 \times 10^3}{.9 \times 420 \times (152 - \frac{7.87}{2})} = 441.2 \text{ mm}^2/\text{m}$$

$$a = 7.67 \text{ mm}, A_s = 440.9 \text{ mm}^2/\text{m}$$

$$c = 9 \text{ mm } E_s > .005 \rightarrow \phi = .9$$

$$E_s = .0177$$

$$S = \frac{1000 A_b}{A_s}, A_b = 1 \text{ No. } 16 \text{ M. (area of one bar)}$$

$$S \rightarrow A_b$$

$$1000 \rightarrow A_s$$

$$S = \frac{1000(199)}{440.9} = 451 \text{ mm} \rightarrow \text{تقریباً 450 mm.}$$

$$S_{\max} = \text{Smaller of } \begin{cases} 3h \\ 450 \text{ mm.} \end{cases}$$

$$3(180) = 540 \text{ mm.}$$

$$\therefore S_{\max} = 450 \text{ mm, use } S = 450 \text{ mm.}$$

$$\downarrow S = S_{\max} \rightarrow \text{ok.}$$

Design for  $M_u(+ve) = 16.74 \text{ kN}\cdot\text{m/m}$ .

$$A_s = \frac{16.74 \times 10^6}{.9 \times 114 \times .95 \times 152} = 311 \text{ mm}^2.$$

$$A_{s\min} = 324 \text{ mm}^2, A_s < A_{s\min} \rightarrow \text{Use } A_{s\min} \rightarrow \text{بما اني استوفيت } A_{s\min} \text{ فانا اتيه}$$

$$A_s = 324 \text{ mm}^2. \text{ (No iterations).}$$

في Tension (الشد) ما في داعي

و Es لا check ولا

Spacing:

$$S = \frac{1000 \times 199}{324} = 614 \text{ mm} \approx 600 \text{ mm.}$$

$$S_{\max} = 450 \text{ mm} > S \rightarrow \text{Use } S_{\max}.$$

$$S = 450 \text{ mm.}$$

Per ACI-code: Shrinkage & Temperature reinforcement is required perpendicular to the span of the slab

↳ (long-direction)

$$A_{s\min} = 324 \text{ mm}^2.$$

بنتقم جازيه الطولي (بالا اتجاه العزل) وبتنقسم بالـ 3 شقات

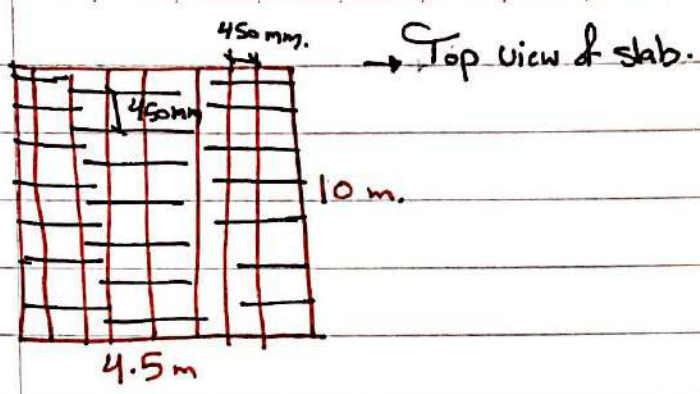
$$S = \frac{1000 \times 199}{324} = 614 \text{ mm.}$$

الموجودة في اللوحة بسبب تغير قسوة h. نبعط 450 mm

بما اني استوفيت  $A_{s\min}$  فانا اتيه

Shrinkage & Temp.  $\leftarrow S_{\max} = \text{Smaller of } \begin{cases} 5h \\ 450 \text{ mm.} \end{cases}$

$$5h = 5(180) = 900 \text{ mm.} / S_{\max} = 450 \text{ mm} > S, \text{ use } S = 450 \text{ mm.}$$

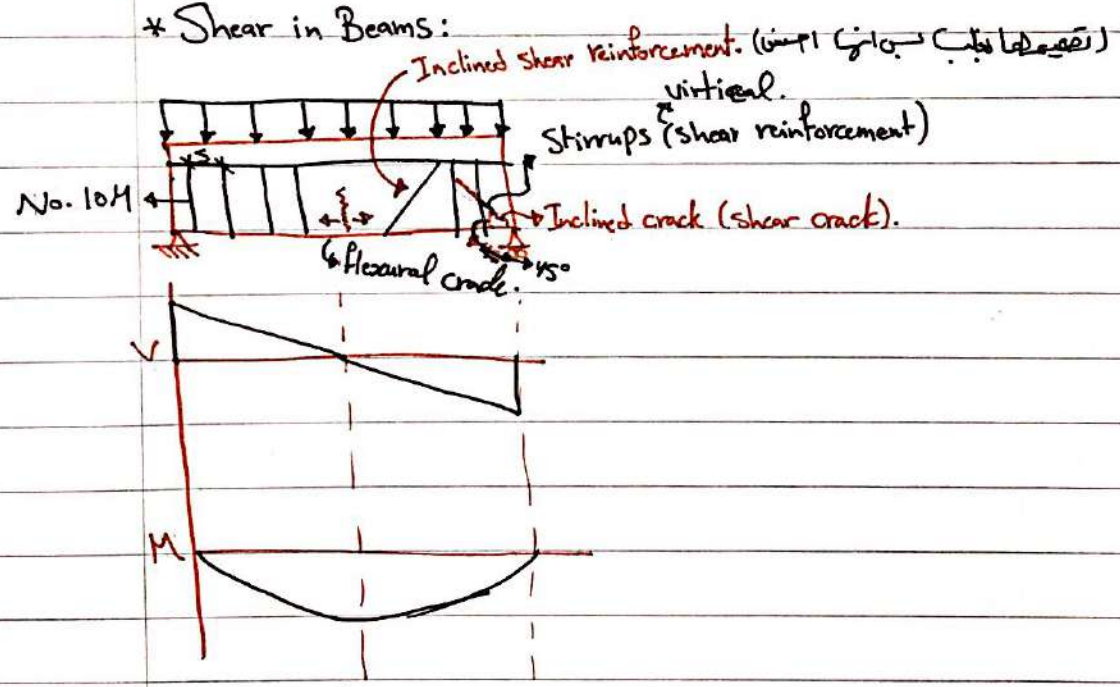


\* مثال طالكه بـ شوي صاري كتره لاني زودق كبر، نوع (نوع حجم الحديد).

No. 13M;  $A_b = 129 \text{ mm}^2$ .

$$S = \frac{1000 \times 129}{324} = \frac{129000}{324} = 398 \text{ mm.}$$

\* Shear in Beams:



\* Internal Forces in a beam:

$V_n = V_c + V_s \rightarrow$  Shear carried by stirrups.  
 $\hookrightarrow$  Shear carried by the conc.

→ dowel action of longitudinal steel <sup>DATE.</sup>

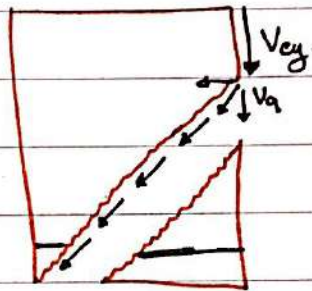
$$V_c = V_{cy} + V_{ay} + V_d$$

Shear in the uncracked conc. section.  $\int$  aggregate interlock on both face of the crack.

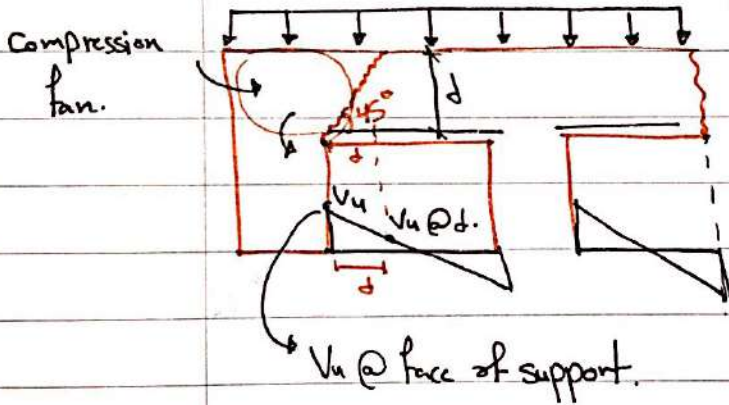
$$V_c = \frac{\sqrt{f_c}}{6} b_w d$$

$$\phi V_n \geq V_u$$

$\phi = 0.75$



\* Location of max. Shear for design of RC Beams ( $V_n$ ) [Critical section].



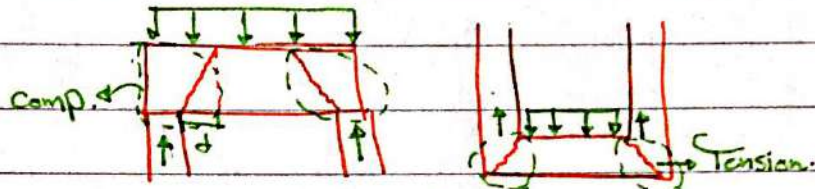
(46)

$$\phi V_n \geq V_u$$

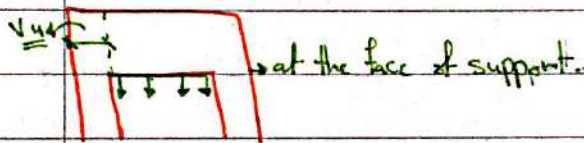
@ face.

@ d from face of support: use only if:

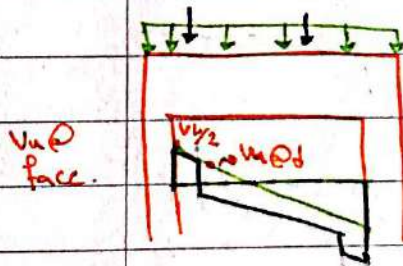
1) Support reaction introduces compression into the end region of the beam.



2) loads are applied on the top of the beam:



3) No concentrated force within a distance  $\frac{d}{2}$  from face of support.



### Analysis & Design of R.C Beams for Shear.

$$\phi V_n \geq V_u$$

$$V_n = V_c + V_s$$

$$V_c = \frac{1}{6} \sqrt{f_c} b w d$$

$$\phi V_n = V_u$$

$$\phi V_n = \phi (V_c + V_s) = V_u$$

$$V_s = \frac{V_u}{\phi} - V_c$$

Case I:  $V_u \leq \frac{\phi V_c}{2}$

No need for shear reinforcement.

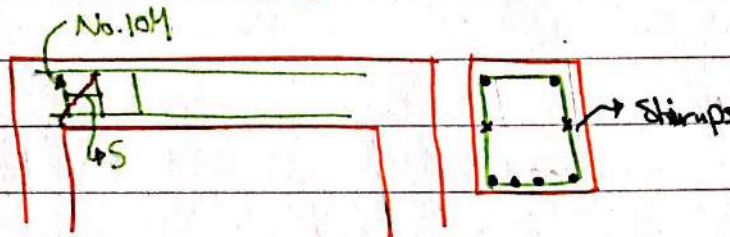


Case II:  $\frac{\phi V_c}{2} < V_u \leq \phi V_c$ .

Use minimum shear reinforcement.

$S_{max} = \text{smaller of } \frac{16 A_v f_y}{\sqrt{f_c} b w}$

$\frac{V_p f_c b w}{A_v f_y} (\approx 33 b w)$  → مورطون قديم  
 $d/2$  → عان الا انة تا الى main shear  
 600mm.



$A_v = 2 A_{v1}$

↳ Cross sectional area for one bar (stirrups).

Case III:  $V_u > \phi V_c$  ;  $V_s \leq \frac{2 \sqrt{f_c} b w d}{3}$

$S_{max} = \text{smaller of } \frac{16 A_v f_y}{\sqrt{f_c} b w}$  &  $\frac{A_v f_y d}{V_s}$  → min

هناك قيم بالاتان  
 ودرجتها من Case II

$V_s \leq \frac{1}{3} \sqrt{f_c} b w d$  →  $d/2$   
 600mm.

$V_s > \frac{1}{3} \sqrt{f_c} b w d$  →  $d/4$   
 300mm.

If  $V_s > 4 V_c$   
 ↳ Enlarge the section.

$V_s \text{ max} = 4 V_c = \frac{2}{3} \sqrt{f_c} b w d$

$M_u = C_m W_u L_n^2$  ← تكون L طولية، الكونست مع تصميم بالبرهان.

$V_u = C_v W_u L_n / 2$  ← وازا كانت مقربة، بالبرهان، ليس مع تصميم.

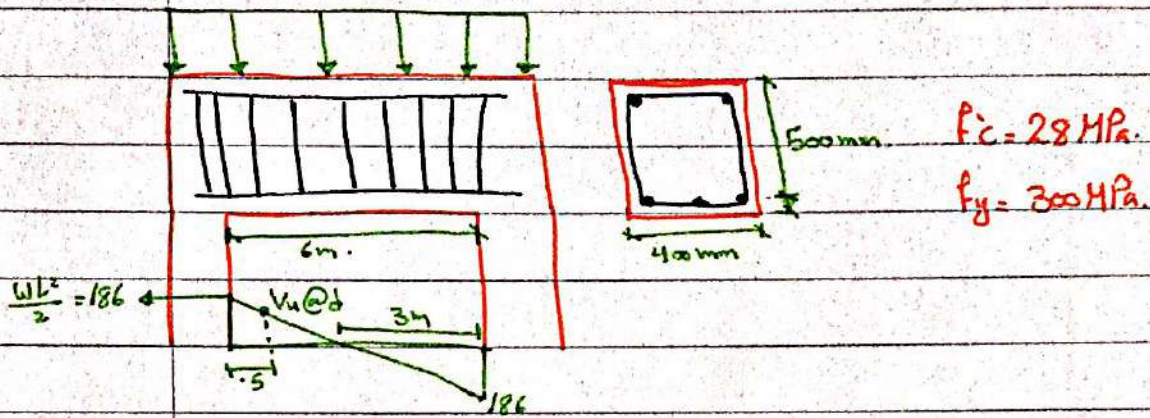
$V_u \text{ max} = \phi (V_c + V_s \text{ max})$

$V_u \text{ max} = \phi 5 V_c$  → check بعد بالبرهان ان كان اشرف الـ conc

آلية اولاً

Example.

$U_L = 20 \text{ kN/m}$ ,  $D_L = 25 \text{ kN/m}$ .



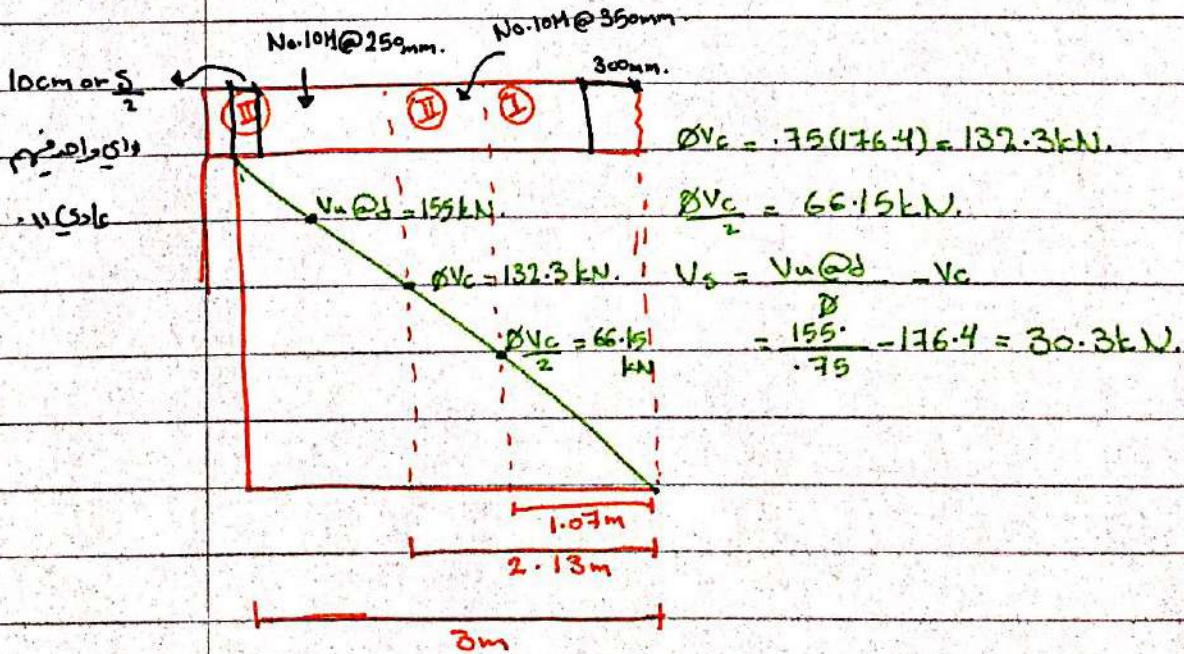
$$W_u = 1.2(25) + (1.6)(20) = 62 \text{ kN/m}$$

$$V_u @ d = 155 \text{ kN} \rightarrow \text{OK OK OK}$$

$$V_c = \frac{1}{6} \sqrt{f_c} (400)(500) = 176.4 \text{ kN}$$

$$V_{u \max} = (0.75)(5)(176.4) = 661.4 \text{ kN}$$

$155 < V_{u \max}$ . (Section is OK)



Case III:  $V_u > \phi V_c$  &  $V_s < 4V_c$  //  $V_s < 2V_c$ .

$S_{max} = \text{Smaller of } \left\{ \begin{array}{l} \frac{A_v f_y d}{V_s} = \frac{157 \times 300 \times 600}{30.3 \times 10^3} = 777 \text{ mm.} \\ \frac{16 A_v f_y}{\sqrt{F_c} b_w} = \frac{16 (157) (300)}{\sqrt{28} (400)} = 356 \text{ mm.} \\ \frac{A_v f_y}{.33 b_w} = \frac{157 (300)}{(0.33) (400)} = 356.8 \text{ mm.} \\ \frac{s}{2} = \frac{500}{2} = 250 \text{ mm.} \\ 600 \text{ mm.} \end{array} \right.$

$S = 250 \text{ mm.}$

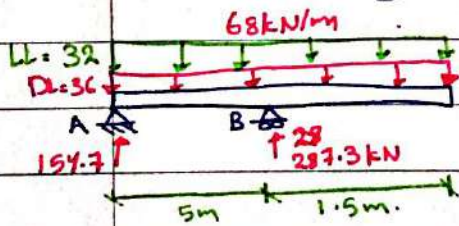
$A_v = 2 \text{ No. } 10M = 157 \text{ mm}^2$

Case II:  $\frac{\phi V_c}{2} < V_u < \phi V_c$ .

↳ Minimum shear reinforcement.

$\left\{ \begin{array}{l} 356 \text{ mm.} \\ 356.8 \text{ mm.} \\ 250 \text{ mm.} \\ 600 \text{ mm.} \end{array} \right. \quad S = 250 \text{ mm.}$

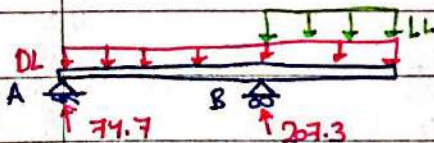
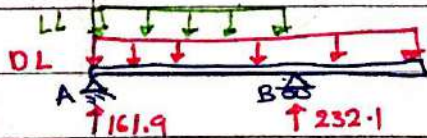
(with & without) \* Cases of loading:



$DL = 30 \text{ kN/m} \times 1.2 = 36 \text{ kN/m.}$

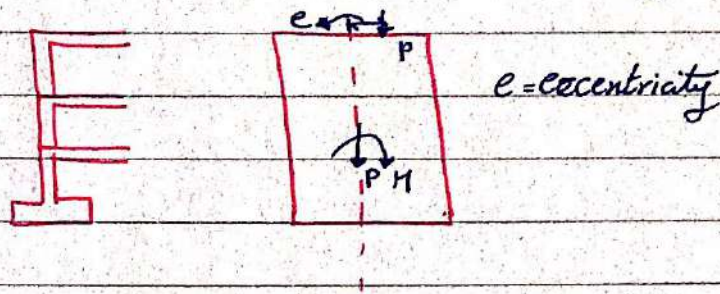
$LL = 20 \times 1.6 = 32 \text{ kN/m.}$

$LL + DL = 68 \text{ kN/m.}$



(50)

\* Columns: Combined Axial Load & Bending:



\* Columns:

- 1] Short
- 2] Slender

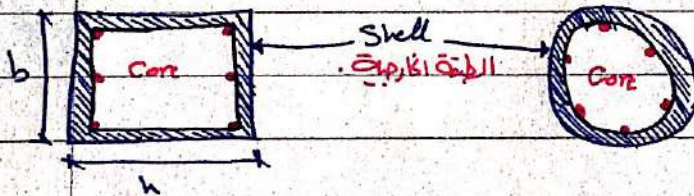


lateral deflection.  
(Buckling).

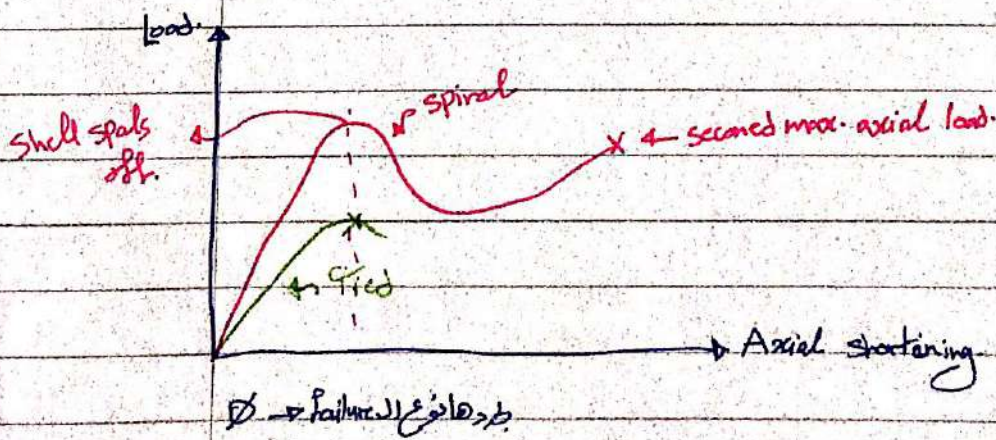
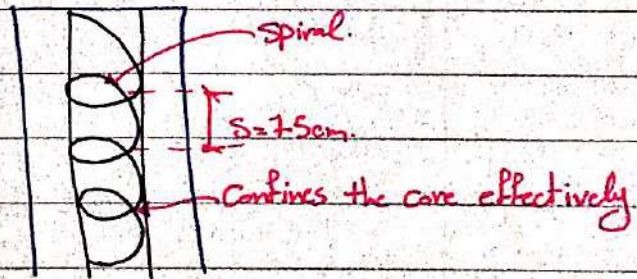
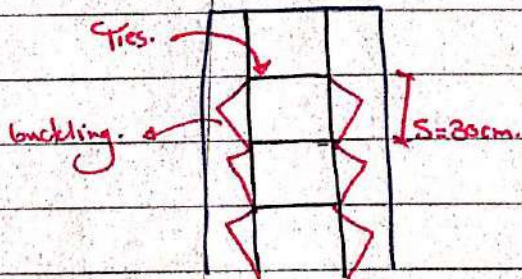
\* Types of columns:

1] Tied Column. ( $\phi = .65$ )

2] Spiral Column. ( $\phi = .75$ ).

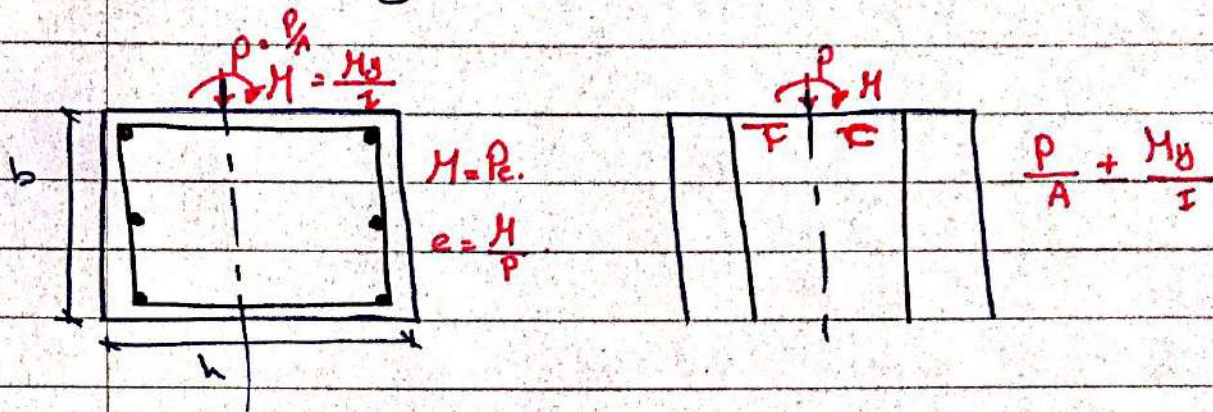


[95% of chms are tied].



(5)

\* Interaction Diagram: (I.D).



$$\text{Comp.} = \frac{P}{A} + \frac{My}{I} = f_{cu} \rightarrow \text{compression strength.}$$

$$\frac{P}{f_{cu} A} + \frac{My}{f_{cu} I} = 1.$$

IF  $M=0 \rightarrow \frac{P}{f_{cu} A} = 1 \rightarrow P = f_{cu} A = P_{max}$

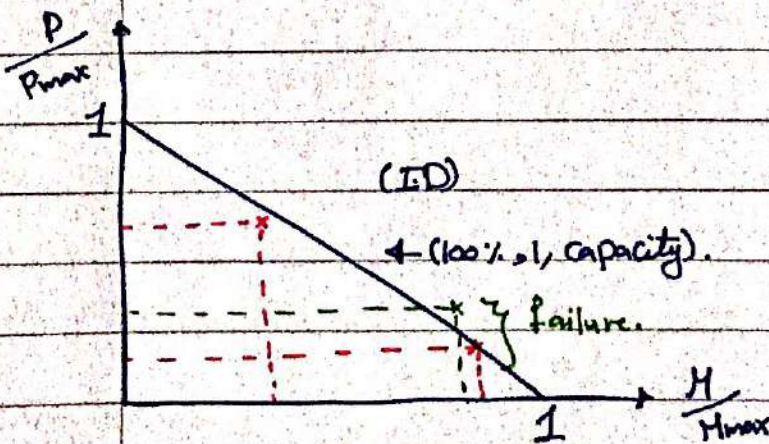
↳ Maximum axial load the moment can support.

IF  $P=0 \rightarrow \frac{My}{I f_{cu}} = 1 \rightarrow M = \frac{f_{cu} I}{y} = M_{max}$

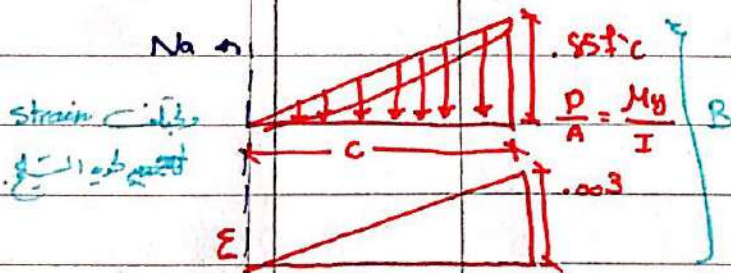
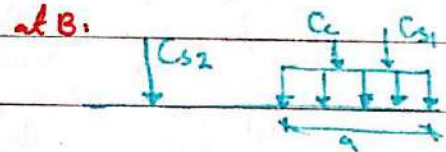
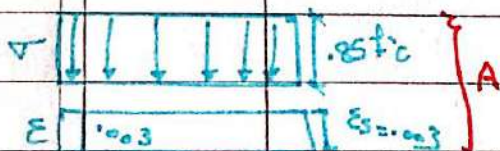
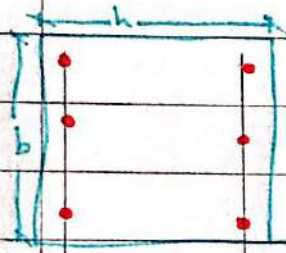
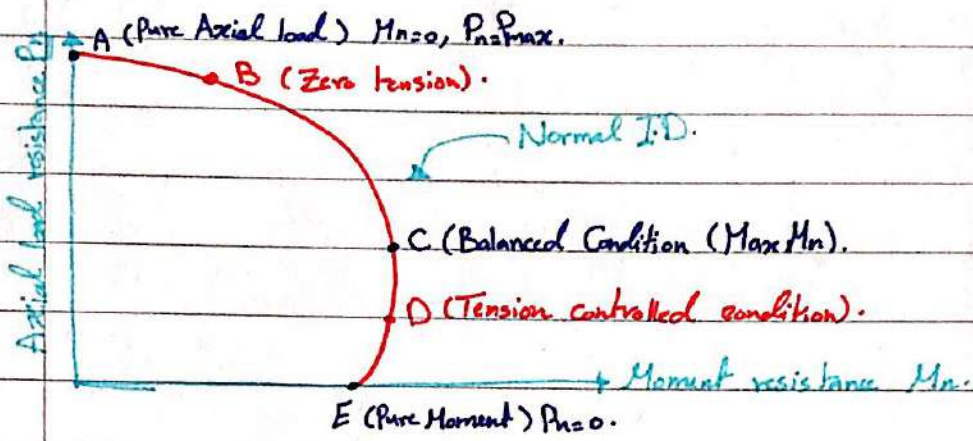
↳ Maximum moment the columns can support.

$$\frac{P}{P_{max} \cdot A} + \frac{My}{M_{max} \cdot I} = 1$$

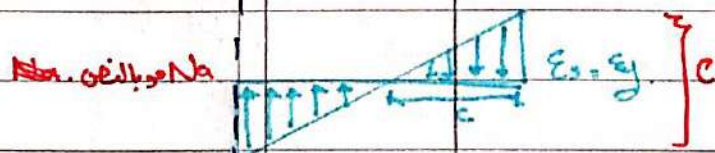
$$\frac{P}{P_{max}} + \frac{M}{M_{max}} = 1 \text{ (Interaction Equation).}$$



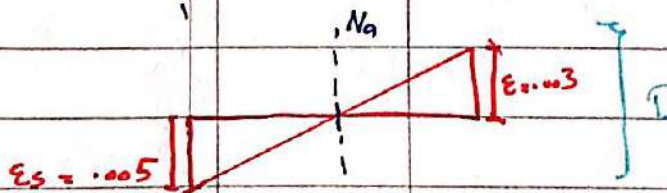
I:D for concrete:



Point A: (Zero tension)  $\epsilon_s = 0$   
 $P_n = 0.85f_c (A_g - A_s) + A_s f_y$   
 $A_g$ : Cross sectional area ( $b \times h$ )

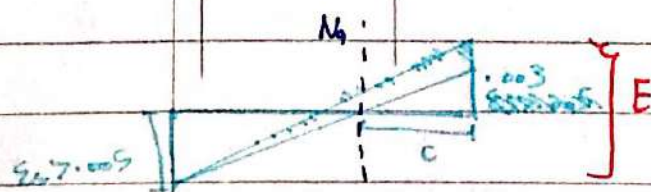


Zero  $\epsilon_s$  at B



Zero  $\epsilon_s$  at B

at Point B:  
 $c = h$  ;  $P_n = C_c + C_{s1} + C_{s2}$



at Point C:  
 $\epsilon_{s1} = \epsilon_y$  ;  $P_n = C_c + C_{s2} - T_{s1}$

at Point D:

$$\epsilon_s = .005$$

at Point E:

Like a beam.

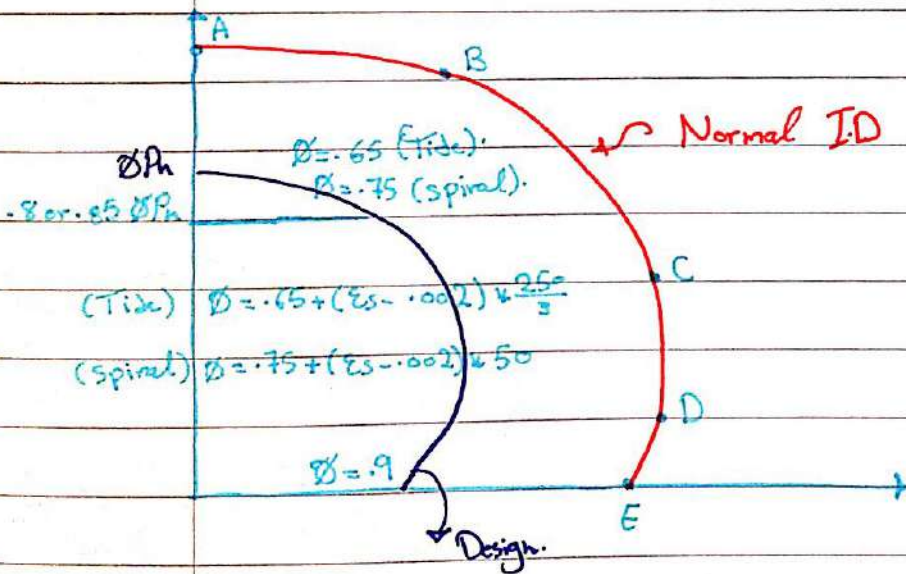
\* Maximum Axial Load:

$$\phi P_n = \phi P_{n, max} = \phi [ .85 f'_c (A_g - A_s) + A_s f_y ]$$

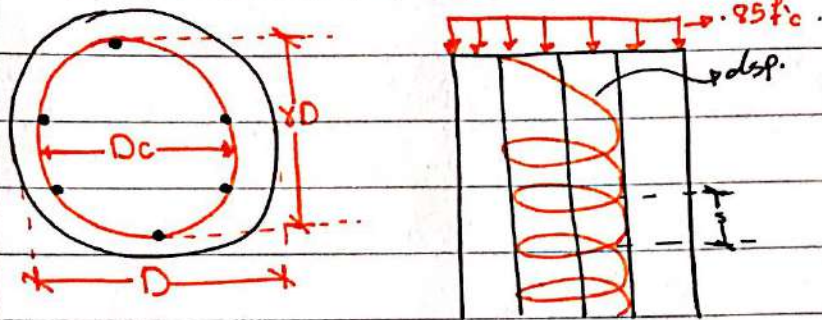
\* In Order to account the effect of accidental Moments:

The ACI ~~code~~ specifies that the max load on:

- On a spiral column must not exceeds 85% of it's strength. ( $\phi P_{n, max} \times .85$ )
- On a tie column must not exceeds 80% of it's strength. ( $.8 \phi P_{n, max}$ ).



\* في حالة عادية  
 في حالة E حيث ان  $\phi = .9$  في حالة سبيل  
 \* في حالة عادية  $(.85 \phi P_n)$  سبيل و  $(.8 \phi P_n)$  Tide  
 \* في حالة سبيل  $(.8 \phi P_n)$  سبيل  
 \* في حالة سبيل  $(.8 \phi P_n)$  سبيل



$$S_{max} \leq \frac{\pi d_{sp}^2 f_y}{.45 D_c F_c \left( \frac{A_g}{A_c} - 1 \right)}$$

$\frac{\pi D_c^2}{4}$  → Core diameter (out to out of spiral).  
 $\frac{\pi D_c^2}{4}$

$S_{max} \leq 75 \text{ mm.}$

$S_{min} = \text{larger of:}$

↳ 25 mm

↳ 1.33 max. size of CA.

\*  $S_{max}$  → To confine the core effectively.

\*  $S_{min}$  → To avoid problems in conc. placing.

\* Design of tied columns:

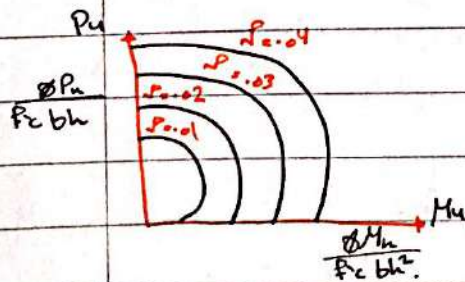
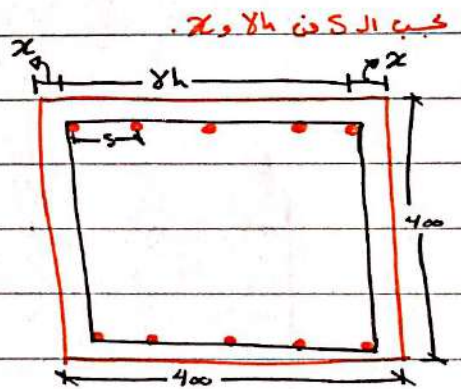
$P_u = 1550 \text{ kN}; M_u = 150 \text{ kN.m.}$

$f_c = 20 \text{ MPa}; f_y = 420 \text{ MPa.}$

$b \times h \leftarrow A_g \geq \frac{P_u}{.4(f_c + .8 f_y)} = \frac{1550 \times 10^3}{.4(20 + .8 \times 420)}$

$A_g = 147338 \text{ mm}^2$  (Square col.)

$b = h = 384 \text{ mm}; \text{ use } 400 \times 400 \text{ mm.}$



→ في بعض الحالات قد يكون  
... في بعض الحالات



$$I:D = \gamma = .6 \rightarrow \rho = .033$$

$$I:D = \gamma = .75 \rightarrow \rho = .028$$

use No. 25M;

$$x = 40 + 10 + \frac{25}{2} = 62.5 \text{ mm.}$$

$$\gamma h + 2x = 400$$

$$\gamma = .69$$

by iterations,  $\rho = .03$

\* If  $\rho$  exceeds 3-4%  $\rightarrow$  large section should be chosen.

\*  $\rho_{min} = .01$

$$\rho = .03 \rightarrow \underline{\text{ok}} \quad ; \quad \rho > \rho_{min} \rightarrow \underline{\text{ok}}$$

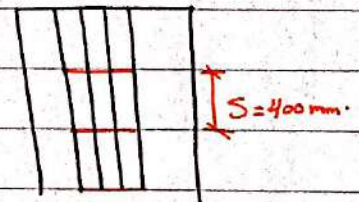
$$A_s = \rho b h = .03 \times 400 \times 400 = 4800 \text{ mm}^2 \text{ (required).}$$

$$10 \text{ No. 25M}; A_s = 5100 \text{ mm}^2$$

\* Spacing for ties:

$$\text{smaller of: } \begin{cases} 16d_p = 16 \times 25 = 400 \text{ mm.} \\ 48d_t = 48 \times 10 = 480 \text{ mm.} \end{cases}$$

$$b = 400 \text{ mm.}$$



$$S_{min} = \text{larger of: } \begin{cases} 40 \text{ mm.} \\ 1.5d_p = 1.5 \times 25 = 37.5 \text{ mm.} \end{cases}$$

$$S_{min} \leq 150 \text{ mm.}$$

\* Spiral جيب تال على ال spiral

\* Development; Anchorage & Splicing of Reinforcement.

\* Development length ( $L_d$ ): Is the shortest length of bar in which the bar stress can increase from zero to  $f_y$ .

\* If the distance from a point where the bar stress equals  $f_y$  to the end of the bar is less than ( $L_d$ ), the bar will pull out of the concrete.

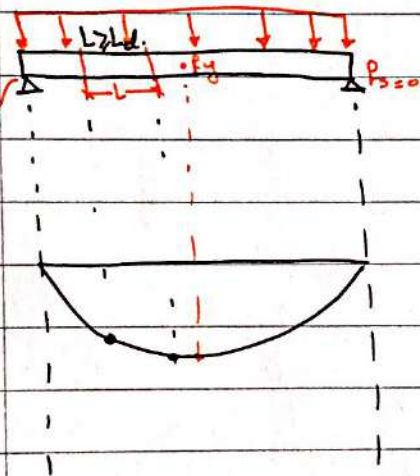
توازن بين القوى

$P_s = F_{res}$

$P_y = M_{max}$

$P_{s0}$

↳ Not enough bond stress to produce Equilibrium.



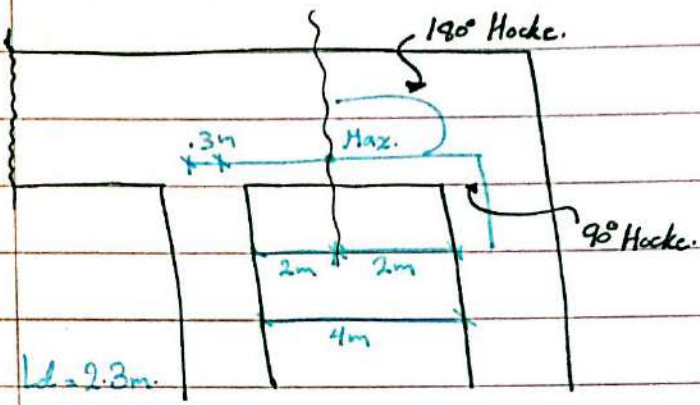
↳  $M_{avg} = A_{vg} \cdot \text{bond stress}$ .

$T_1 + M_{avg} = T_2$

$T_1 \neq T_2 \rightarrow \dots$

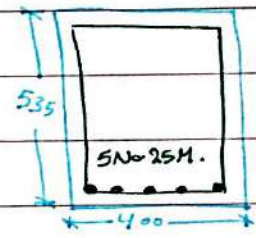
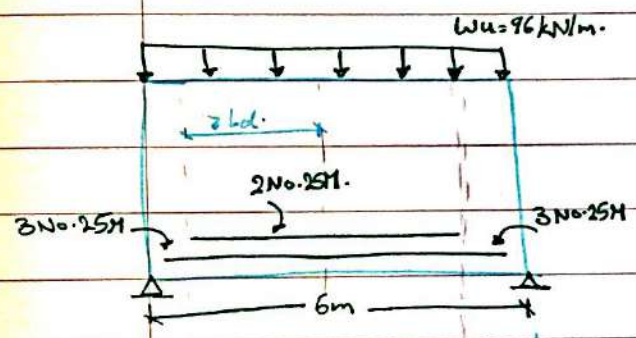
\* الـ  $T_1$  و  $T_2$  بيكونان متساويين من الطرفين

\* equilibrium (توازن) بين القوى

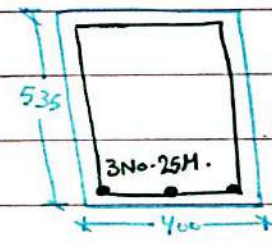
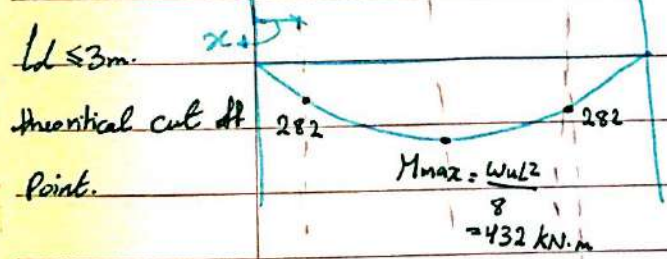


Hooks & Anchorage

\* Example : (Bar cut off).

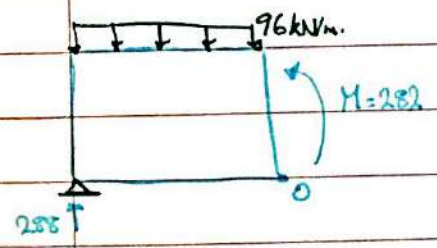


$M_u = 440 \text{ kN}\cdot\text{m}$   
↳  $\rho_{min} \leq \rho \leq \rho_{max}$



$M_u = 282 \text{ kN}\cdot\text{m}$   
فوق  $M_u$  و  $\rho_{min}$  و  $\rho_{max}$  و  $\rho_{min}$  و  $\rho_{max}$  و  $\rho_{min}$  و  $\rho_{max}$

\* cut off two bars.



$M = 282$   
 $\sum M_o = 0 ; x = 1.23m$   
use  $x = 1.25m$